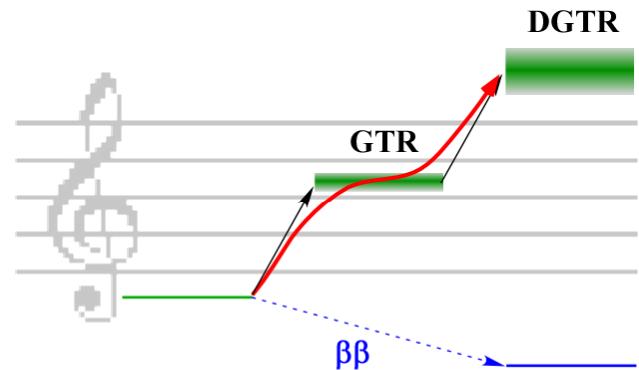


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# Double-beta decay matrix elements and charge exchange reactions

M. Sasano, Spin-Isospin Laboratory, RIKEN Nishina Center  
K. Yako, Center for Nuclear Physics, University of Tokyo

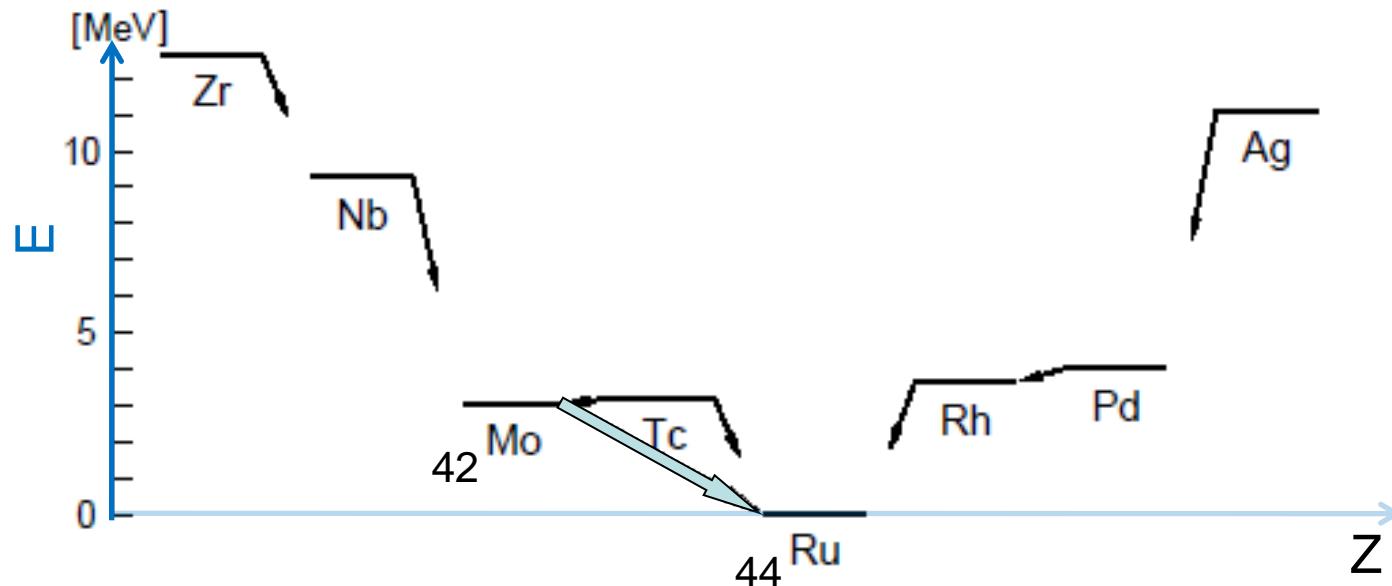


# Double beta decay

## Double beta decay (DBD):

decay process where a nucleus releases  
two beta rays as a single process

example:  $A = 100$  ( $^{100}\text{Mo}$ )



DBD nuclei (studied so far):

$^{48}\text{Ca}$ ,  $^{76}\text{Ge}$ ,  $^{82}\text{Se}$ ,  $^{96}\text{Zr}$ ,  $^{100}\text{Mo}$ ,  $^{128}\text{Te}$ ,  $^{130}\text{Te}$ ,  $^{136}\text{Xe}$ ,  $^{150}\text{Nd}$ ,  $^{238}\text{U}$

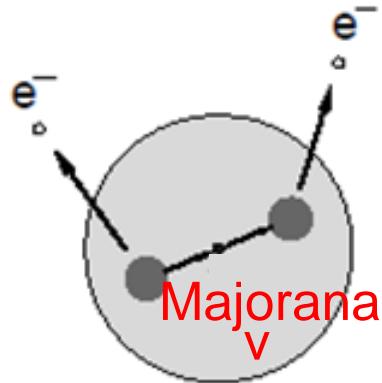
# Two modes

forbidden in  
“standard” model

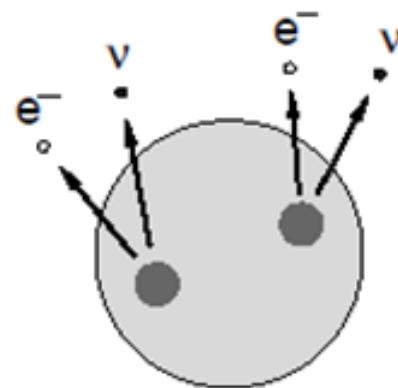
DBD

- 0v mode  $(A, Z) \rightarrow (A, Z + 2) + 2e^-$
- 2v mode  $(A, Z) \rightarrow (A, Z + 2) + 2e^- + 2\bar{\nu}_e$

0v mode



2v mode



0v event ...

→  $\nu$  is Majorana particle.

→ absolute mass is deduced from  
the half life. ...mass hierarchy

→ origin of matter / antimatter imbalance?

→ ...

# Nuclear Matrix Elements

... $0\nu$  DBD occurs in nucleus

- second order process
- intermediate states:
  - g.s.
  - other states of various  $J^\pi$ .

$0\nu$  life time and  $\nu$  mass

$$\left(T_{1/2}^{0\nu}\right)^{-1} = G^{0\nu} \langle m_\nu \rangle^2 |M_{\text{DGT}}^{0\nu} - M_{\text{DF}}^{0\nu}|^2 + \dots$$

Phase space / weak coupling      “nuclear matrix element” (NME)

nuclear structure calculation  
Shell model, RPA, ...

NME is important!

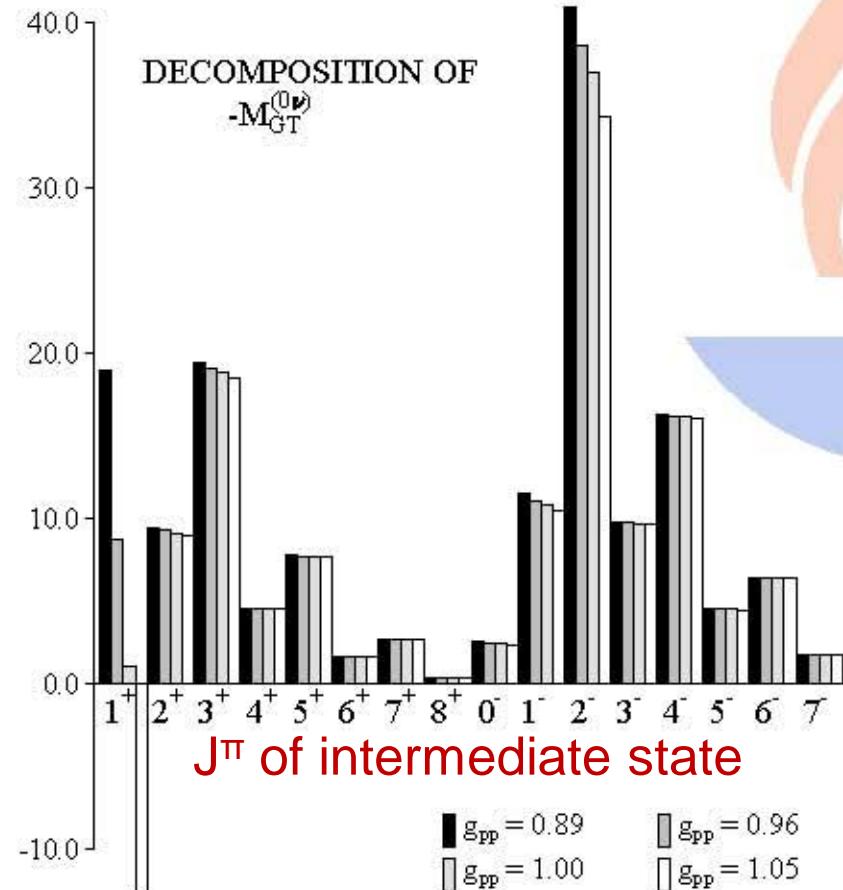
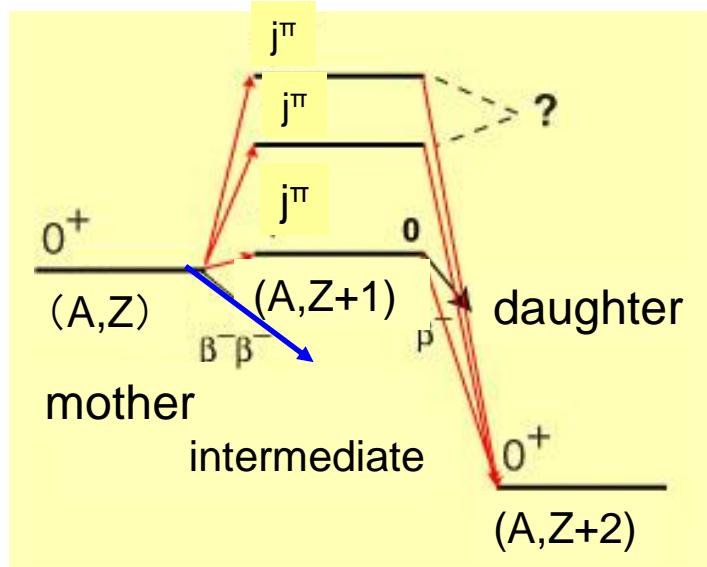
- analysis ... absolute mass / mass limit of  $\nu$
- search planning ... which nucleus is the best candidate?

# $0\nu\beta\beta$ Matrix Element: Decomposition in the pnQRPA

$$M_{\text{GT}}^{(0\nu)} = \sum_{J^\pi} M_{\text{GT}}^{(0\nu)}(J^\pi),$$

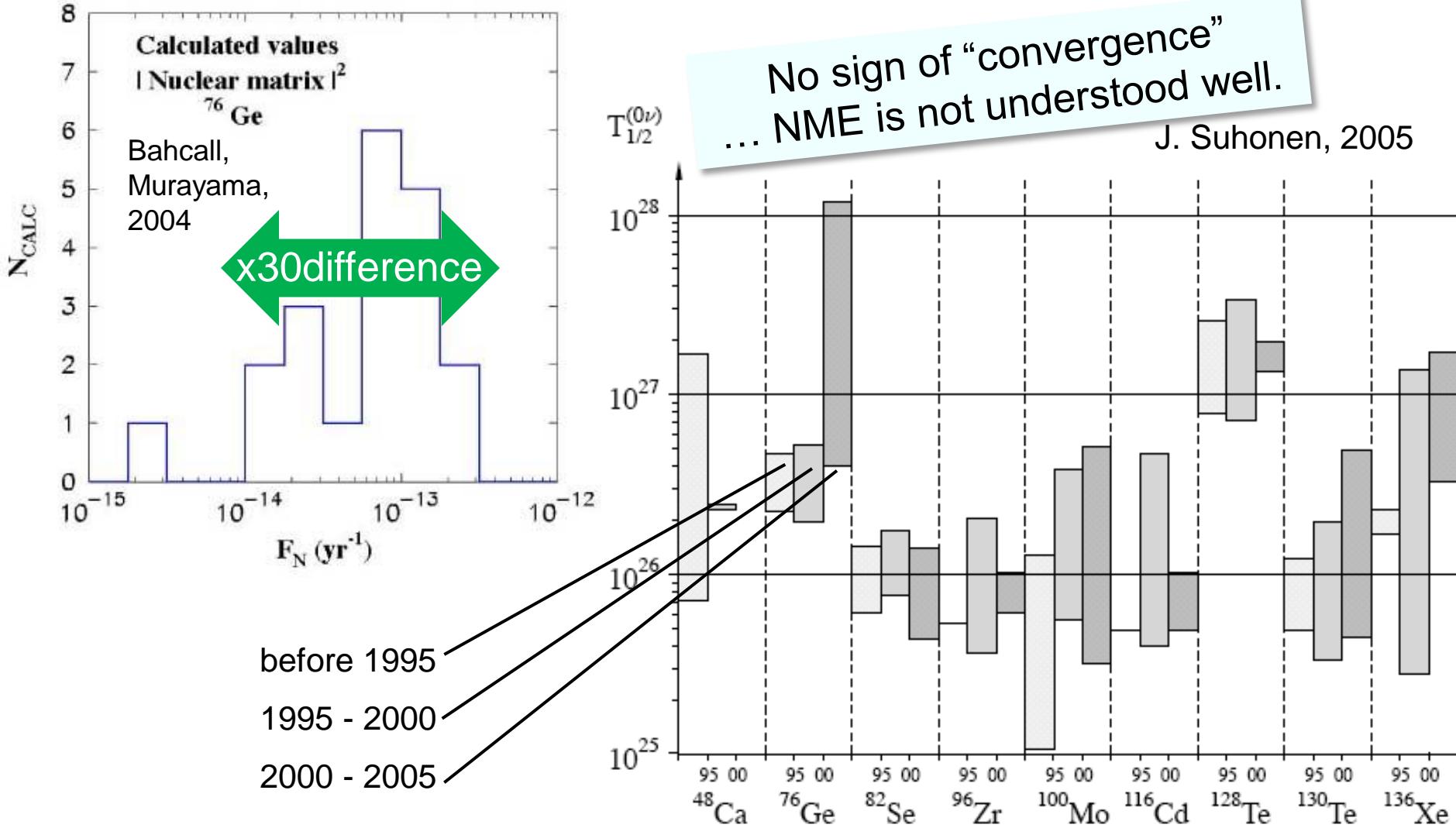
Suhonen, 2005

$$\begin{aligned} M_{\text{GT}}^{(0\nu)}(J^\pi) &= \sum_{n\lambda} (0_f^+ \parallel \sum_j [\sigma_j F_\lambda(\mathbf{r}_j)]_J t_j^- \parallel J^\pi n) \\ &\times (J^\pi n \parallel \sum_j [\sigma_j F_\lambda(\mathbf{r}_j)]_J t_j^- \parallel 0_i^+) \end{aligned}$$



