

**UGAP 2022: Unravelling the History of the Universe
and Matter Evolution with Underground Physics**
Tokyo University of Science, Japan, June 14, 2022

Self-resonant dark matter

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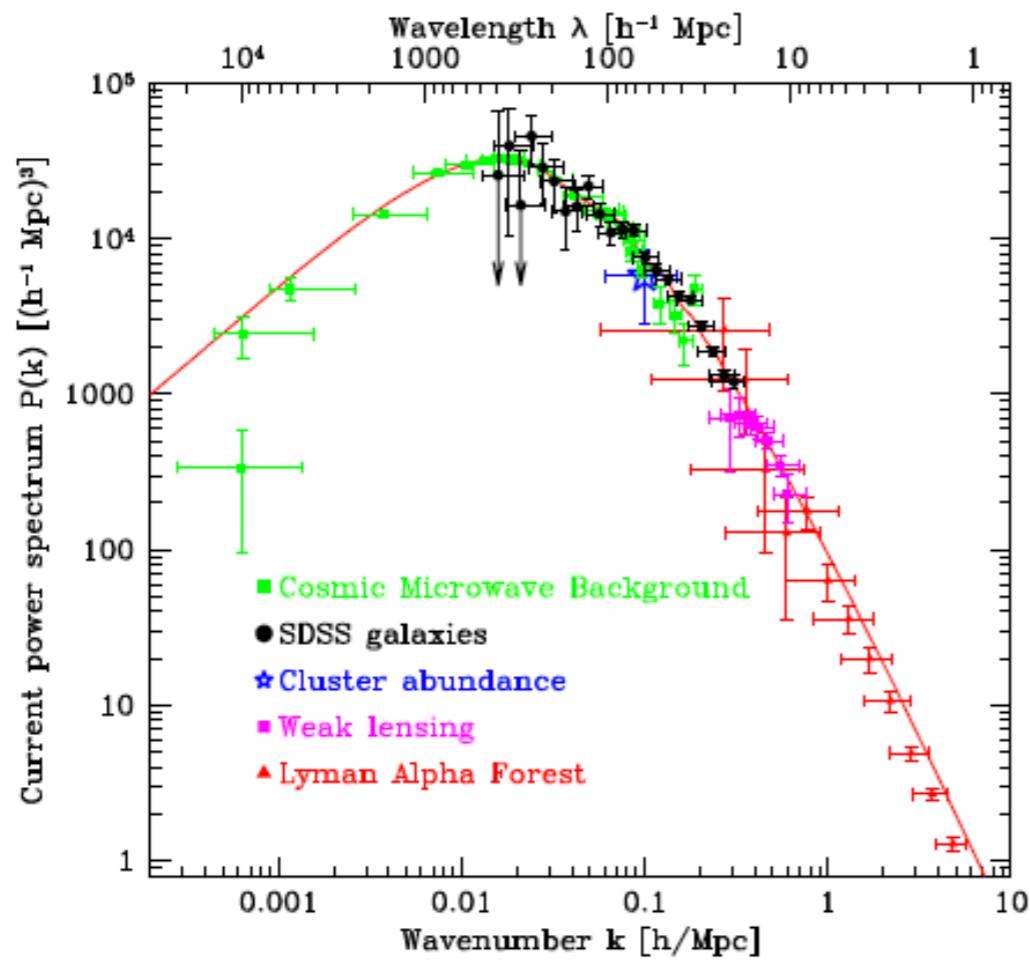
In collaboration with Seong-Sik Kim & Bin Zhu,
JHEP 10 (2021) 239, JHEP 05 (2022) 148

Outline

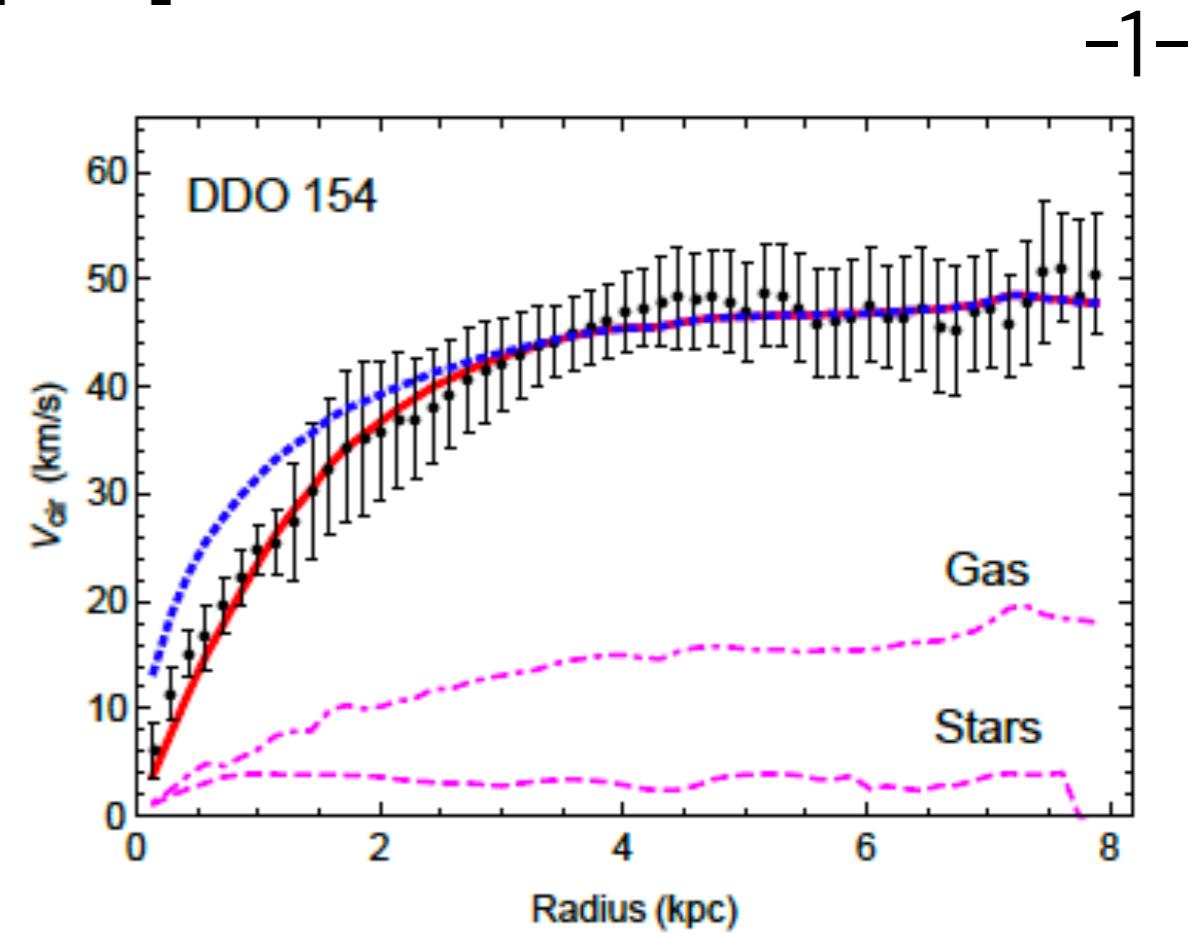
- Self-interacting dark matter
- u-channel resonances
- Models for u-channel resonances
- Conclusions

**Self-interacting dark
matter**

Core-Cusp problem



CDM works well at $> \text{Mpc}$



Galaxy rotation curves at $< 1 \text{ kpc}$
 [Spergel, Steinhardt, 2000; Tulin, Yu, 2017]

- CDM N-body simulation predicts cuspy DM profile (NFW), making rotation velocities overshooting at small scales.

