

Neutrinoless double beta decay in the seesaw mechanism

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1. Introduction

Puzzles of neutrino in SM

- ✓ Neutrino mass (oscillation experiment)
- ✓ Dirac type or Majorana type ?
- ✓ Right-handed neutrino ... ?

Oscillation experiment data

Neutrino mass hierarchy	$\Delta m_{21}^2/10^{-5}eV^2$	$\Delta m_{3l}^2/10^{-3}eV^2$	[NuFIT 5.1(21)]
NH ($m_1 < m_2 < m_3$)	$7.42^{+0.21}_{-0.20}$	$2.510^{+0.027}_{-0.027}$	
IH ($m_3 < m_1 < m_2$)	$7.42^{+0.21}_{-0.20}$	$-2.490^{+0.026}_{-0.028}$	

- At least two generations of neutrinos are **massive**.
- **Smallness** of neutrino mass,

$$m_\nu \sim \mathcal{O}(10^{-11})\text{GeV} \lll m_e \sim 10^{-4}\text{GeV}$$

Beyond SM physics is needed to explain these discrepancies

2. SM + RHν

$F_{\alpha I}$: Yukawa coupling L_α : SM lepton doublet Φ : SM Higgs doublet
 ν_{RI} : right-handed neutrino M_I : Majorana mass of right-handed neutrino

$$\mathcal{L} = \mathcal{L}_{SM} + i\bar{\nu}_{RI}\gamma^\mu\partial_\mu\nu_{RI} - \left(F_{\alpha I}\bar{L}_\alpha\Phi\nu_{RI} + \frac{M_I}{2}\bar{\nu}_{RI}\nu_{RI} + h.c. \right)$$

Weak interaction of neutrino

$$\nu_{L\alpha} = \sum_i U_{\alpha i}\nu_i + \sum_I \Theta_{\alpha I}N_I^c$$

$U_{\alpha i}$: Mixing element of active ν (PMNS matrix)
 $\Theta_{\alpha I}$: Mixing element of RHν
 All mass eigenstates have the weak interactions.

Yukawa coupling

$$F = \frac{i}{(\Phi)}UD\nu^{1/2}\Omega D_N^{1/2}$$

$D_\nu = \text{diag}(m_1, m_2, m_3)$ ω : Complex parameter
 $D_N = \text{diag}(M_1, M_2)$ $\Omega = \begin{pmatrix} 0 & 0 \\ \cos\omega & -\sin\omega \\ \xi\sin\omega & \xi\cos\omega \end{pmatrix}$

Seesaw mechanism works!

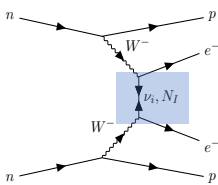
Assumption for Dirac mass & Majorana mass $M_D (= (\Phi)F) \ll M_I$

Predictions

- Majorana neutrino
- Smallness of neutrino masses
- **New particles and interactions**

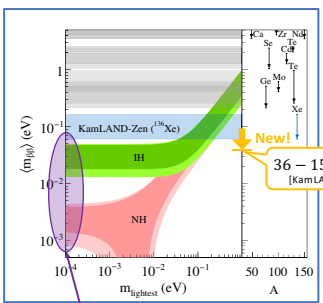
3. $0\nu\beta\beta$ decay

Why is $0\nu\beta\beta$ decay?



- One possibility for the decay is Majorana neutrino mediation.
 → It is possible to verify the Majorana nature of the neutrino.
- The decay process violates the lepton number.
 → Application to Leptogenesis is expected.

Active ν's contribution [KamLAND-Zen ('16)]



Effective mass

$$m_{\text{eff}} = m_{\text{eff}}^{\nu} + m_{\text{eff}}^N$$

Active ν's contribution $m_{\text{eff}}^{\nu} = \sum_i U_{ei}^2 m_i$

RHν's contribution $m_{\text{eff}}^N = \sum_I \Theta_{eI}^2 M_I f_\beta(M_I)$

Suppression factor by the propagator

$$f_\beta(M_I) = \frac{\Lambda_\beta^2}{\Lambda_\beta^2 + M_I^2}$$

When $M_I \ll \Lambda_\beta$, RHν great contribution!!

Testable region $m_{\text{highest}} = 0$
 $|m_{\text{eff}}^{\nu}| = \begin{cases} 1.45 - 3.68 \text{ meV (NH)} \\ 18.6 - 48.4 \text{ meV (IH)} \end{cases}$

4. $0\nu\beta\beta$ decay in the seesaw mechanism

Cancellation by N

Mass assumption $M_1 < \Lambda_\beta \ll M_2$ $\begin{cases} f_\beta(M_1) = 1 - \delta_f^2 \\ f_\beta(M_2) = 0 \end{cases}$

The effective mass can be expanded into a concrete expression by using Casas-Ibarra parametrization.