# Reliability of NME (2005)

Ex)  $^{76}\text{Ge}$



# Constraints on the calculations

## step1 first order transitions

- Single  $\beta^-$  &  $\beta^+$  rates
- $2\nu$ -DBD rate

## step2 ground states

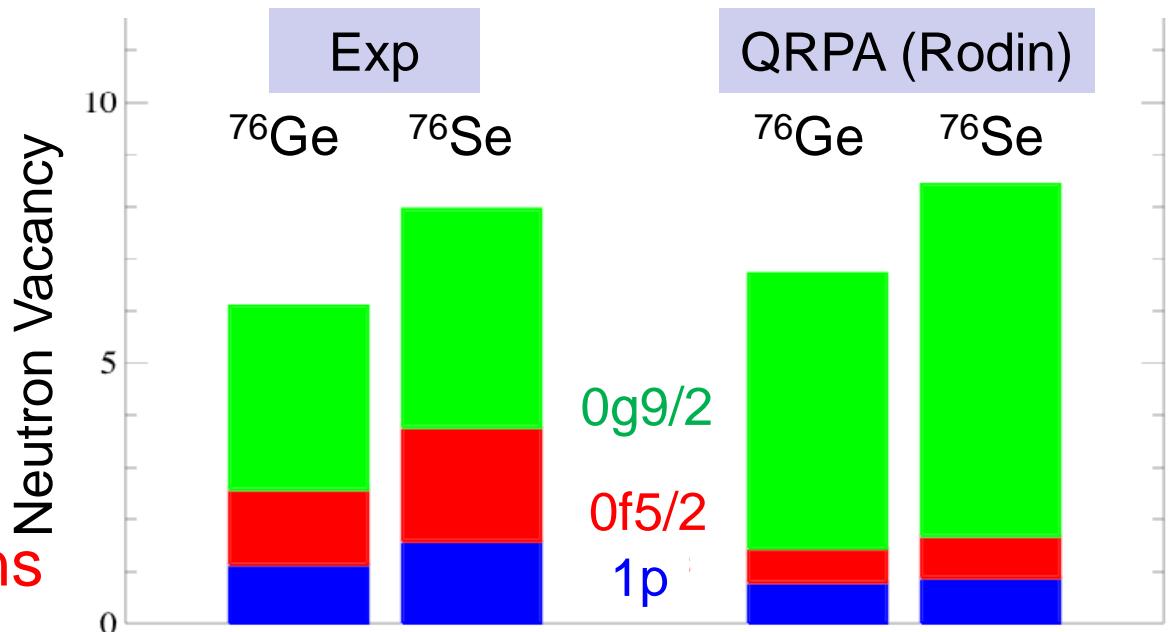
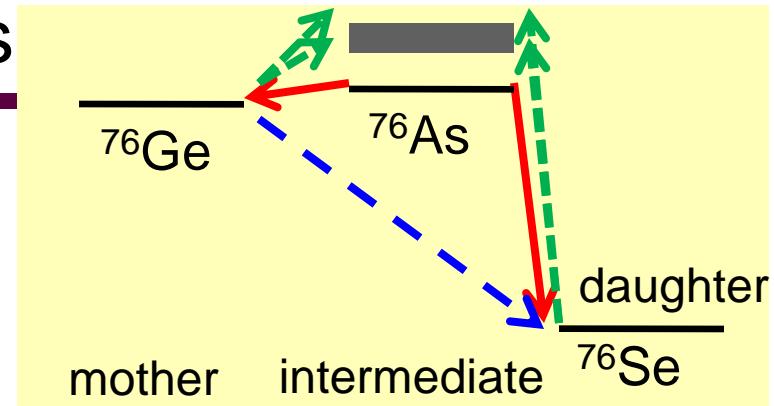
- Occupation numbers of “valence” nucleons:  
 $(d,p)$ ,  $(p,d)$ ,  
 $(\alpha, {}^3He)$ ,  $({}^3He,\alpha)$

Extra g.s. correlation is necessary.

## step3 relevant transitions

- $\beta$ -type transitions:  
energy, strength, ...

mother → intermediate → daughter



Kay, Schiffer et al., 2009

Our work:  
Gamow-Teller ( $1^+$ )  
( $\Delta L=0$ ,  $\Delta S=\Delta T=1$ )

# GT transitions and 2v-DBD

## 2v $\beta\beta$ decay

$$(A, Z) \rightarrow (A, Z+2) + 2e^- + 2\bar{\nu}_e$$

- second order weak process
- rarest process confirmed so far
- if thoroughly understood,  
it helps analysis of 0v $\beta\beta$  decay rate.

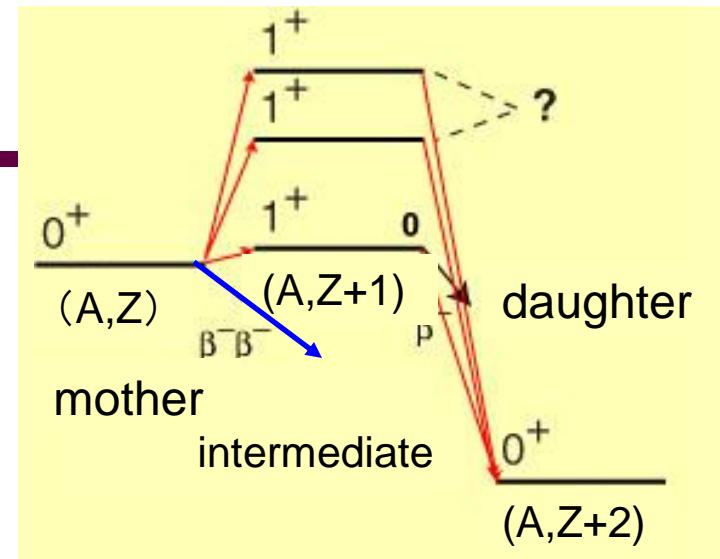
## Half-life and matrix element:

$$\left(T_{1/2}^{2\nu}\right)^{-1} = G^{2\nu} \left|M_{\text{DGT}}^{2\nu}\right|^2$$

$$M_{\text{DGT}}^{2\nu} = \sum_m \frac{\langle f | O_{\text{GT-}} | m \rangle \langle m | O_{\text{GT-}} | i \rangle}{E_m - (M_i + M_f)/2}$$

GT operator:  $O_{\text{GT}\pm} = \sum_j \sigma_j t_\pm$

GT strength:  $B(\text{GT}^\pm) = \left| \langle j | O_{\text{GT}\pm} | i \rangle \right|^2$

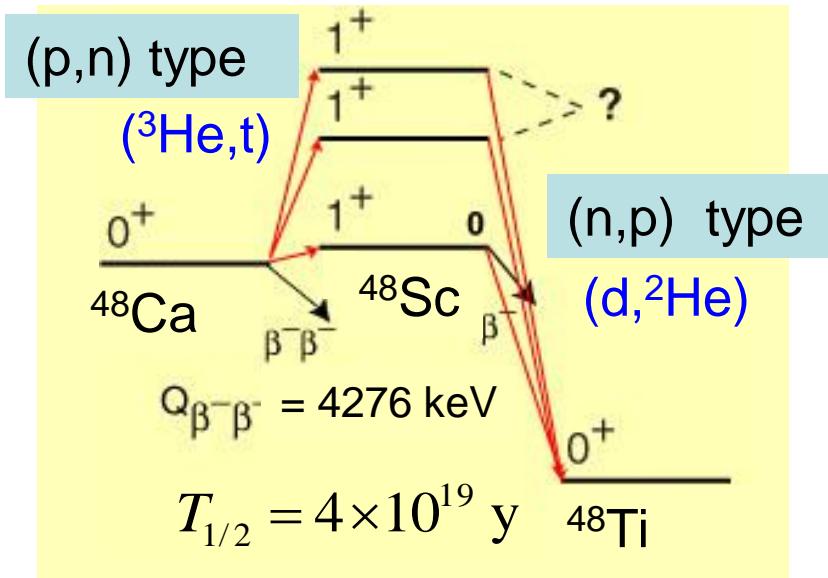


Half lives ... not understood well  
 Suhonen et al., PR300(1998)123

Nucleus	Exp T <sub>1/2</sub> (y)	Calc T <sub>1/2</sub> (y)
<sup>48</sup> Ca	$\sim 4.3 \times 10^{19}$	$(1.3 - 6.0) \times 10^{19}$
<sup>76</sup> Ge	$\sim 1.4 \times 10^{21}$	$(0.8 - 1.4) \times 10^{21}$
<sup>82</sup> Se	$\sim 0.9 \times 10^{20}$	$(0.1 - 1.1) \times 10^{20}$
<sup>96</sup> Zr	$\sim 2.1 \times 10^{19}$	$(3.0 - 11) \times 10^{19}$
<sup>100</sup> Mo	$\sim 8.0 \times 10^{18}$	$(1.7 - 32) \times 10^{18}$
<sup>116</sup> Cd	$\sim 3.3 \times 10^{19}$	$(5.1 - 10) \times 10^{19}$
<sup>128</sup> Te	$\sim 2.5 \times 10^{24}$	$(0.6 - 37) \times 10^{24}$
<sup>130</sup> Te	$\sim 0.9 \times 10^{21}$	$(0.3 - 2.7) \times 10^{21}$
<sup>150</sup> Nd	$\sim 7.0 \times 10^{18}$	$(6.7 - 27) \times 10^{18}$