$$v_{\text{cir}} \sim \sqrt{r}, \quad \rho_{\text{dm}} \sim r^{-1}$$

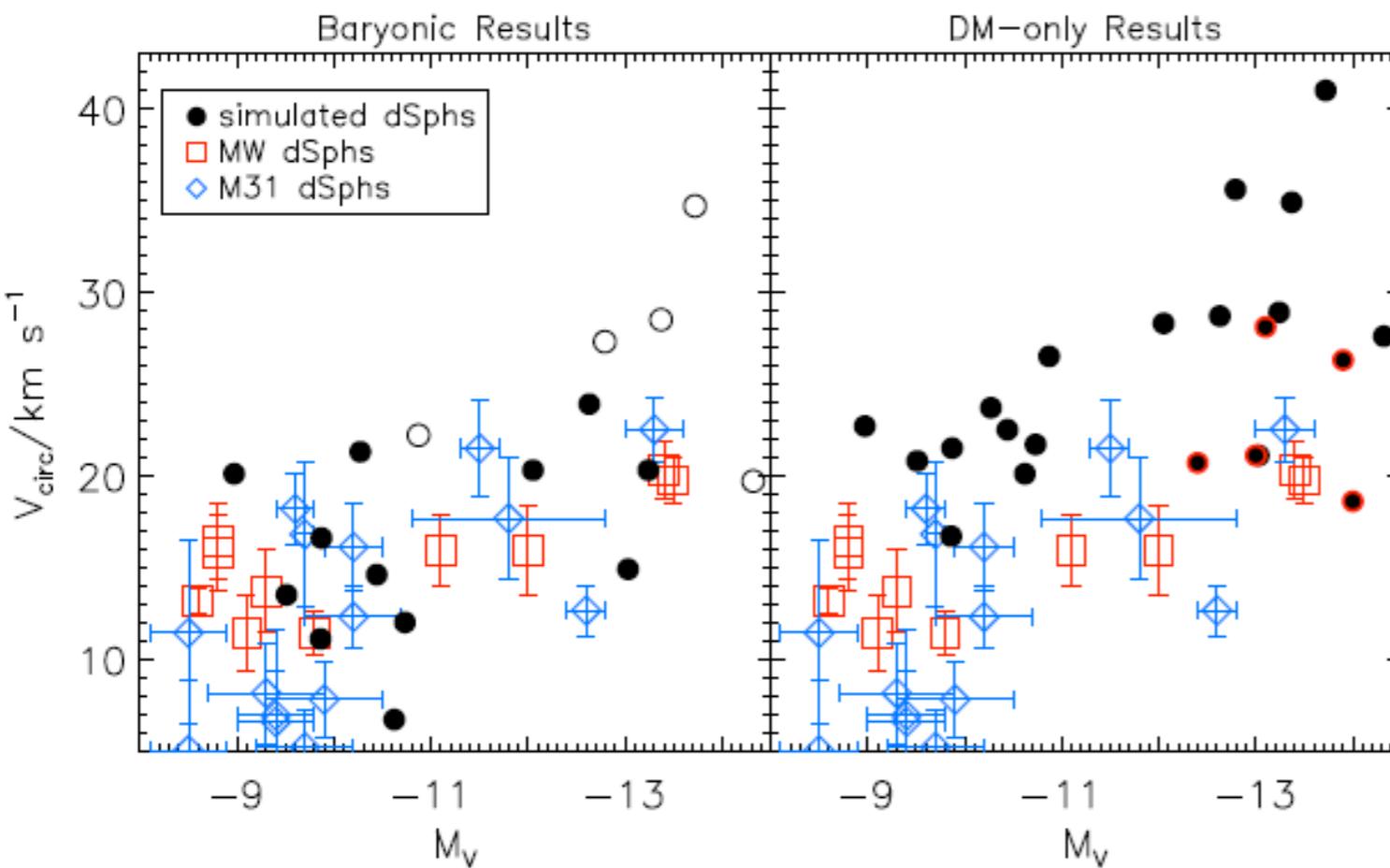
$$v_{\text{cir}} \sim r, \quad \rho_{\text{dm}} \sim r^0$$

“Cuspy”

“Cored”

Too-big-to-fail problem

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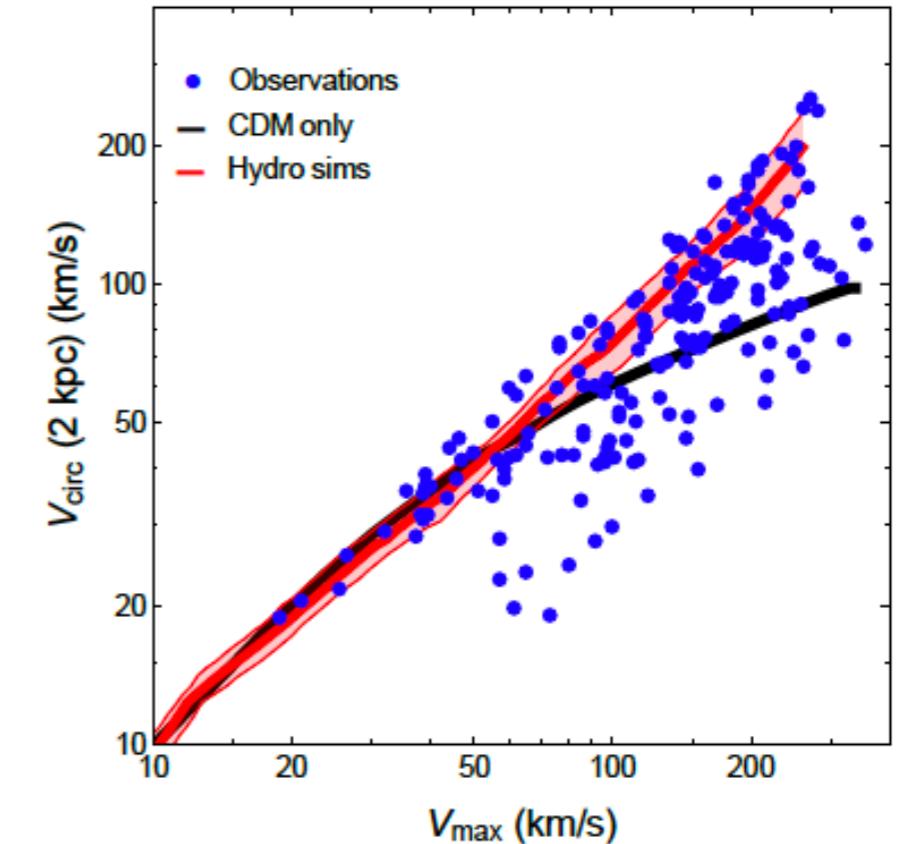


[Brooks & Zolotov, 2012]

Massive subhalos are too dense to host dwarf galaxies.