$$m_{\text{eff}} = \sum_i U_{ei}^2 m_i + \sum_I \Theta_{eI}^2 M_I f_\beta(M_I)$$

NH case ($m_1 = 0$)
 $= [1 - f_\beta(M_1)] [U_{e2}m_2^{1/2} \cos\omega + U_{e3}m_3^{1/2} \sin\omega]^2 + [1 - f_\beta(M_2)] [U_{e2}m_2^{1/2} \sin\omega - U_{e3}m_3^{1/2} \cos\omega]^2$
 $= (U_{e2}m_2^{1/2} \sin\omega - U_{e3}m_3^{1/2} \cos\omega)^2 + (U_{e2}m_2^{1/2} \cos\omega + U_{e3}m_3^{1/2} \sin\omega)^2 \times \delta_f^2$

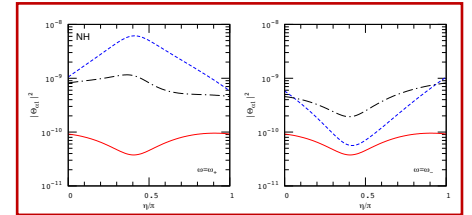
solved ↓

$$\tan\omega = \frac{A \pm i\delta_f}{1 \mp i\delta_f A} \equiv \tan\omega_\pm$$

$$A = \frac{U_{e3}m_3^{1/2}}{U_{e2}m_2^{1/2}}$$

Decay suppressed by the RHν!!

Even if no decay is observed, the nature of RHν can be characterized!



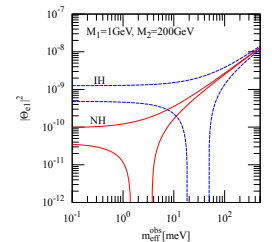
Enhancement by N

Assuming the effective mass observed at $|m_{\text{eff}}| = m_{\text{eff}}^{\text{obs}}$

Mass assumption $M_1 \neq M_2$

- The absolute value of the mixing element is determined by the effective mass of the observed decay.

$$\Theta_{e1}^2 = \frac{m_{\text{eff}}^{\text{obs}} - m_{\text{eff}}^{\nu}}{M_1 [f_\beta(M_1) - f_\beta(M_2)]}$$

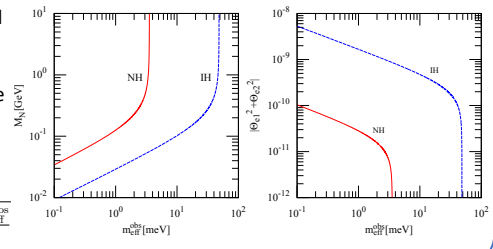


Mass assumption $M_1 = M_2 = M_N$

- Predictions are obtained regarding the absolute value of the sum of the mixing elements and the mass of the RHν.

$$M_N = \Lambda_\beta \sqrt{\frac{m_{\text{eff}}^{\text{obs}}}{|m_{\text{eff}}^{\nu}| - m_{\text{eff}}^{\text{obs}}}}$$

$$|\Theta_{e1}^2 + \Theta_{e2}^2| = \frac{|m_{\text{eff}}^{\nu}|}{\Lambda_\beta} \sqrt{\frac{|m_{\text{eff}}^{\nu}| - m_{\text{eff}}^{\text{obs}}}{m_{\text{eff}}^{\text{obs}}}}$$



5. Future experiments

The effective masses of the decays including N's contribution becomes different depending on the decay nuclei.

→ The nature of RHν is more limited.

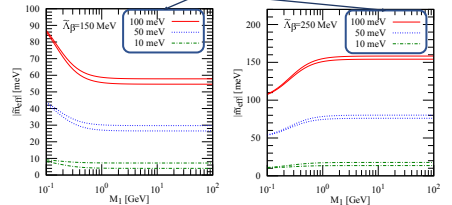
Fermi momentum of nuclei

⁷⁶Ge : 159.0 - 193.0 MeV
¹³⁶Xe : 178.0 - 211.0 MeV

[Faessler, Gonzalez, Kovalenko, Simkovic('14)]

Predicted effective mass

$$m_{\text{eff}} = [1 - \tilde{f}_\beta(M_2)] m_{\text{eff}}^{\nu} + m_{\text{eff}}^N = m_{\text{eff}}^{\nu} [1 - \tilde{f}_\beta(M_2)] \frac{\tilde{f}_\beta(M_1) - \tilde{f}_\beta(M_2)}{\tilde{f}_\beta(M_1) - \tilde{f}_\beta(M_2)}$$



6. Conclusion

- We discussed the $0\nu\beta\beta$ decay in the seesaw mechanism.
- We comprehensively investigated the contribution to the decay of the RHν.
- Especially, when it is **lighter than the typical fermi momentum**, the decay is **strongly suppressed** and may no longer occur.
- We showed that the properties of RHν may be characterized by the future decay-observation-experiments.
- We pointed out that multiple experiments using different nuclei are important to understand the properties of right-handed neutrinos (masses and mixing elements).

Huge region can be searched on future experiments.