## B(GT) in low-lying states

## GT strengths:

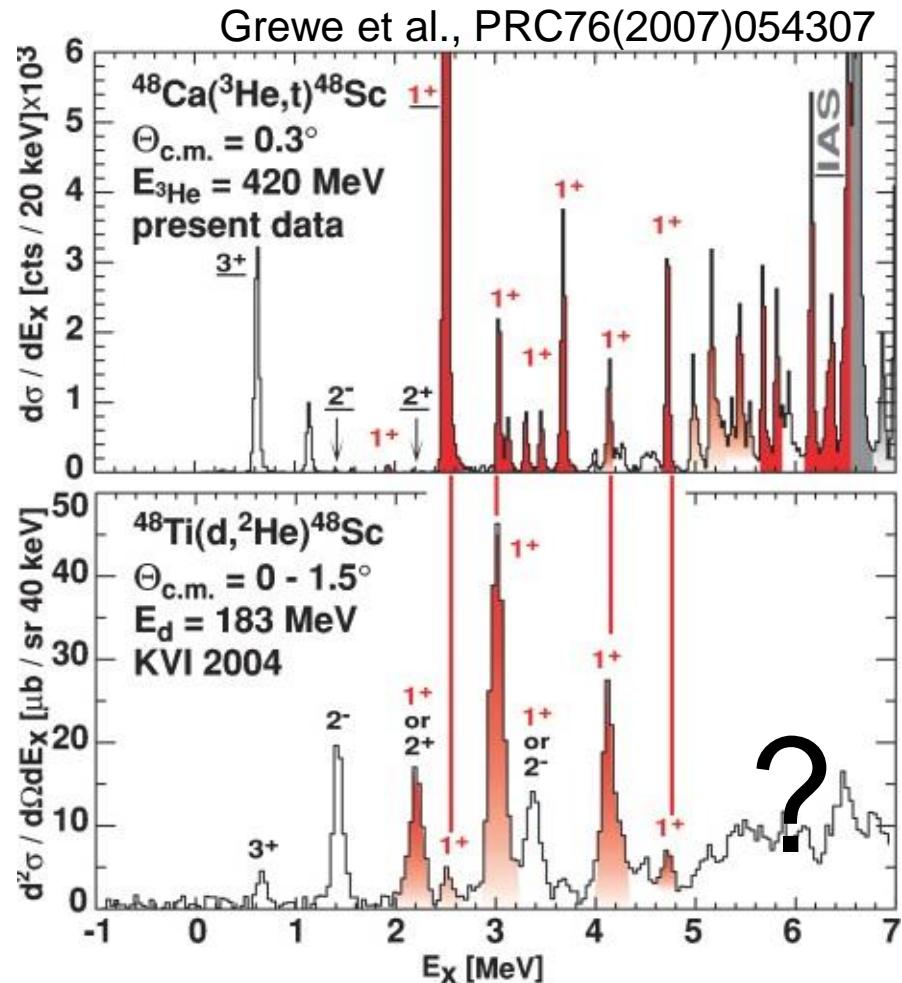


## Low lying states

... high resolution measurements

## <sup>48</sup>Ca(<sup>3</sup>He,t) @ 140A MeV (RCNP)

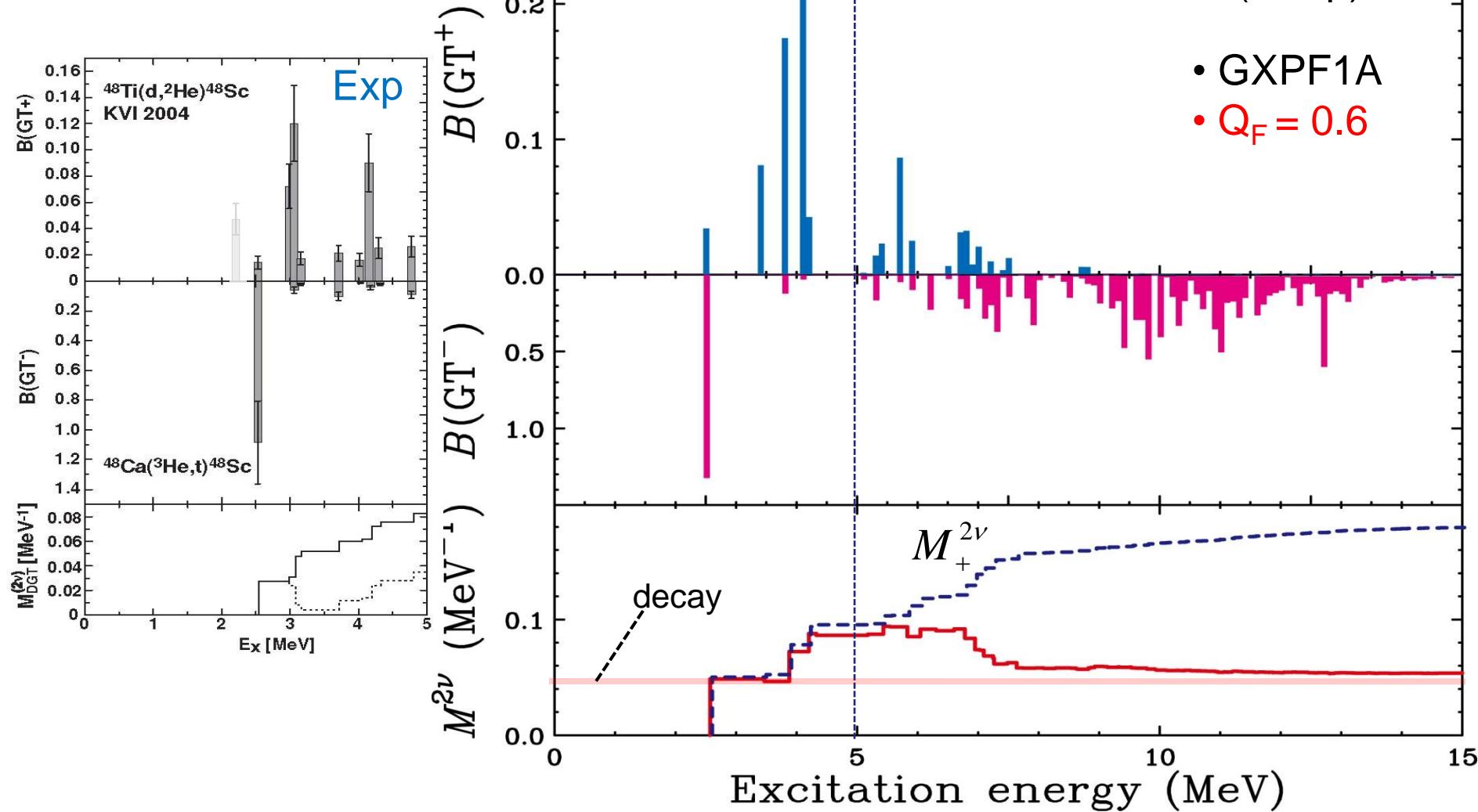
## $^{48}\text{Ti}(\text{d},^2\text{He})$ @ 90A MeV (KVI)



# Current understanding by shell model

Same as Horoi et al.  
PRC75(2007)034303

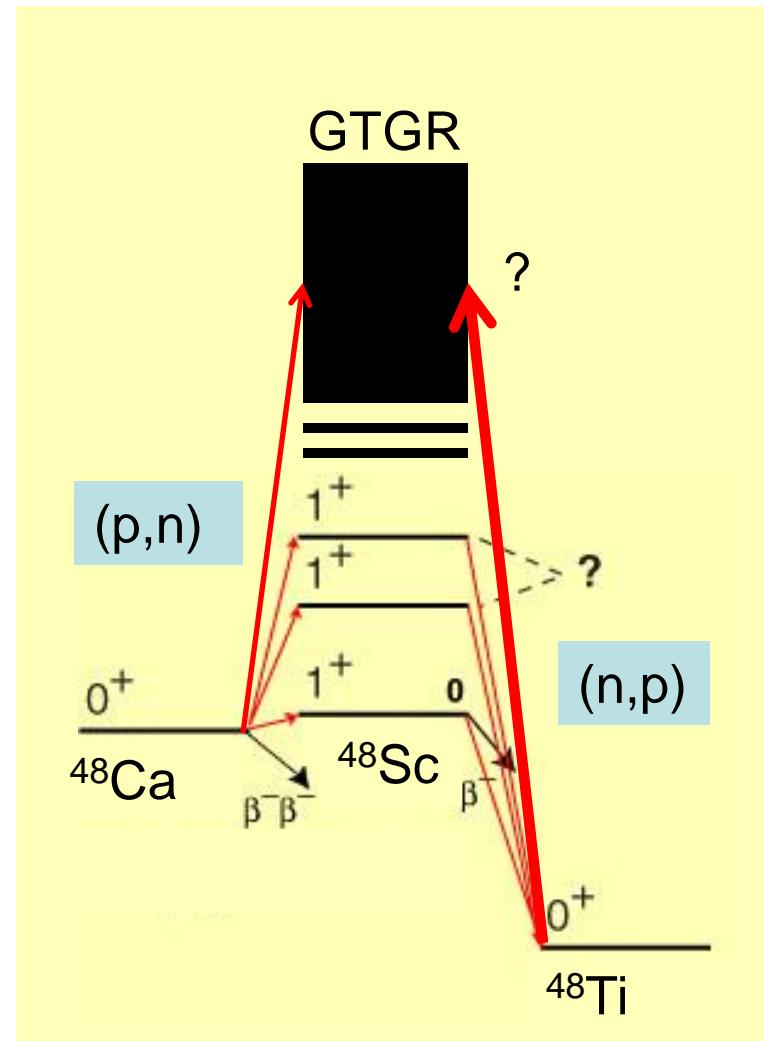
Shell model calculation  
... reasonable.



# Aim

- If your strategy is to check or constrain the theoretical calculations, you need the full snapshots of the  $B(GT)$  distribution.
- $B(GT^{+/-})$  distributions were studied up to the continuum, in the intermediate nuclei,  $^{48}\text{Sc}$ ,  $^{116}\text{In}$ .
- Measurement
  - $E_{\text{beam}} = 300 \text{ MeV}$
  - $\theta = 0^\circ \sim 12^\circ$

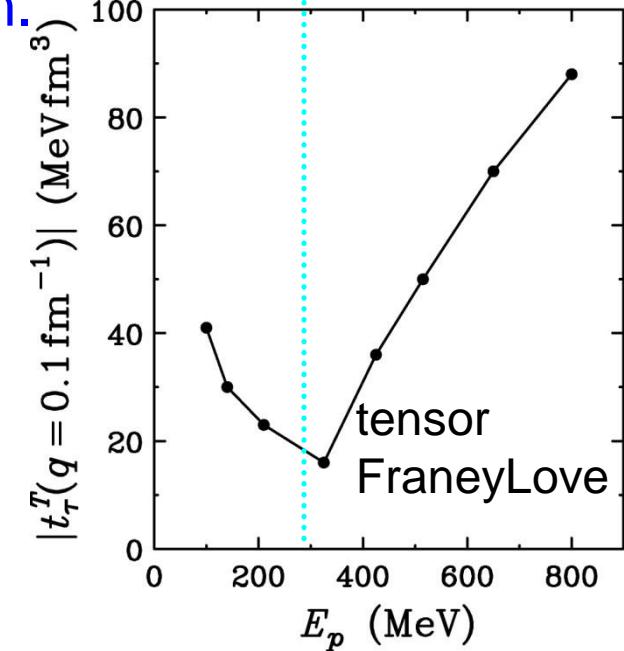
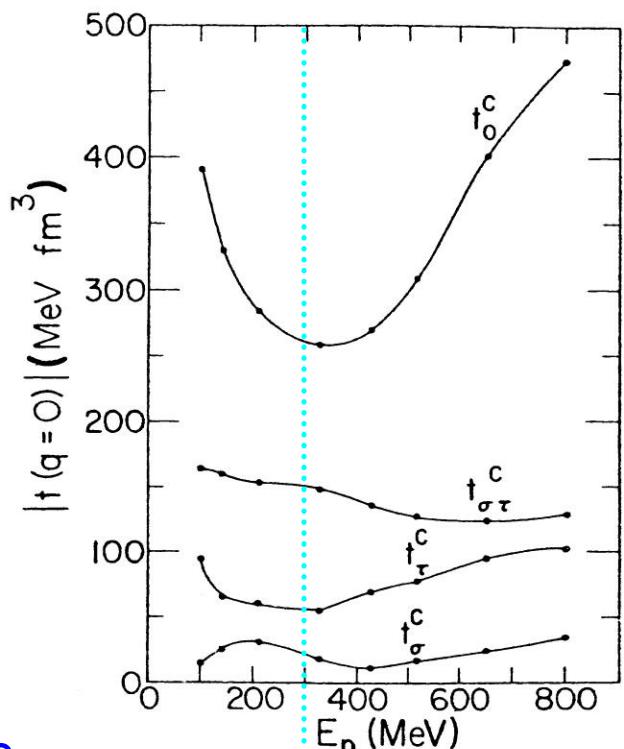
$$\begin{cases} {}^{48}\text{Ca}(p,n){}^{48}\text{Sc} \\ {}^{48}\text{Ti}(n,p){}^{48}\text{Sc} \end{cases} \quad \begin{cases} {}^{116}\text{Cd}(p,n){}^{116}\text{In} \\ {}^{116}\text{Sn}(n,p){}^{116}\text{In} \end{cases}$$



# (p,n) & (n,p) at 300 MeV

## Advantages

- Simple reaction mechanism
- 300 MeV:
  1. Effective interaction favors Spin-flip transitions over Non-Spin-flip ones  
 $(t_{\sigma\tau} / t_\tau)$   
⇒ GT transitions are most clearly seen.
  2. Distortion effects are smallest ( $t_0$ ).  
⇒ analysis with DWIA is reliable.
  3. Tensor interaction is smallest ( $t_\tau^T$ ).  
⇒ Proportionality relation is reliable.  
cross section  $\Leftrightarrow$  strength
- ... Multipole decomposition analysis works best.