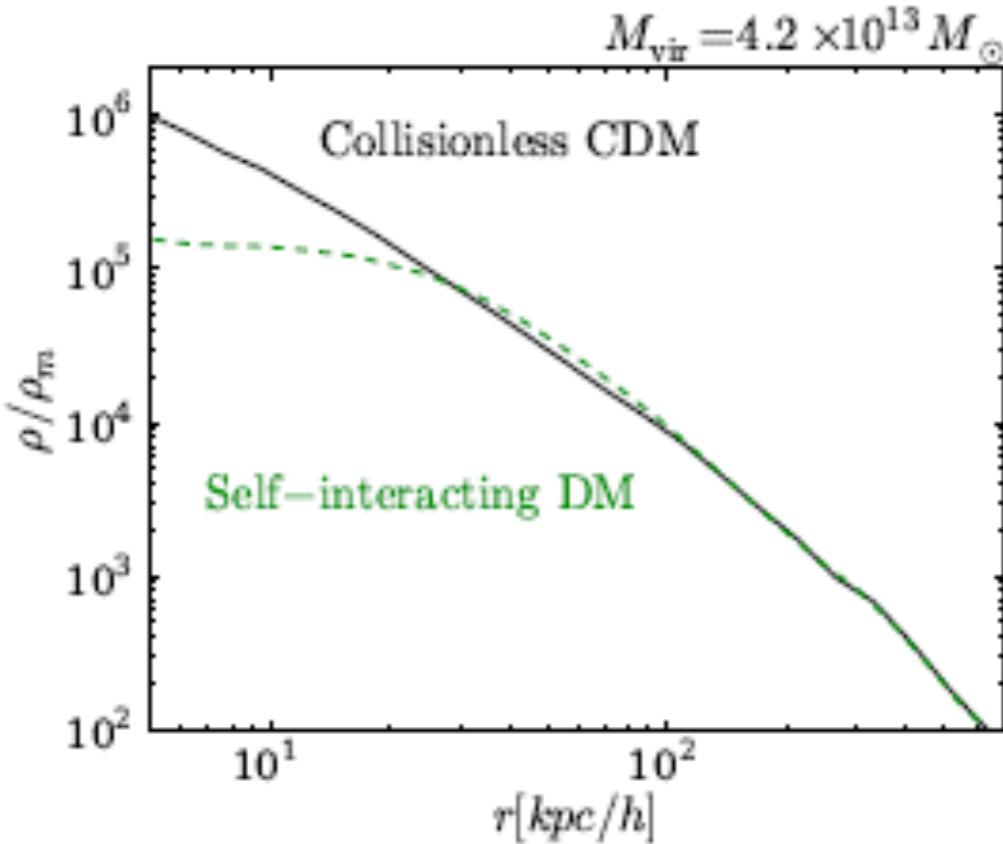
Baryonic effect (SN feedback) can make halo profile shallow.

Diversity problem: large scatter for the same maximum velocity

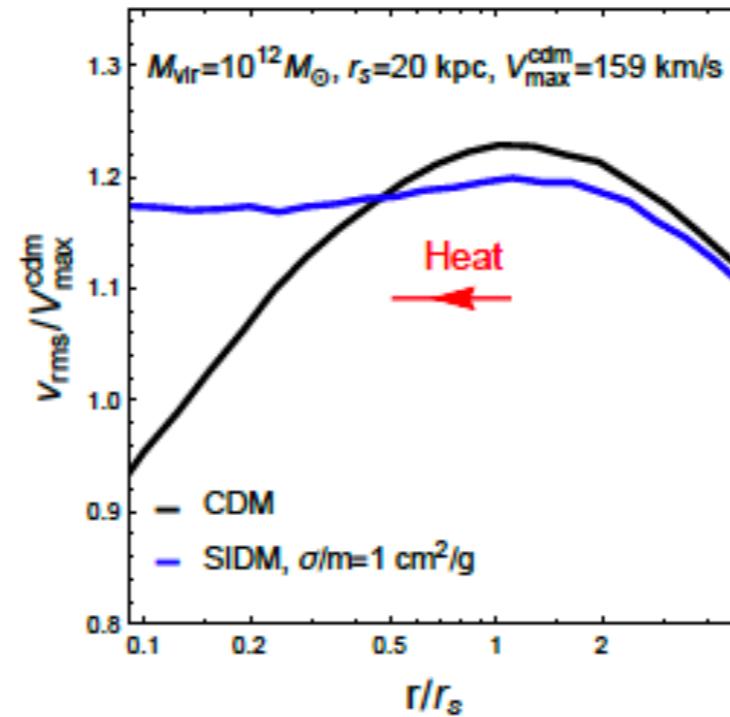


Self-Interacting Dark Matter

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[Weinberg et al, 2013]



[Tulin, Yu, 2017]

Transport heat from outside makes DM scatter and cored.

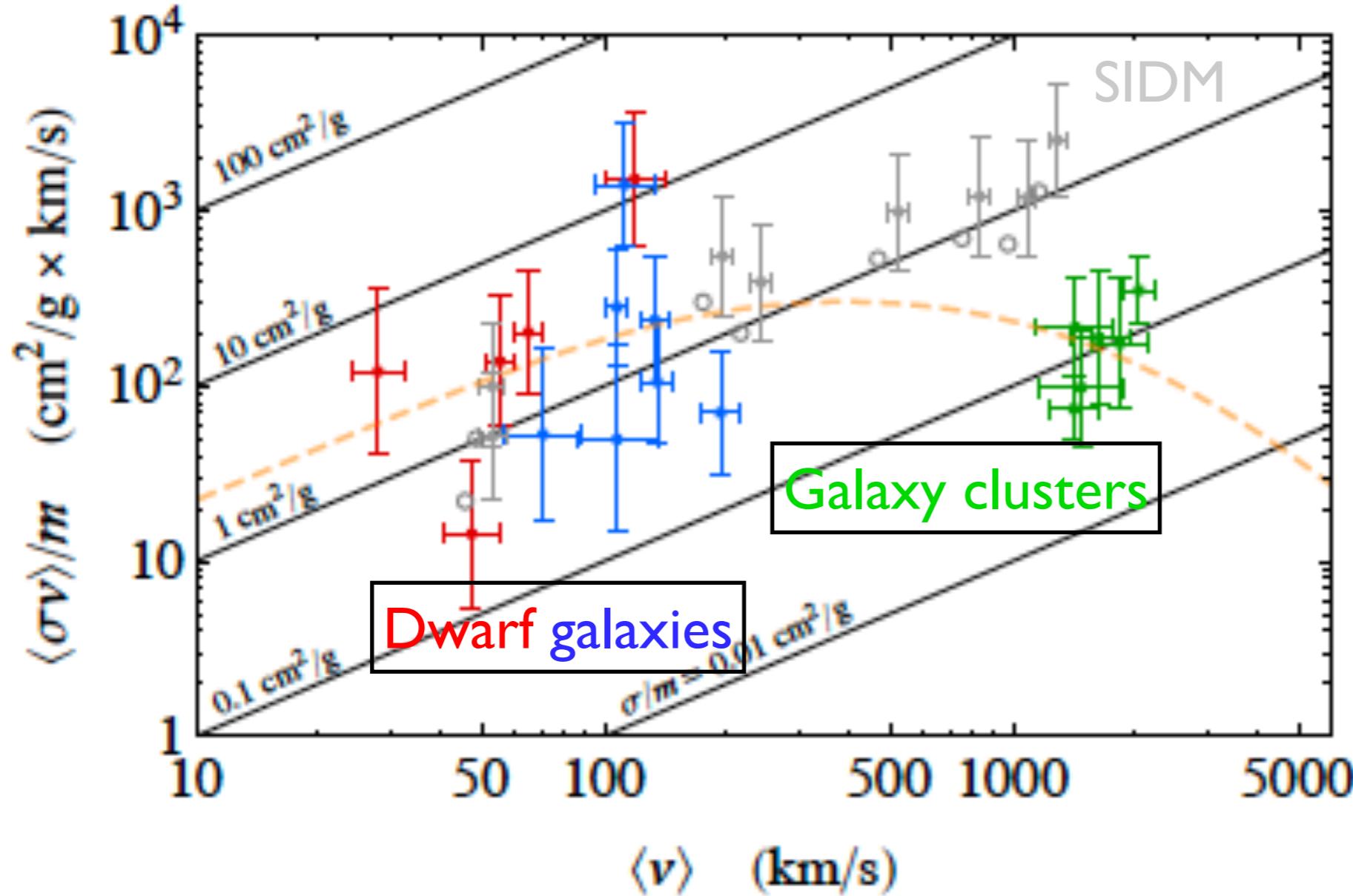
→ Self-Interacting cross section solves small-scale problems:

$$\frac{\sigma_{\text{self}}}{m_{\text{DM}}} \sim 0.1 - 10 \text{ cm}^2/\text{g}$$

cf. Bullet cluster for DM self-scattering at clusters. $\sigma/m \lesssim 0.7 \text{ cm}^2/\text{g}$

Velocity-dependent SIDM

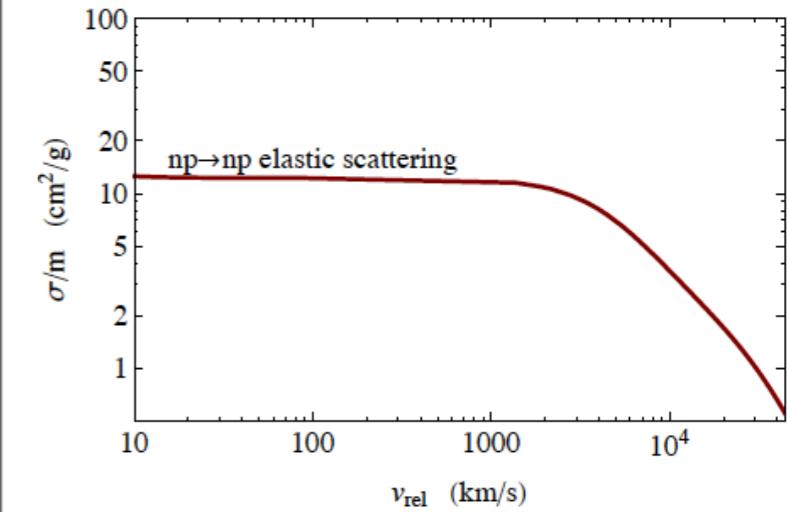
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THINGS dwarf galaxies (red), LSB galaxies (blue), and clusters (green).

SIDM *N*-body simulations, with $\sigma / m = 1 \text{ cm}^2/\text{g}$ (gray)

[M. Kaplinghat et al, 2015]



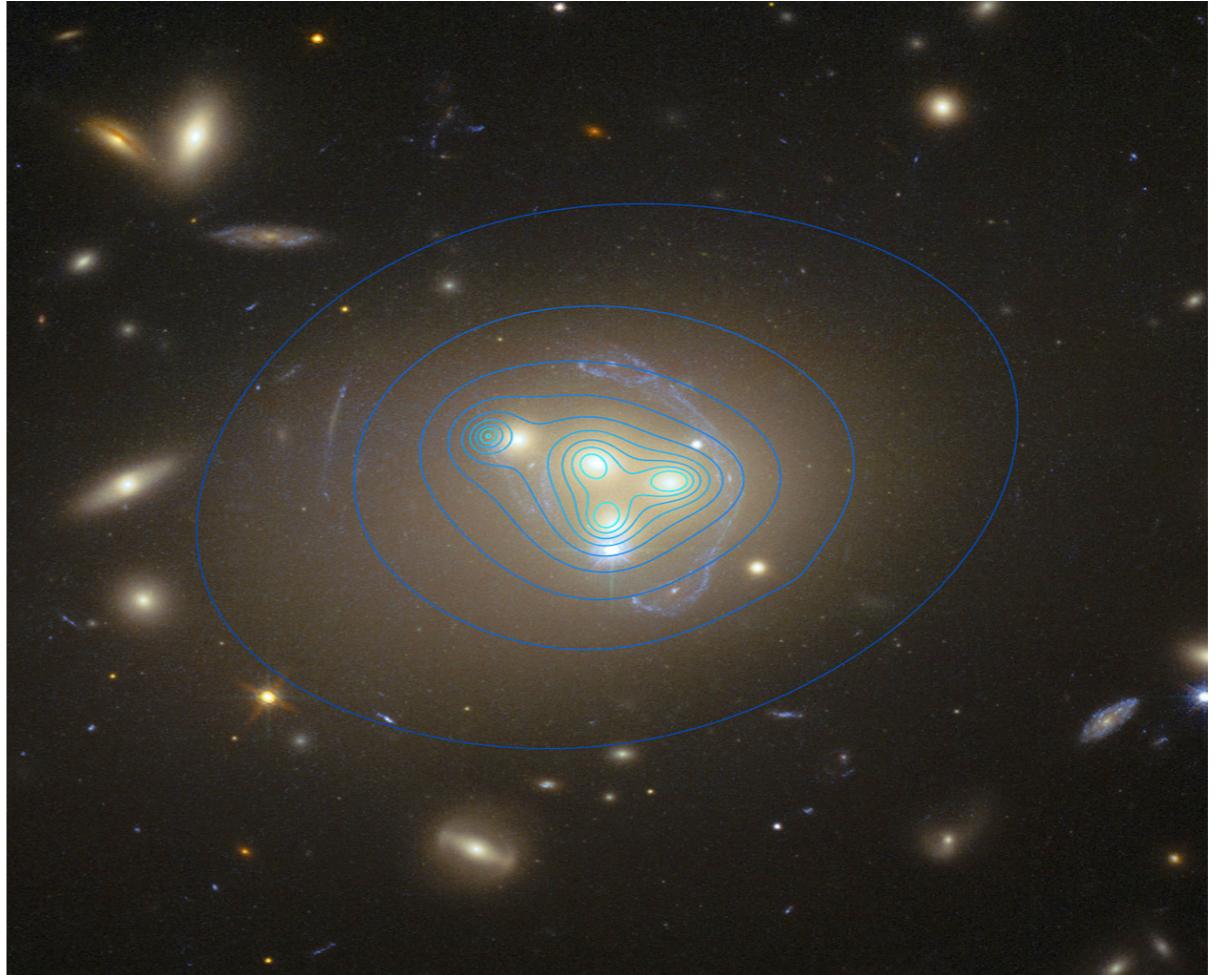
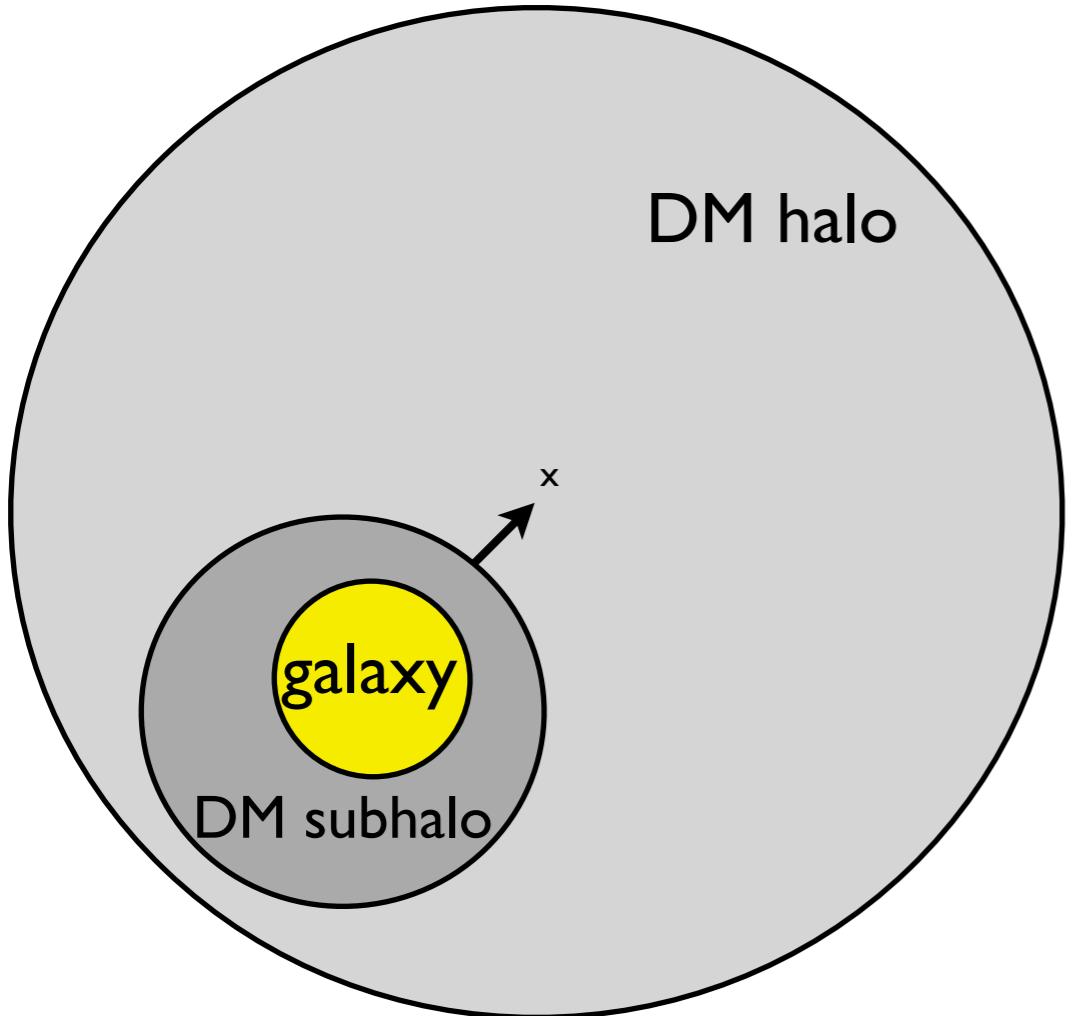
$$\rightarrow \sigma \propto \frac{1}{\langle v \rangle}$$