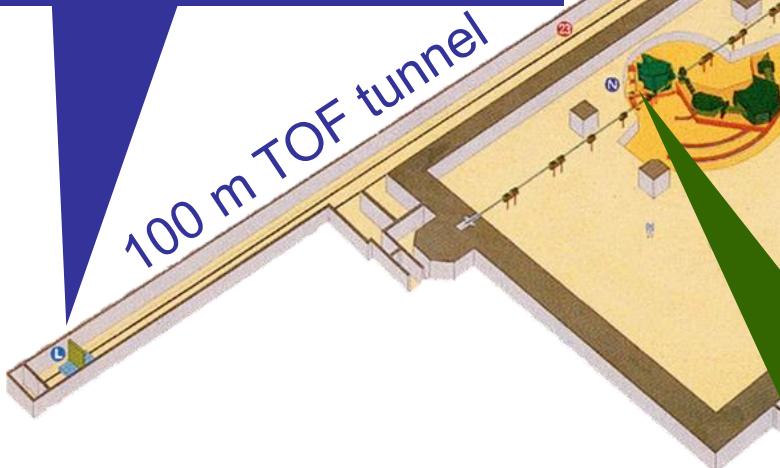
# $(p,n)$ & $(n,p)$ facilities at RCNP



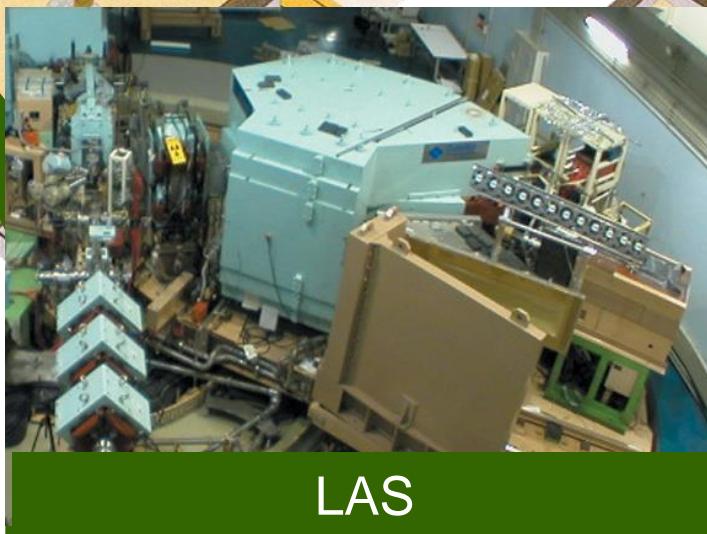
$(p,n)$  facility

Ring Cyclotron  
 $K = 400$

NPOL



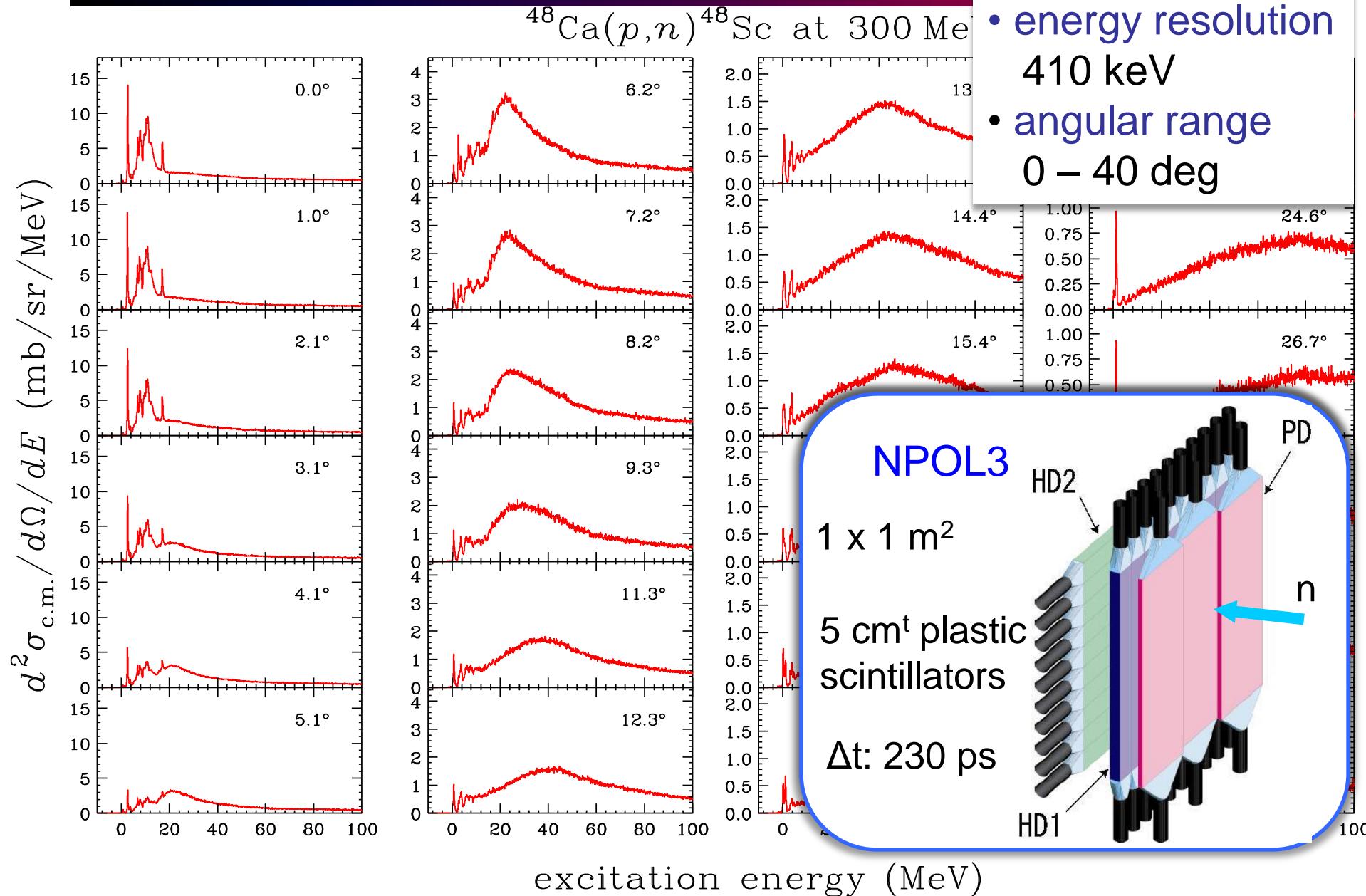
$(n,p)$  facility



LAS

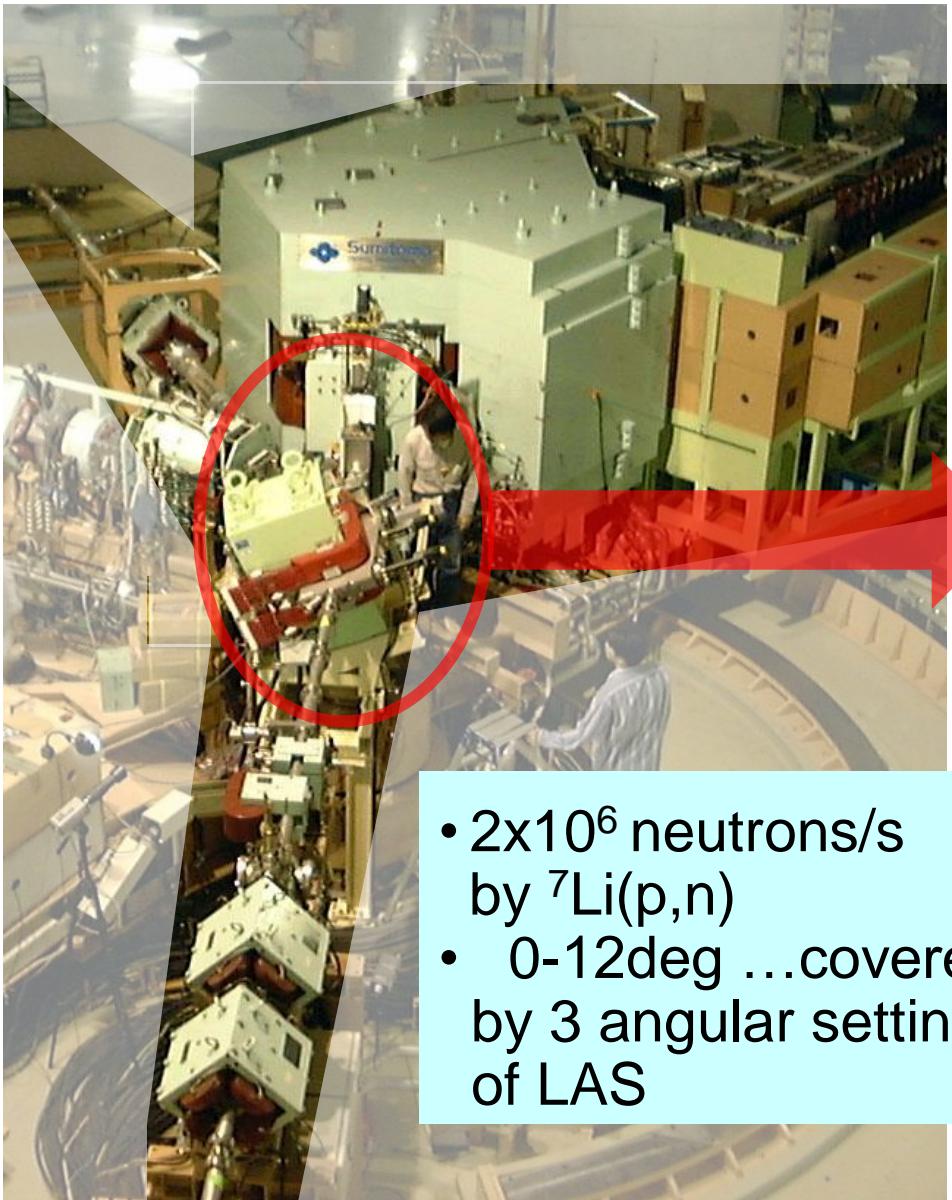
AVF Cyclotron  
 $K = 120$

# $^{48}\text{Ca}(\text{p},\text{n})$ measurement

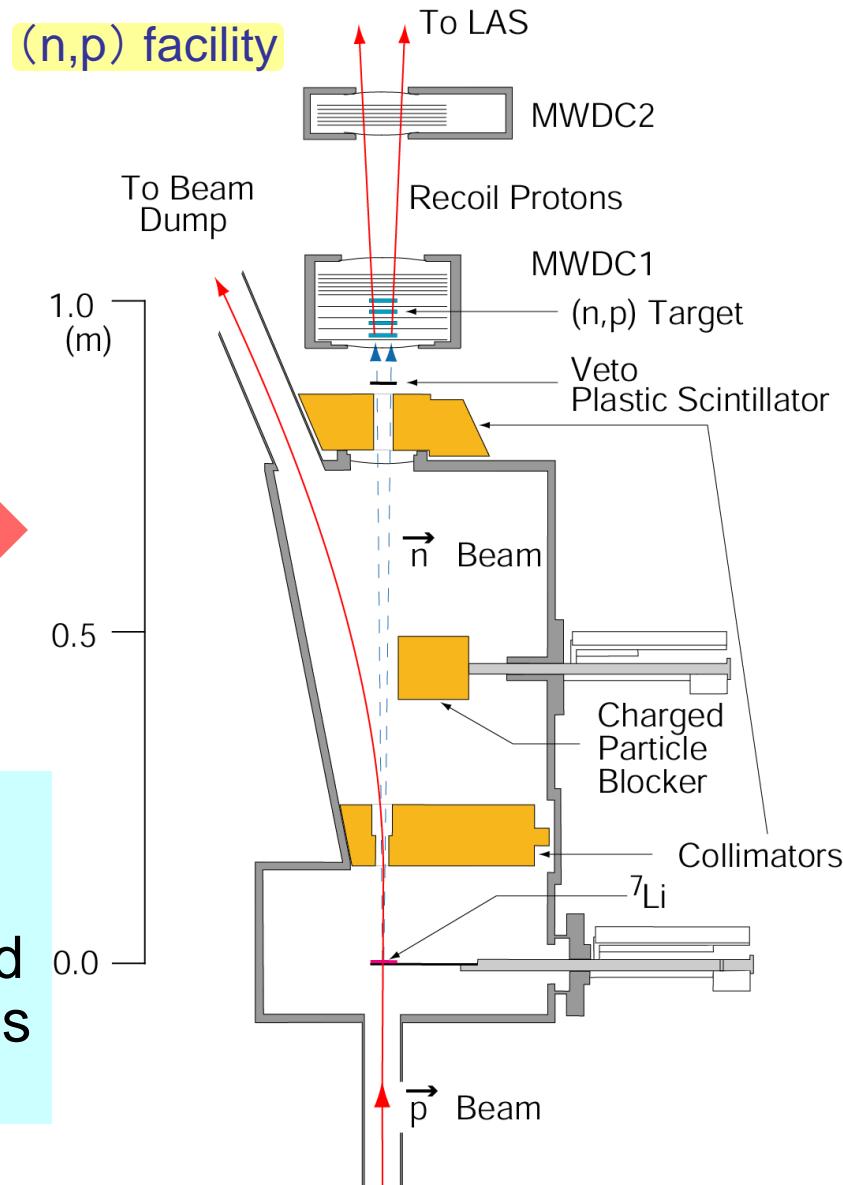


# (n,p) measurement

K.Y. et al., NIMA592(2008)88

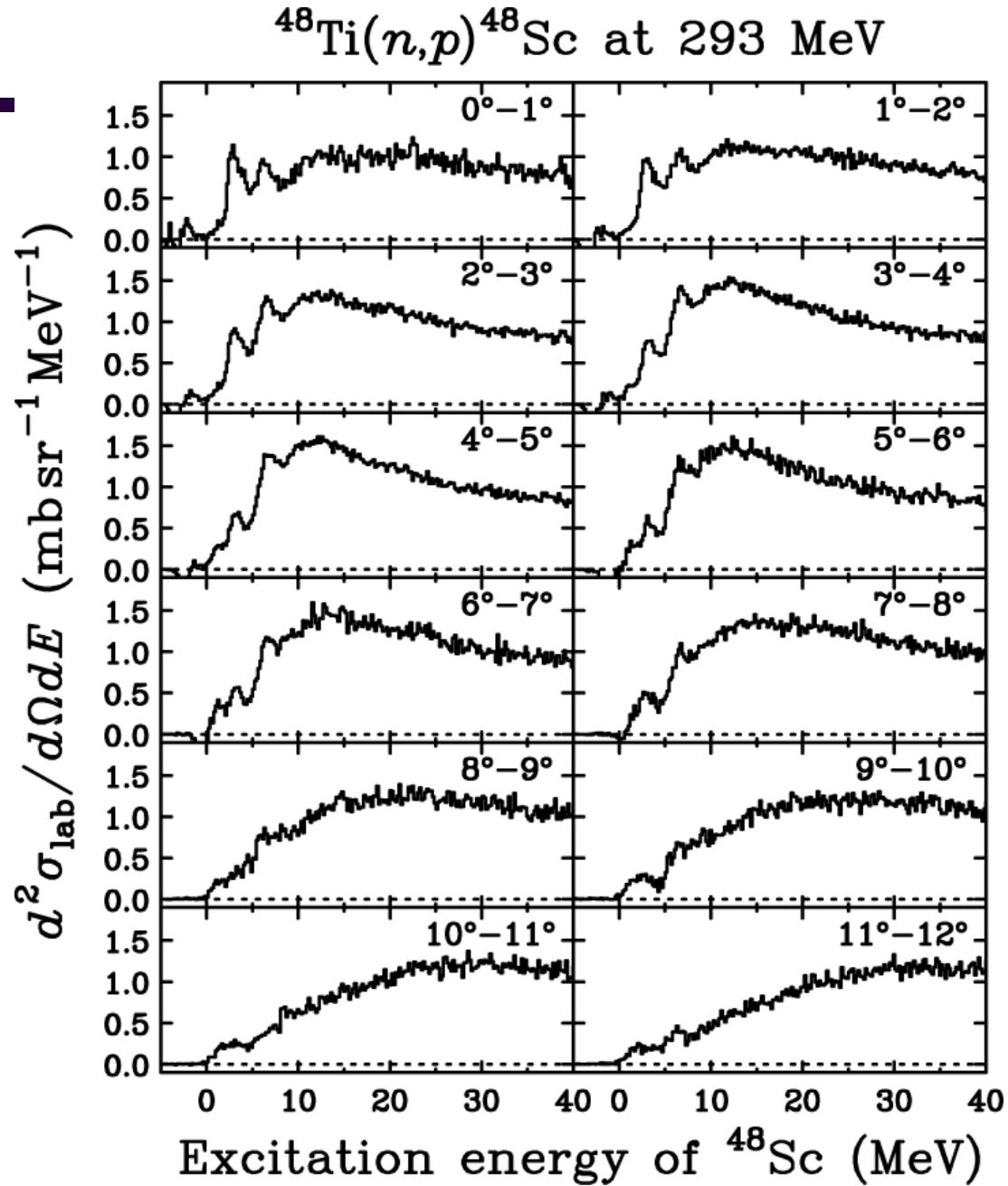


- $2 \times 10^6$  neutrons/s by  ${}^7\text{Li}(p,n)$
- 0-12deg ...covered by 3 angular settings of LAS



# $^{48}\text{Ti}(n,p)$ spectra

- angular range  
0 -12 deg
- energy resolution  
1.2 MeV
- statistical accuracy  
1--3% / 2MeV · 1deg
- systematic uncertainty  
4%



# Multipole decomposition analysis (MDA)

$$\sigma^{\text{exp}}(\theta_{\text{cm}}, E_x) \approx \sum_{J^\pi} a_{J^\pi} \sigma_{ph; J^\pi}^{\text{calc}}(\theta_{\text{cm}}, E_x)$$

$\Delta L = 0, 1, 2, 3$  [  $J^\pi = 1^+, (0^-, 1^-, 2^-), (2^+, 3^+), 4^-$  ]

DWIA inputs (DW81)

- NN interaction:

t-matrix by Franey & Love @325 MeV

- optical model parameters:

Global optical potential

(phenomenological, Cooper et al.)

- one-body transition density:

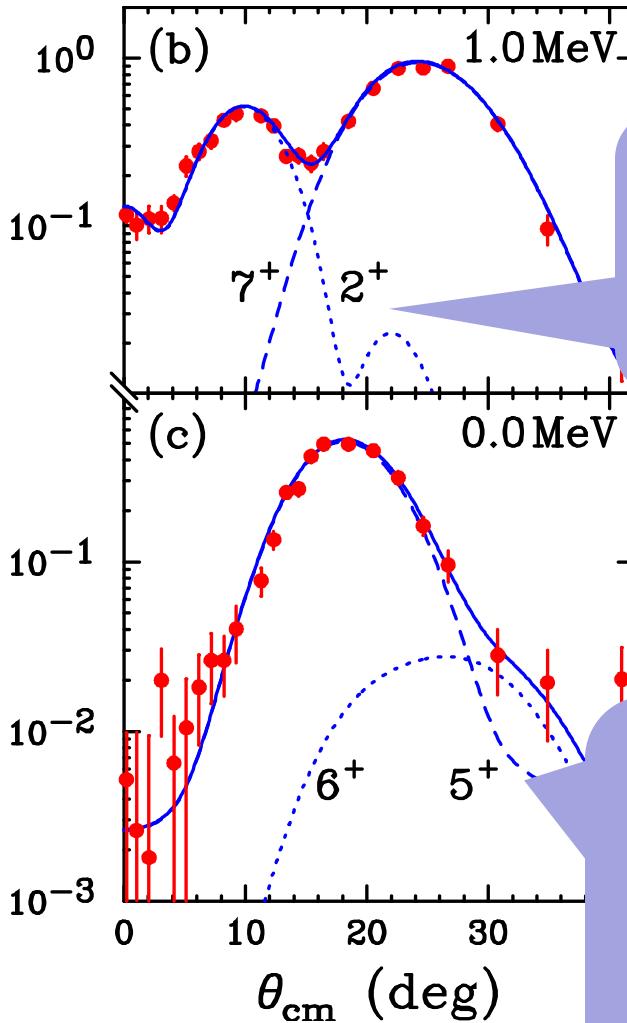
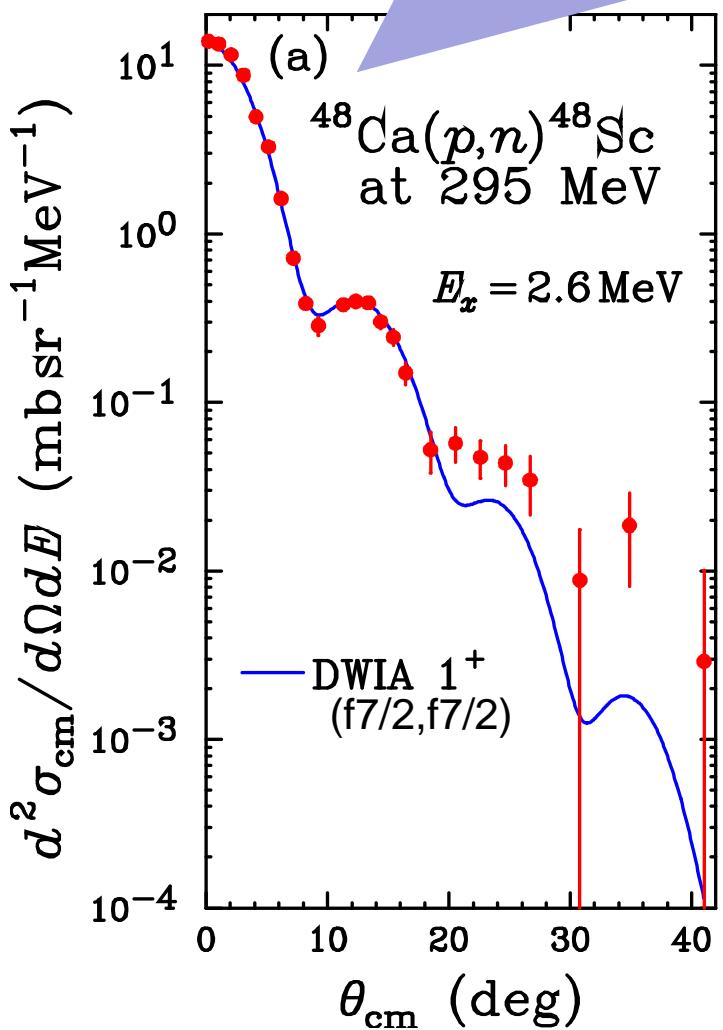
pure 1p-1h configurations

Particle:	1f, 2p, 1g, 2d, 3s, or 1h11/2
Hole:	1p, 1d, 2s, or 1f

radial wave functions ... W.S. / H.O.

# Examples of angular distribution

The DWIA description of GT transition is good.



The description of  $\Delta L=2$  is reasonable.

The  $\Delta L>3$  component does not contribute much at  $0^\circ$

# B(GT<sup>+-</sup>) distribution

K.Y. et al., PRL103(2009)012503

## MD analysis ...

(p,n) : strengths exist  
beyond GTGR

(n,p) : peak at 3 MeV  
shoulder at 6 MeV  
bump(?) at 12 MeV

Integrated strengths  
( $E_x < 30$  MeV)

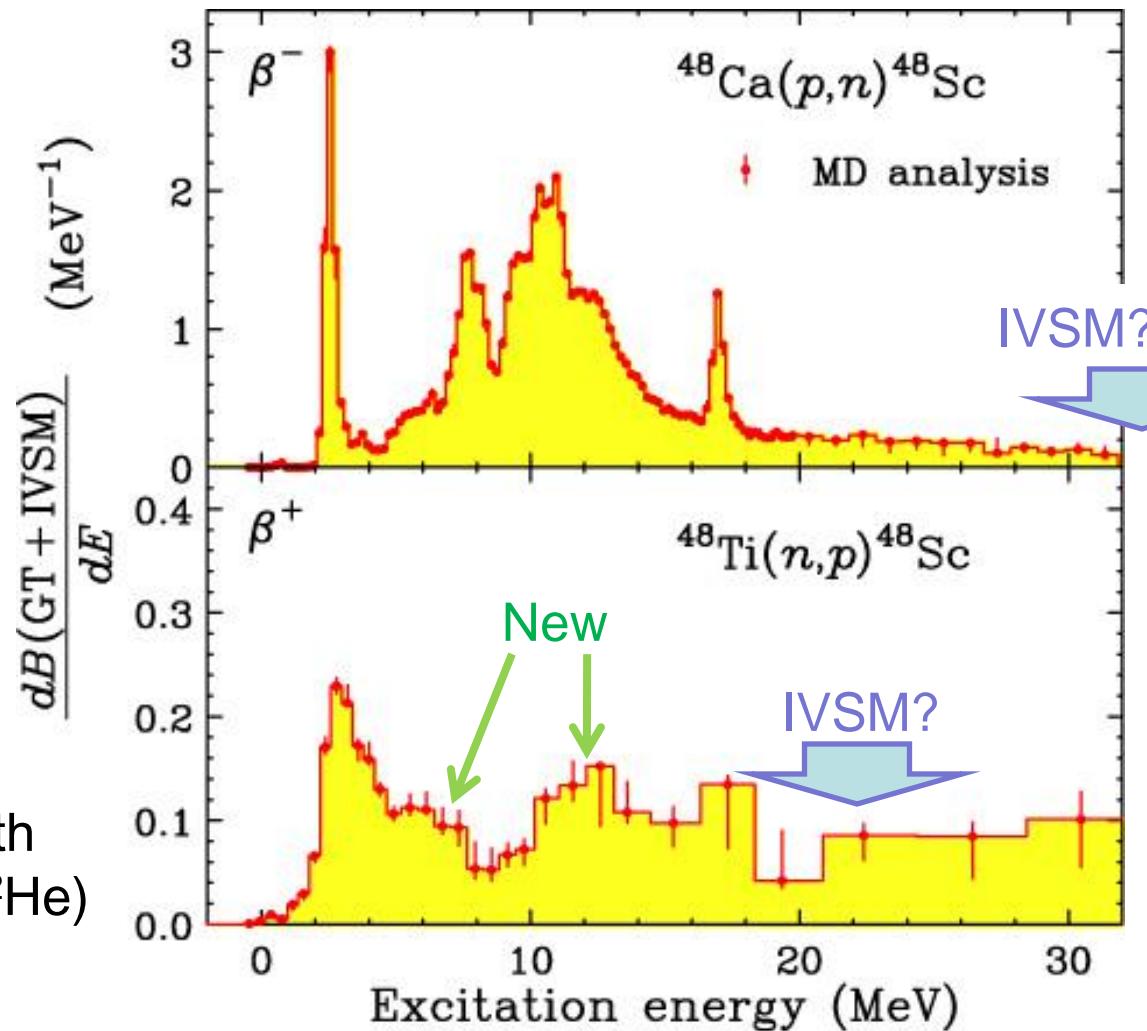
$$\begin{cases} \Sigma B(GT^-) = 15.3 \pm 2.2 \\ \Sigma B(GT^+) = 2.8 \pm 0.3 \end{cases}$$

$E_x < 5$  MeV ... consistent with  
( ${}^3\text{He}, t$ ) & ( $d, {}^2\text{He}$ )

## Contamination of IVSM?

isovector spin monopole ...  $\Delta S=1, \Delta L=0, 2\hbar\omega, O=r^2\sigma\tau$

contribution estimated by DWIA:  $0.9 \pm 0.2$  for (p,n),  $0.9 \pm 0.4$  for (n,p)



# B(GT<sup>+-</sup>) distribution ... comparison with shell model

Shell model ...

with quenched operator

Spectra agree qualitatively  
up to ...