Suppressed cross section at clusters

- Velocity-dependence resolves tension galaxies & clusters.

SIDM: Halo separation

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Friction between halos > Gravity between sub-halo and galaxy

→ splitting of sub-halo from galaxy

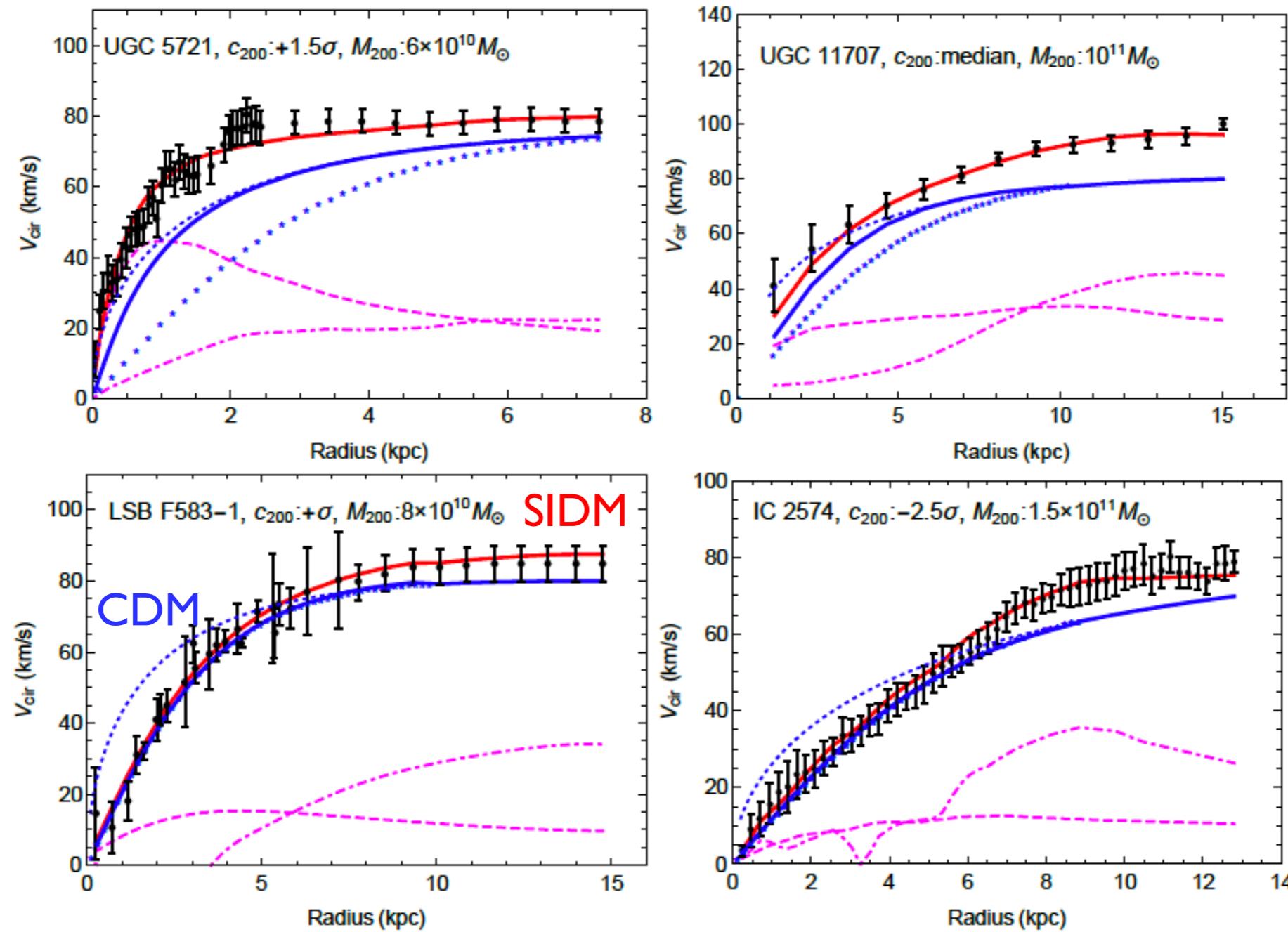
e.g. Abell 3827 cluster

off-set: $\Delta = 1.62^{+0.47}_{-0.49}$ kpc

[Massey et al(2015); F. Kalhoefer et al (2015)]

Diversity solved

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[A. Kamada et al, 2016]

SIDM with baryons explains diversity of rotation curves
at inner region for the same maximum velocity.

SIDM: resonances

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$$\times e^{-m_\phi r}$$

Mediator	Interaction	Yukawa	spin-spin	dipole
		$1/r$	$(\vec{s}_1 \cdot \vec{s}_2)/r$	D_{12}/r^3
Scalar	$\lambda_s \bar{\chi} \chi s$	$-\lambda_s^2$	0	0
Pseudoscalar	$i\lambda_a \bar{\chi} \gamma^5 \chi a$	0	$\frac{\lambda_a^2 m_a^2}{3m_\chi^2}$	$\frac{\lambda_a^2}{m_\chi^2} h(m_a, r)$
Goldstone	$\frac{1}{f} \bar{\chi} \gamma^\mu \gamma^5 \chi \partial_\mu a$	0	$\frac{4}{3} \frac{m_a^2}{f^2}$	$\frac{4}{f^2} h(m_a, r)$
Vector	$g_v \bar{\chi} \gamma^\mu \chi A_\mu$	$\pm g_v^2 \left(1 + \frac{m_A^2}{4m_\chi^2}\right)$	$\pm \frac{2g_v^2 m_A^2}{3m_\chi^2}$	$\mp \frac{g_v^2}{m_\chi^2} h(m_A, r)$
Axial vector	$g_a \bar{\chi} \gamma^\mu \gamma^5 \chi A_\mu$	0	$-\frac{8g_a^2}{3} \left(1 - \frac{m_A^2}{8m_\chi^2}\right)$	$g_a^2 \left(\frac{1}{m_\chi^2} + \frac{4}{m_A^2}\right) h(m_A, r)$
Field strength	$\frac{i}{2\Lambda} \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu}$	0	$\mp \frac{2m_A^2}{3\Lambda^2}$	$\pm \frac{1}{\Lambda^2} h(m_A, r)$
Graviton	$-\frac{1}{\Lambda} T^{X,\mu\nu} G_{\mu\nu}$	$-\frac{2m_X^2}{3\Lambda^2} \left(1 - \frac{3}{2} \frac{m_G^2}{m_S^2}\right)$	$-\frac{m_G^2}{3\Lambda^2}$	$\frac{1}{2\Lambda^2} h(m_G, r)$
Graviton	$-\frac{1}{\Lambda} T^{S,\mu\nu} G_{\mu\nu}$	$-\frac{2}{3\Lambda^2} \left(1 - \frac{1}{2} \frac{m_G^2}{m_S^2}\right)$	0	0
Graviton	$-\frac{1}{\Lambda} T^{X,\mu\nu} G_{\mu\nu}$	$-\frac{2}{3\Lambda^2} \left(1 + \frac{1}{6} \frac{m_G^2}{m_X^2}\right)$	$-\frac{m_G^2}{3\Lambda^2}$	$-\frac{1}{2\Lambda^2} h(m_G, r)$

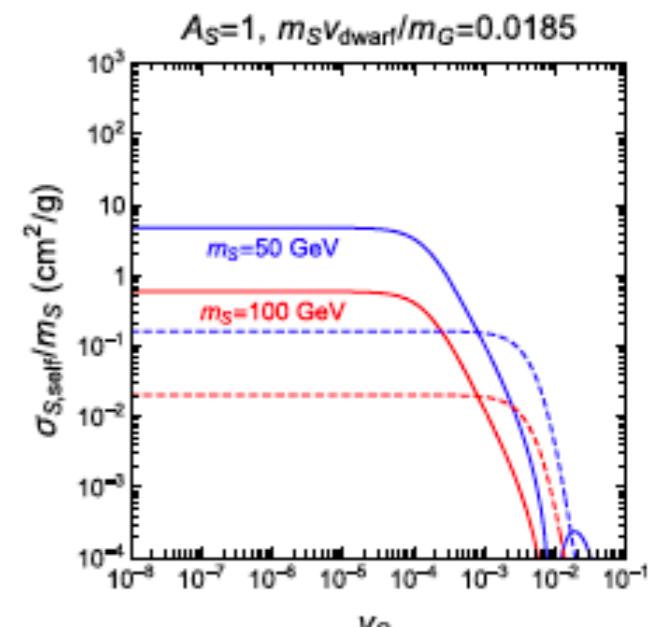
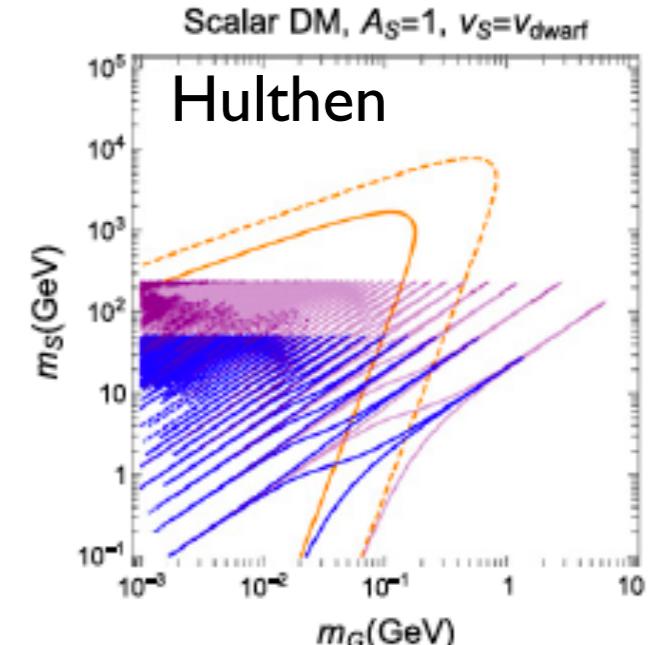
[Kang, HML, 2020]

$$h(m, r) = 1 + mr + \frac{1}{3}(mr)^2$$

Effective potential with light mediators:

$$V_{\chi,\text{eff}}(\mathbf{r}) = -\frac{1}{4m_\chi^2} \int \frac{d^3 q}{(2\pi)^3} e^{i\vec{q} \cdot \vec{r}} \mathcal{L}_{\chi,\text{eff}}$$

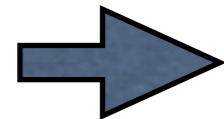
$$= \frac{1}{4\pi r} \left\{ c_1(r) + c_2(r)(\vec{s}_1 \cdot \vec{s}_2) + \frac{c_3(r)}{m_\chi^2 r^2} [3(\vec{s}_1 \cdot \hat{r})(\vec{s}_2 \cdot \hat{r}) - \vec{s}_1 \cdot \vec{s}_2] + \frac{c_7(r)}{m_\chi r} (\vec{s}_1 + \vec{s}_2) \cdot (\hat{r} \times \vec{v}) \right\} \times e^{-m_\phi r}$$