(p,n) :  $E_x = 15$  MeV

(n,p) : 8 MeV

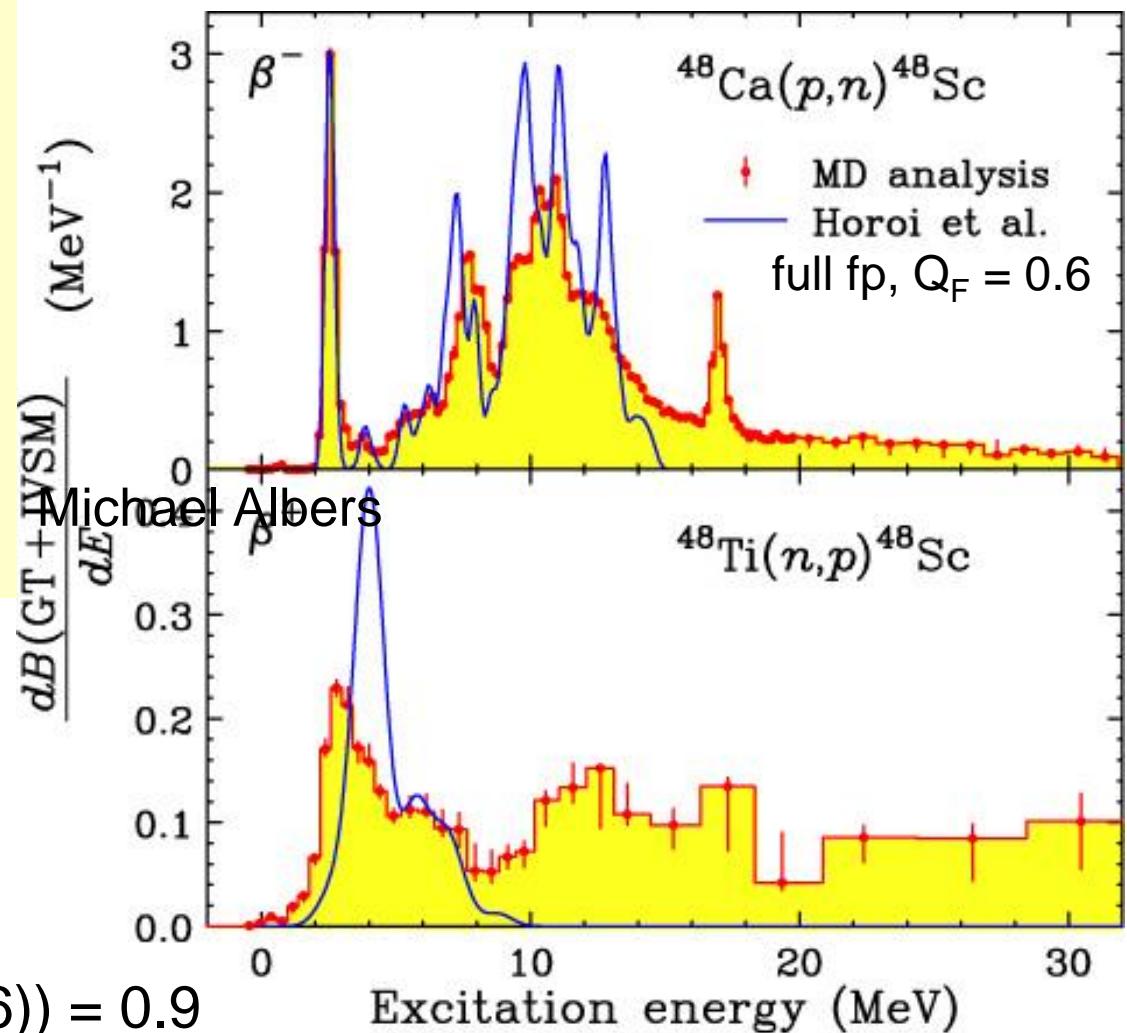
Strengths beyond  
... underestimated.

(n,p) channel :  
 $\Sigma B(\text{GT}^+;\text{exp}) = 1.9 \pm 0.3 \dots$

(w subtraction of IVSM)

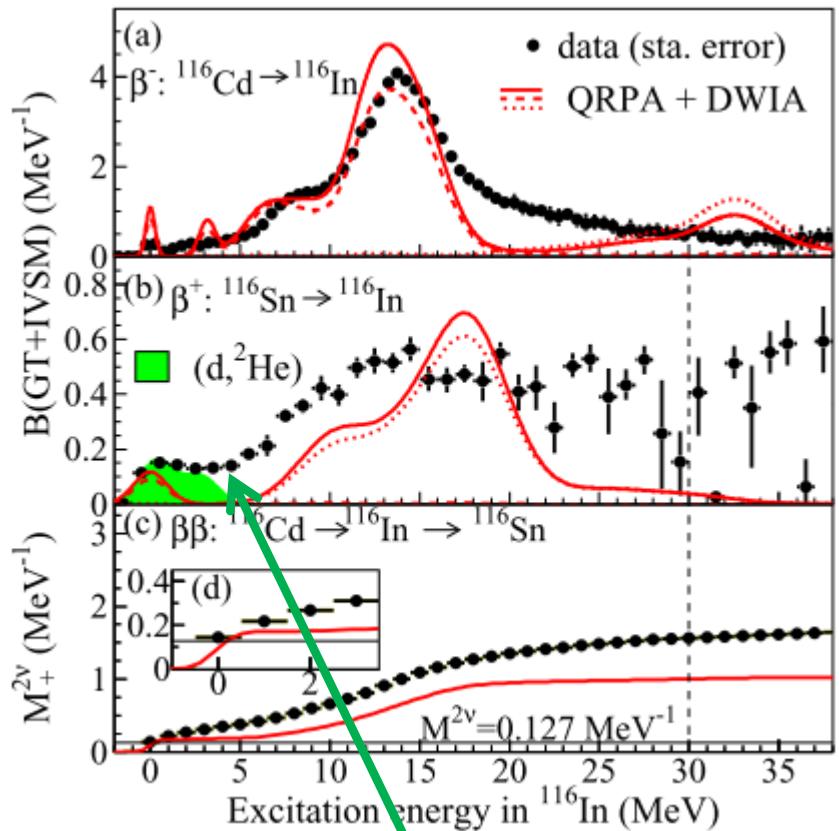


$\Sigma B(\text{GT}^+;\text{ShellModel}(Q_F=0.6)) = 0.9$



The “best” calculations fail to account for the spectra.  
Necessity of larger model space? Correlations?, ...

# $^{116}\text{Cd}$ case



$\beta^-$ : strengths in the low energy region to be pushed up  
 $\beta^+$ : extra strength of about 2 and/or strengths around 22 MeV to be pushed down

	Theo.			Exp.
	GT	IVSM	GT+IVSM	GT+IVSM
$\beta^+$	0.4	5.4	6.8	$11 \pm 1$
$\beta^-$	42	4	52	$45 \pm 8$



Interf. : ~15%

Strengths around 10 MeV are underestimated.  
 Extra g.s. correlation?

# Missing correlations?

For example, comparing SM w/ QRPA

- Each has uncertainty of
- SM predictions ...  
20-50% smaller than  
QRPA.
- Concerns...

SM : limited model space

QRPA :  
sufficient correlation?

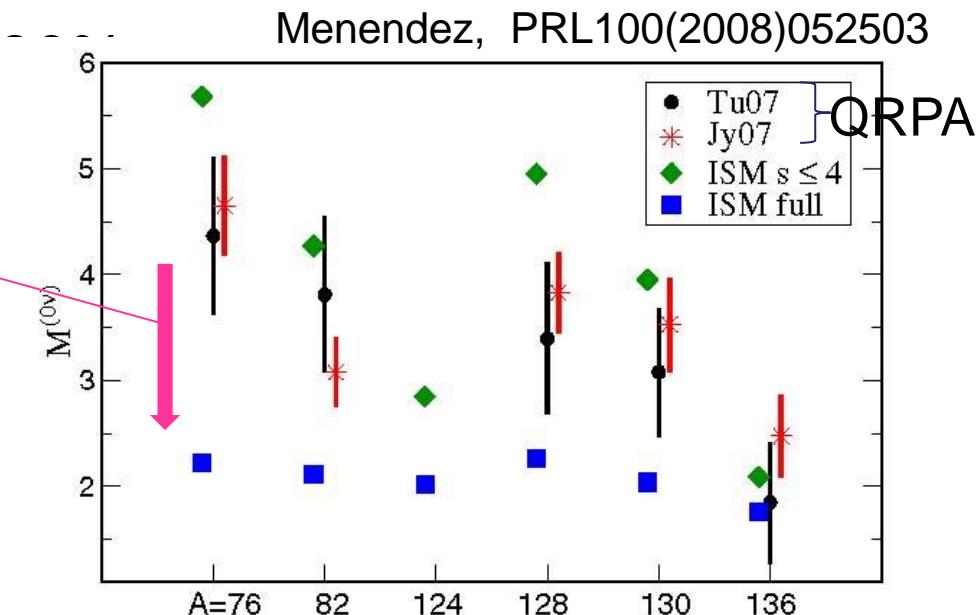
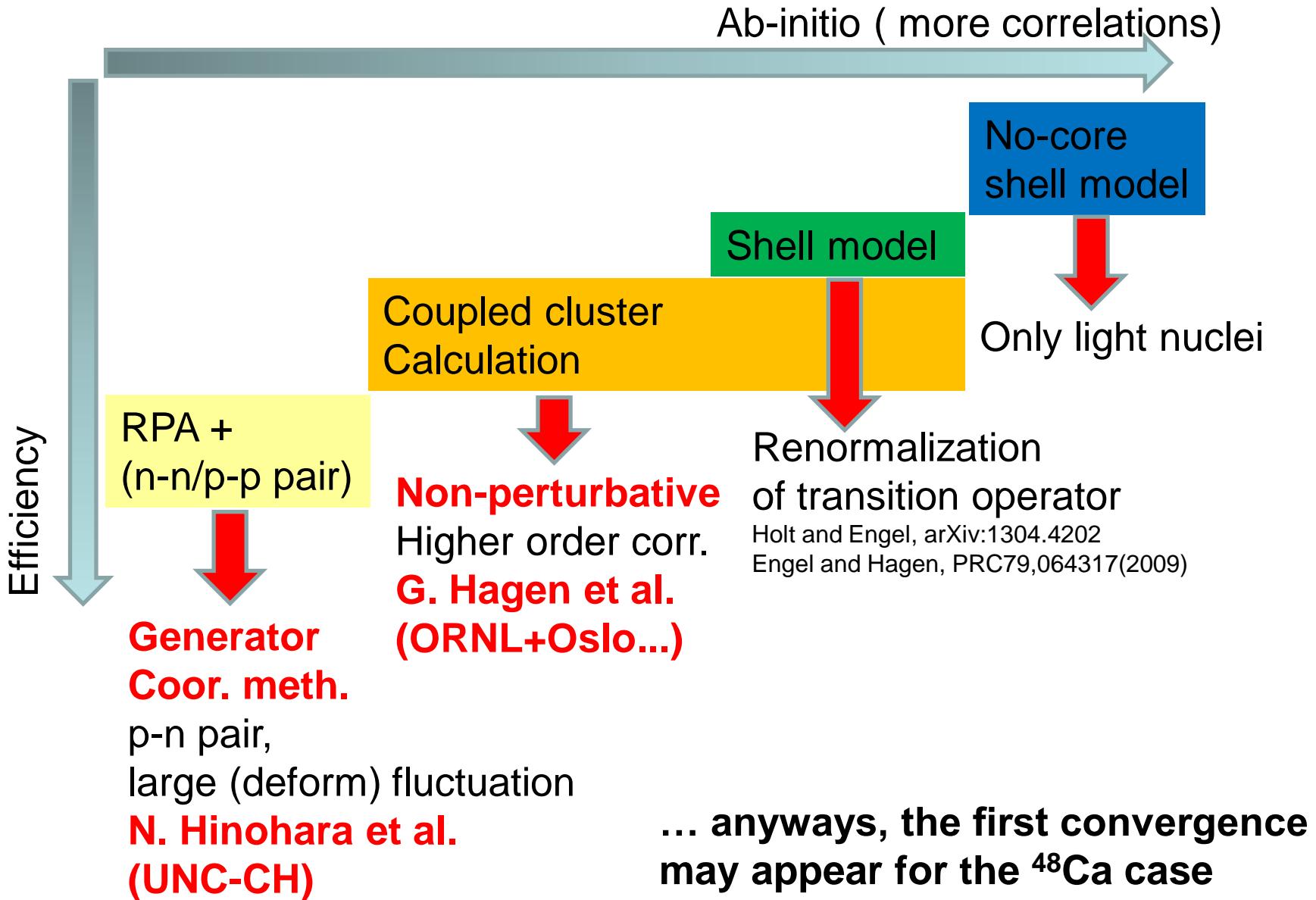


FIG. 3 (color online). The neutrinoless double beta decay NME's; comparison of ISM and QRPA calculations. Tu07; QRPA results from Ref. [20]. Jy07; QRPA results from Ref. [21]. ISM  $s \leq 4$  and ISM; present work. The ISM results have uncertainties in the 20% range (see text).

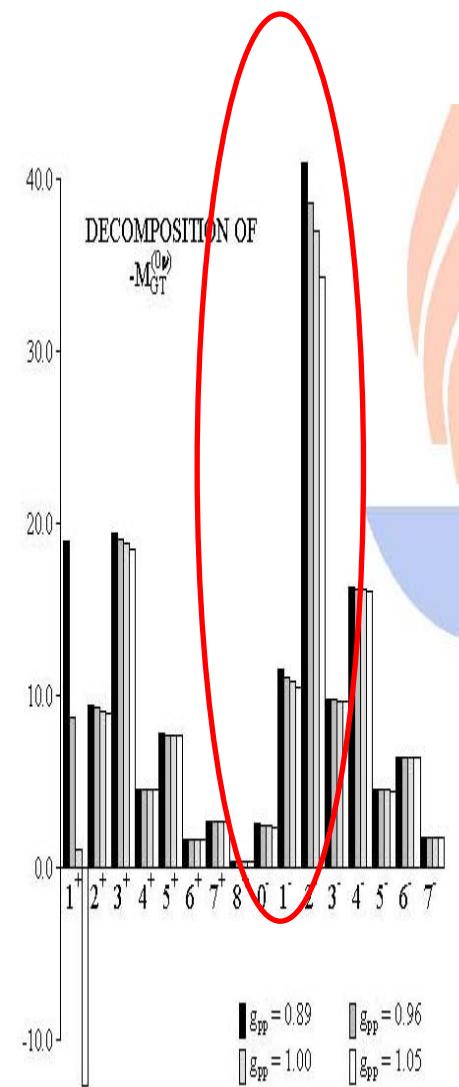
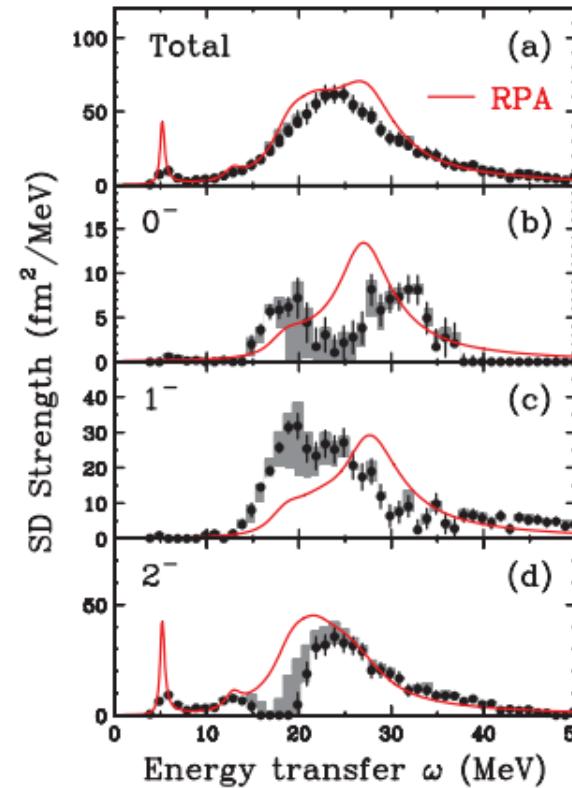
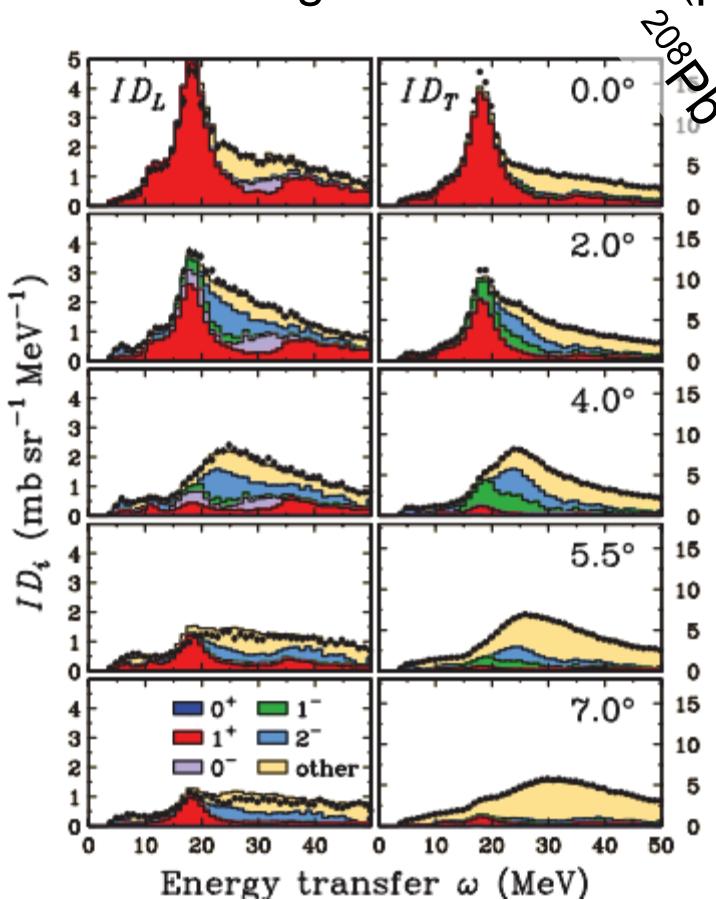
Different theories with different model spaces and different correlations

# How do theories converge ...



# What can be done further experimentally?

breakthrough at RCNP via ( $p \rightarrow, n \rightarrow$ ) meas...



Wakasa et al., PRC85, 064606 (2012)

Ingredients most important for neutrinoless mode can be directly probed...  
Measurement on  $^{48}\text{Ca}$  would be interesting...

# Summary

---

- Half-lives, transfer and (p,n)/(n,p) reactions  
→ constrains the structure theories
- We measured the cross section spectra for
  - the  $^{48}\text{Ca}(\text{p},\text{n})^{48}\text{Sc}$  /  $^{48}\text{Ti}(\text{n},\text{p})^{48}\text{Sc}$  reactions and
  - the  $^{116}\text{Cd}(\text{p},\text{n})^{116}\text{In}$  /  $^{116}\text{Sn}(\text{n},\text{p})^{116}\text{In}$  reactionsat 300 MeV
- Currently, the understanding of nuclear correlations is not enough!
  - Challenges w/ more sophisticated frameworks!
  - A new tool, (p→,n→) at RCNP
  - 0-, 1-, 2-, (important for neutrinoless mode)

# Summary

---

# Multipole decomposition analysis

MDA

$$\sigma^{\text{exp}}(\theta_{\text{cm}}, E_x) \approx \sum_{J^\pi} a_{J^\pi} \sigma_{ph; J^\pi}^{\text{calc}}(\theta_{\text{cm}}, E_x)$$

$$\Delta L = 0, 1, 2, 3 \quad [J^\pi = 1^+, (0^-, 1^-, 2^-), (2^+, 3^+), 4^-]$$

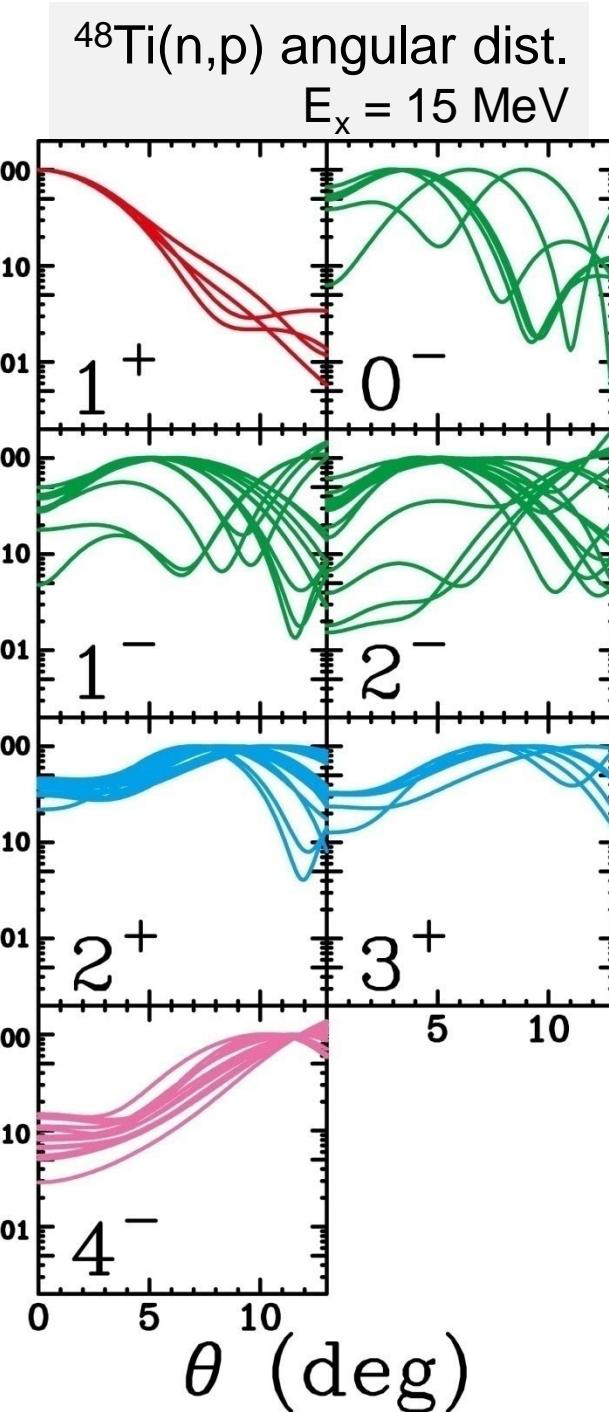
DWIA inputs (DW81)

- NN interaction:  
t-matrix by Franey & Love @ 325 MeV
- optical model parameters:  
Global optical potential  
(phenomenological, Cooper et al.)
- one-body transition density:  
pure 1p-1h configurations

Particle: 1f, 2p, 1g, 2d, 3s, or 1h11/2

Hole: 1p, 1d, 2s, or 1f

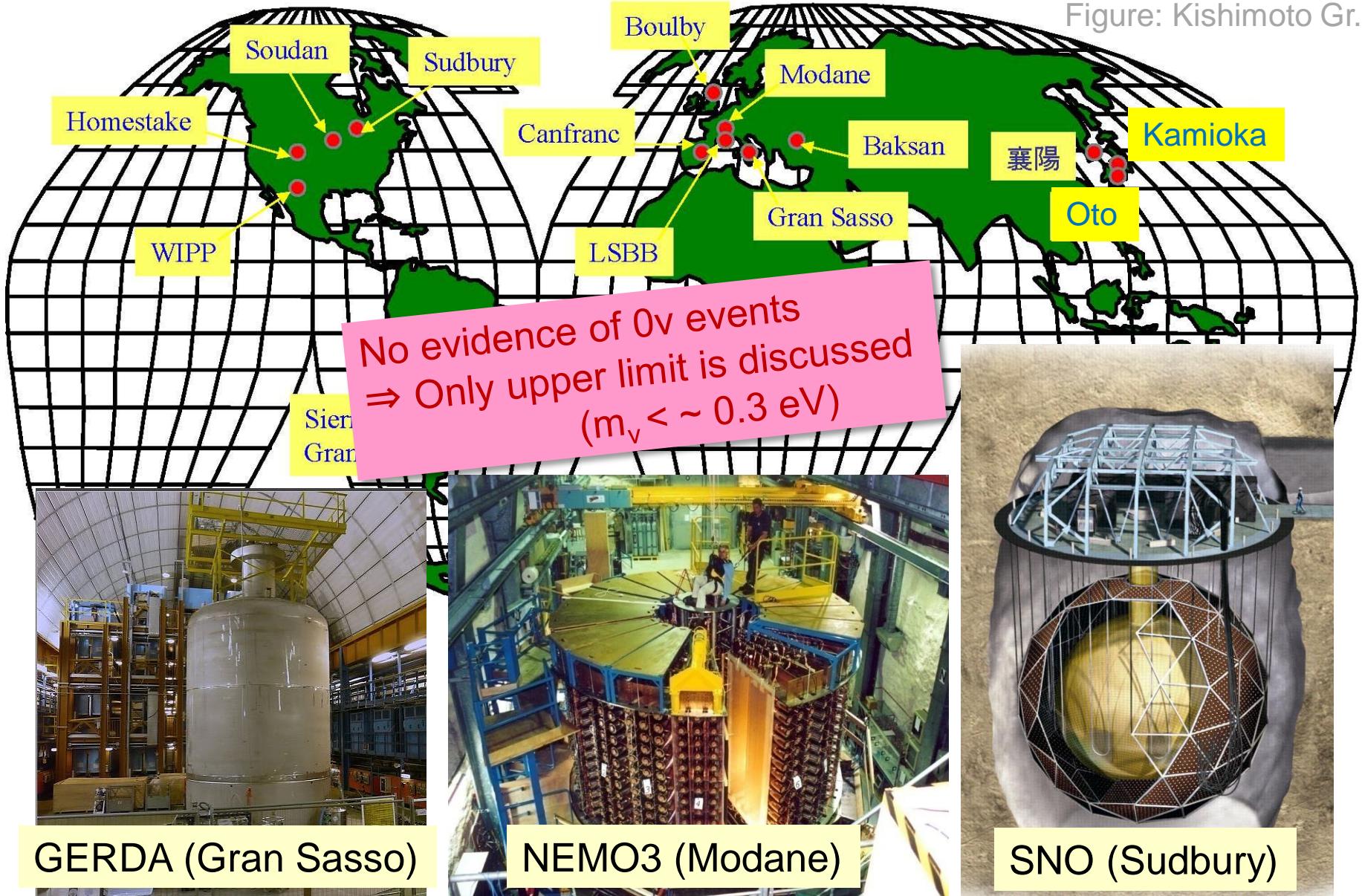
radial wave functions ... W.S. / H.O.