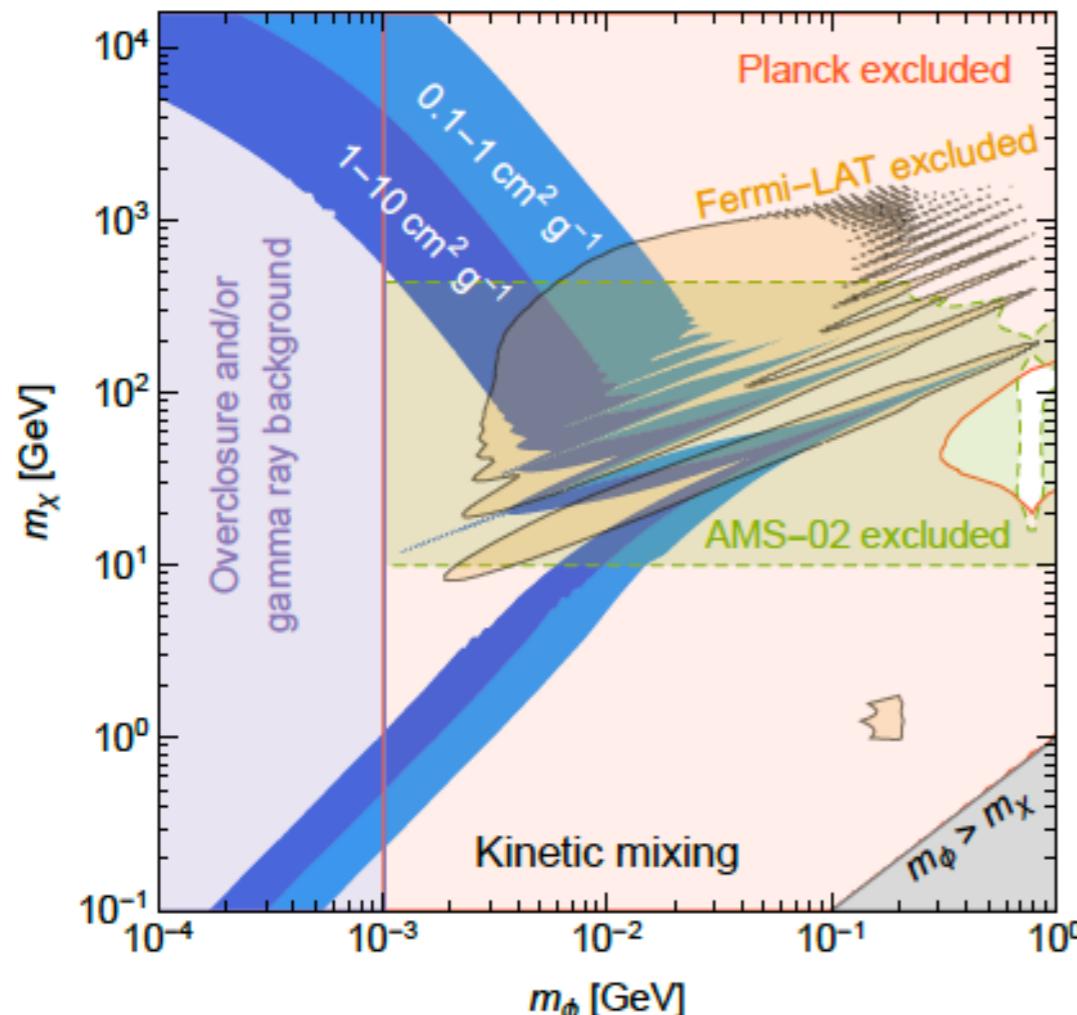
Bounds on light mediators

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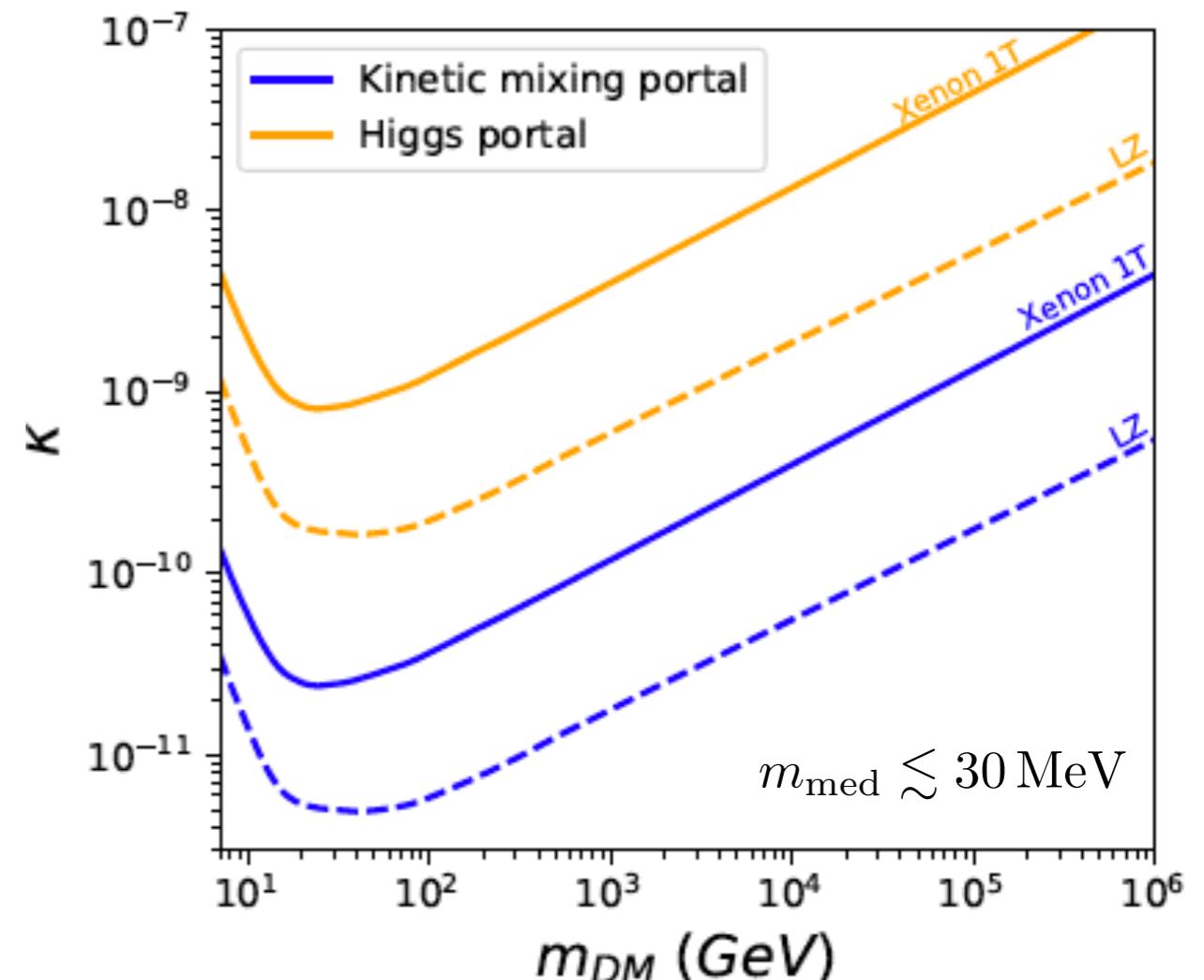
Light mediators enhance dark matter annihilations/detection.



Strong constraints from indirect and direct detections.



[Bringmann et al, 2016]



[Hambye et al, 2019]

Dark matter annihilates into neutrinos or hidden sector particles.

SIDM: sub-GeV

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Born cross section (w/ heavy mediator):

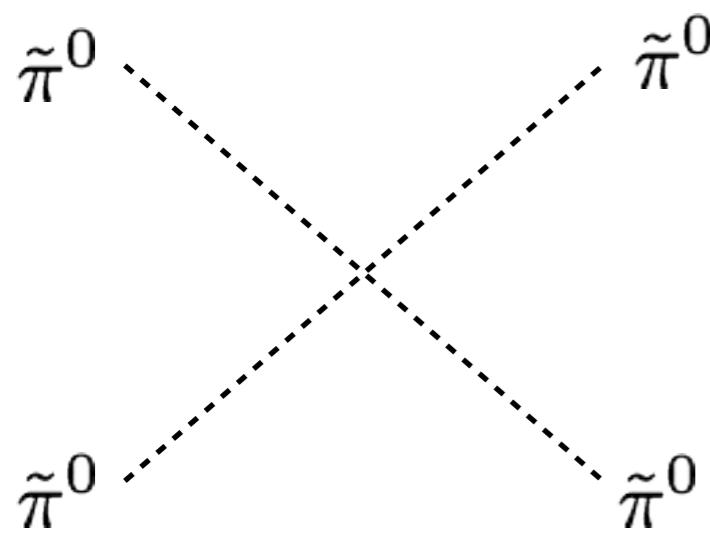
$$\sigma_T^{\text{Born}} = \frac{A_{\text{DM}}^2}{2\pi m_{\text{DM}}^2 v^4} \left[\ln \left(1 + \frac{m_{\text{DM}}^2 v^2}{m_G^2} \right) - \frac{m_{\text{DM}}^2 v^2}{m_G^2 + m_{\text{DM}}^2 v^2} \right] , \quad \left(V = -\frac{A_{\text{DM}}}{4\pi} \frac{e^{-m_G r}}{r} \right)$$

sub-GeV DM mass => large & velocity-dependent at perturbative level.

DM relic freeze-out with $2 \rightarrow 2$ (forbidden) annihilation: CMB safe

Contact interactions:

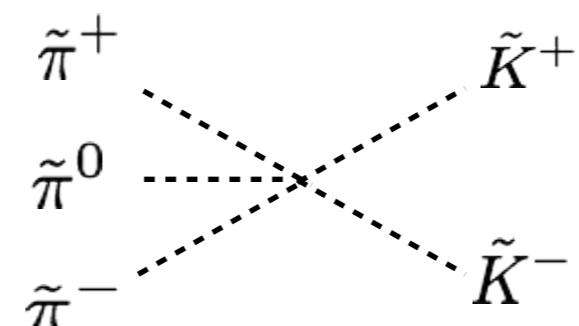
e.g. Dark mesons in dark QCD



[Hochberg et al, 2014;
M.-S. Seo, HML, 2015]

$$\mathcal{L}_0 = \text{Tr}(\partial_\mu \pi \partial^\mu \pi) + \frac{1}{3f^2} \text{Tr}[\partial_\mu \pi, \pi]^2 + \dots$$

$$\sigma_{\text{self}} = \frac{m_\pi^2}{32\pi f^4} \frac{a^2}{N_\pi^2}, \quad a^2 \sim N_\pi^4 \longrightarrow m_\pi \lesssim 1 \text{ GeV}$$