Study of Gamow-Teller transition strengths  
in the intermediate nucleus  $^{116}\text{In}$   
of the  $^{116}\text{Cd}$  double- $\beta$  decay  
via the  $^{116}\text{Cd}(\text{p},\text{n})$  and  $^{116}\text{Sn}(\text{n},\text{p})$  reactions  
at 300 MeV

Masaki Sasano (RIKEN)

# 0v labs



# QRPA calculation with a large model space

QRPA prediction (GT + IVSM)

(Rodin et al., Tuebingen Univ.)

Large model space (34 levels)

⇒ Enough for  $2\hbar\omega$  excitation by Rodin et al.

- quenching factor, 0.843 &  $g_{pp} = 0.5$

⇒ adjusted for  $M(2\nu)$  and  $\beta$  decays from the  $^{116}\text{In}$  g.s.

Transition density

+ DWIA calculation (DW81) (K. Amos, A. Faessler and V. Rodin, Phys. Rev. C **76**, 014604 (2007))

Base: H.O.  $b=2.23$  fm

NN int. : FL325MeV

Global optical potential by Cooper & Hama

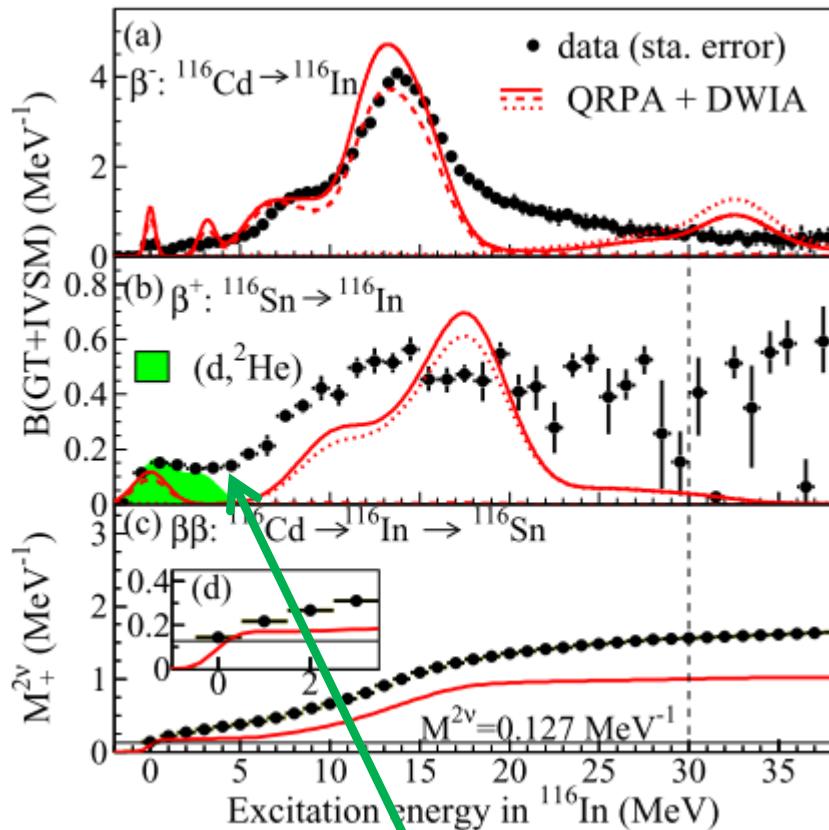
⇒ Cross sections

⇒ Strengths

⇒ Smearing with escape width & exp. res.

(Rodin & Urin, Phys. of Atomic Nuclei, 66 (2009), 2128)

# Comparison



$\beta^-$  : strengths in the low energy region to be pushed up  
 $\beta^+$  : extra strength of about 2 and/or strengths around 22 MeV to be pushed down

	Theo.			Exp.
	GT	IVSM	GT+IVSM	GT+IVSM
$\beta^+$	0.4	5.4	6.8	$11 \pm 1$
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Interf. : ~15%

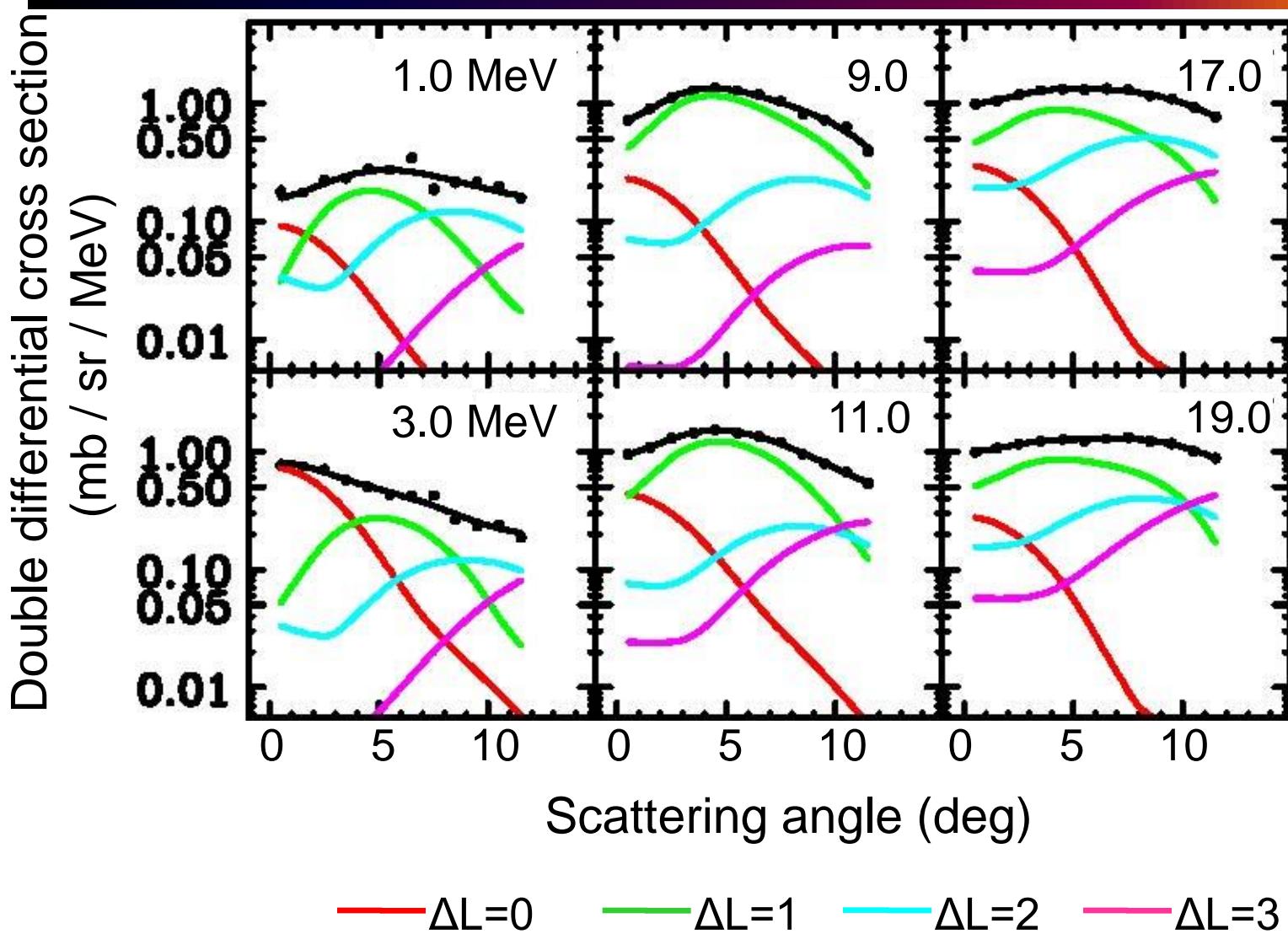
Strengths around 10 MeV are underestimated.  
 Extra g.s. correlation?

# Summary

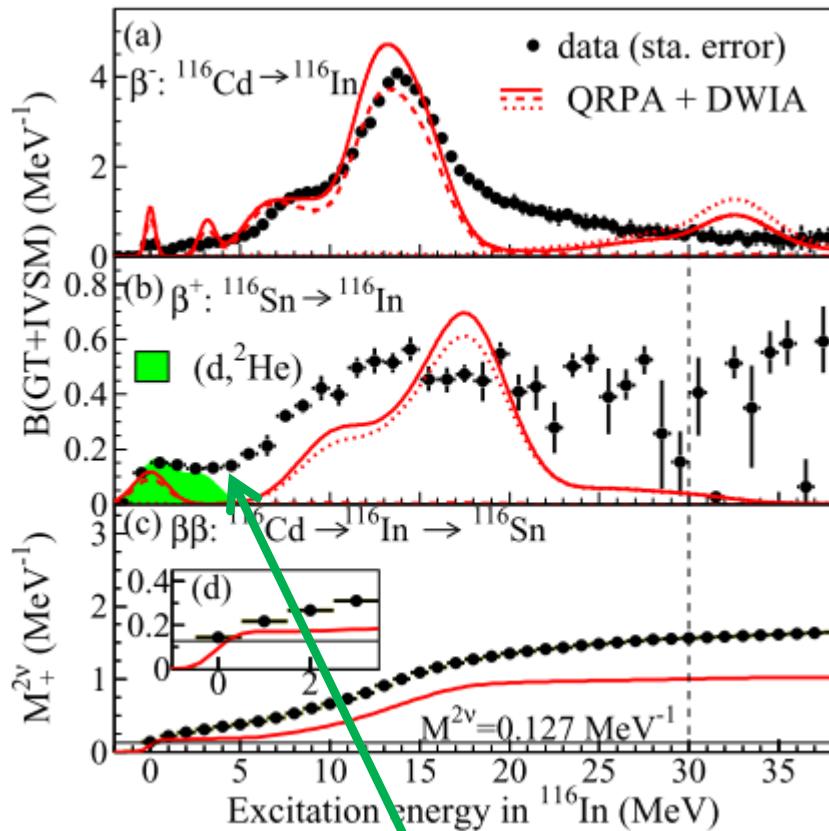
---

- Study of beta-type transitions in DBD nuclei can guide / constrain the structure theories used in the prediction of NME.
- We measured the cross section spectra for
  - the  $^{48}\text{Ca}(\text{p},\text{n})^{48}\text{Sc}$  /  $^{48}\text{Ti}(\text{n},\text{p})^{48}\text{Sc}$  reactions and
  - the  $^{116}\text{Cd}(\text{p},\text{n})^{116}\text{In}$  /  $^{116}\text{Sn}(\text{n},\text{p})^{116}\text{In}$  reactionsat 300 MeV.
- MD analysis →  $B(\text{GT}^{+/-})$  distribution ( $E_x < 30$  MeV)
- $^{48}\text{Ca} \rightarrow ^{48}\text{Sc} \rightarrow ^{48}\text{Ti}$  [PRL103(2009)012503]
  - $\Sigma B(\text{GT}^-) = 15.3 \pm 2.2$
  - $\Sigma B(\text{GT}^+) = 2.8 \pm 0.3$
  - shell model predictions :
    - $B(\text{GT}^-)$ : good agreement up to GTGR ( $E_x < 15$  MeV).
    - $B(\text{GT}^+)$ : reasonable for  $E_x < 8$  MeV,  
underestimation for  $E_x > 8$  MeV
- Watch out! Current predictions of 0v-NME might be a way off!

# Decomposed angular distributions [ $^{48}\text{Ti}(\text{n},\text{p})$ ] Miki



# $^{116}\text{Cd}$



$\beta^-$  : strengths in the low energy region to be pushed up  
 $\beta^+$  : extra strength of about 2 and/or strengths around 22 MeV to be pushed down

	Theo.			Exp.
	GT	IVSM	GT+IVSM	GT+IVSM
$\beta^+$	0.4	5.4	6.8	$11 \pm 1$
$\beta^-$	42	4	52	$45 \pm 8$



Interf. :  $\sim 15\%$

Strengths around 10 MeV are underestimated.  
 Extra g.s. correlation?