Wess-Zumino-Witten term:
DM relic by self-interactions

$$\frac{m_\pi}{f} \sim 4, \quad m_\pi \sim 300 \text{ MeV}$$

u-channel resonances

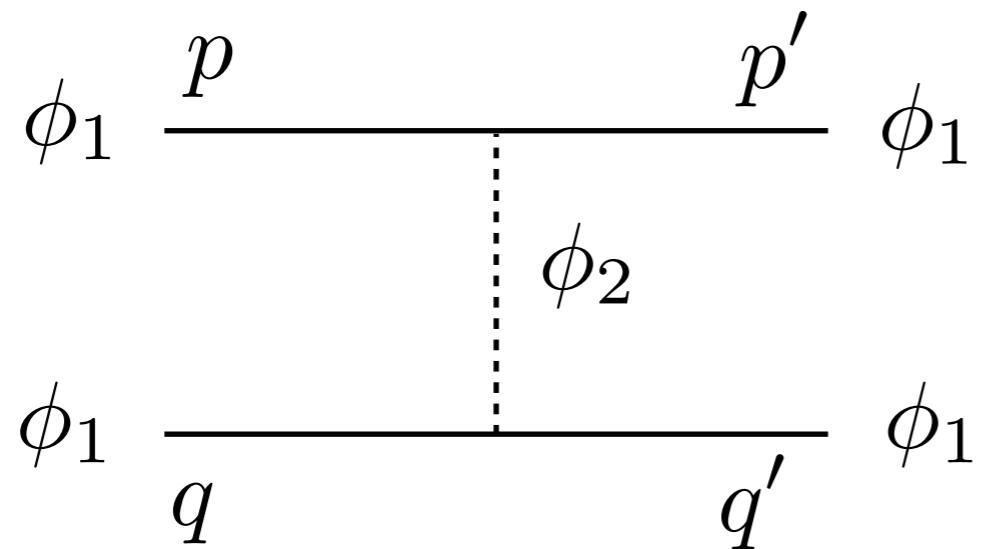
t-channel resonance

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- Consider dark matter and mediator with masses, m_1 & m_2 .

Self-coupling for dark matter: $\mathcal{L}_{\text{int}} = -2g m_1 \phi_2 |\phi_1|^2$

→ Elastic 2→2 self-scattering in t-channel



$$\tilde{\Gamma}_t(p, q; p', q') = \frac{4g^2 m_1^2}{|\vec{p} - \vec{p}'|^2 + m_2^2 - \omega^2}$$

$w = p_0 - p'_0 \simeq 0$: “Instantaneous” interaction

→ A small mass m_2 leads to enhanced t-channel!

Resummation of ladder diagrams: Sommerfeld factor

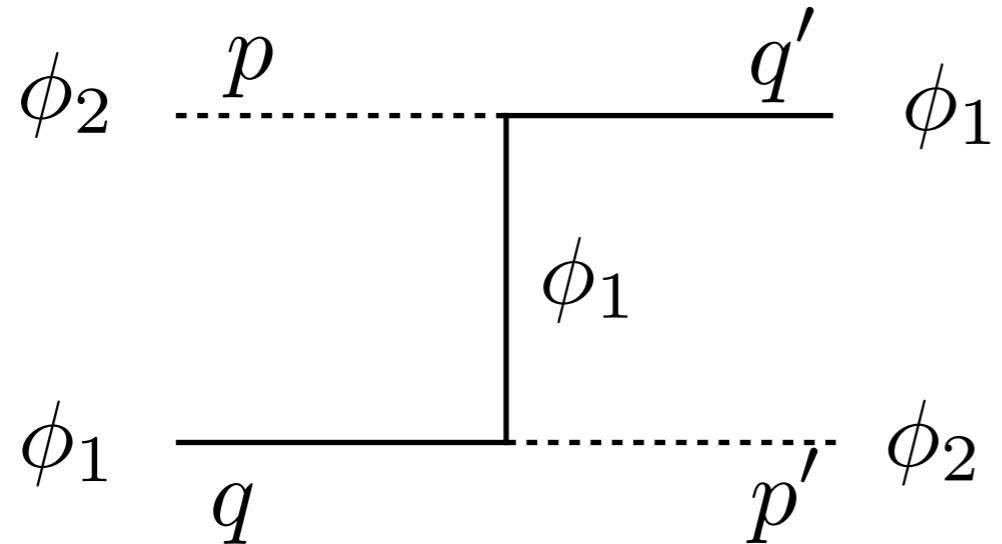
u-channel resonance

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- Take two component dark matter with masses, m_1 & m_2

Self-coupling between dark matter: $\mathcal{L}_{\text{int}} = -2g m_1 \phi_2 |\phi_1|^2$

→ Elastic 2→2 co-scattering in u-channel



$$\tilde{\Gamma}_u(p, q; p', q') = \frac{4g^2 m_1^2}{|\vec{p} - \vec{q}'|^2 + m_1^2 - \omega^2}$$

[S. Kim, HML, B. Zhu, 2021, 2022]

$\omega = p_0 - q'_0 \approx m_2 - m_1 \neq 0$ “Delayed” interaction

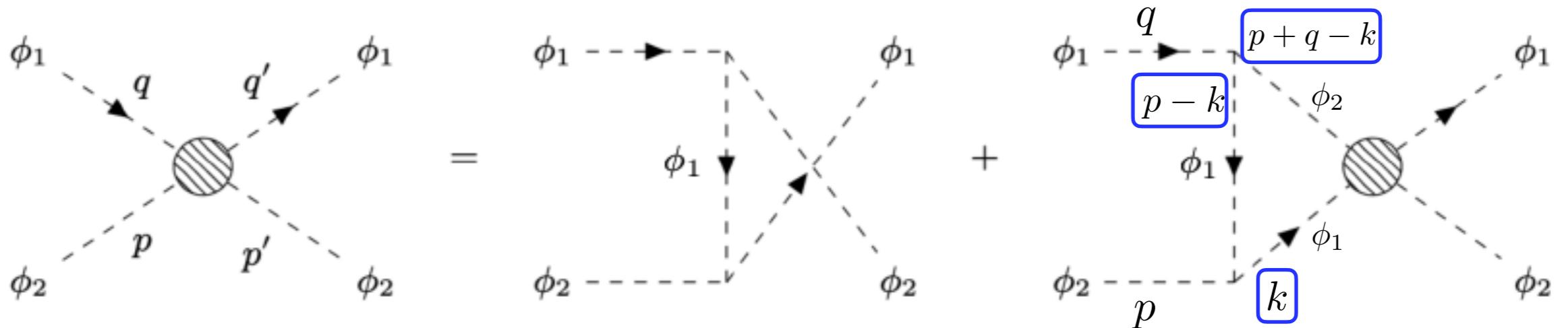
$m_2 = 2m_1 \longrightarrow$ “Effectively massless” off-shell DM

Similar resummation of ladder diagrams is also needed.

Non-perturbative scattering

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Non-perturbative co-scattering in u-channel



$$i\Gamma(p, q; p', q') = i\tilde{\Gamma}(p, q; p', q') - \int \frac{d^4k}{(2\pi)^4} \tilde{\Gamma}(p, q; p + q - k, k) G_1(k) G_2(p + q - k) \Gamma(p + q - k, k; p', q')$$

Bethe-Salpeter wave function for two-component DM:

$$\chi(p, q; p', q') \equiv G_2(p) G_1(q) \Gamma(p, q; p', q') \equiv \chi(p, q)$$

→ $i\chi(p, q) = -G_2(p) G_1(q) \int \frac{d^4k}{(2\pi)^4} \tilde{\Gamma}(p, q; p + q - k, k) \chi(p + q - k, k)$

(tree-level amplitude ignored)

Bethe-Salpeter equation

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Change of variables:

$$P = \frac{1}{2}(p + q), \quad Q = \mu\left(\frac{p}{m_2} - \frac{q}{m_1}\right) \longrightarrow \begin{cases} \chi(p, q) = \tilde{\chi}(P, Q) \\ \chi(p + q - k, k) = \tilde{\chi}\left(P, \frac{2\mu}{m_2}P - k\right) \end{cases}$$

$$i\tilde{\chi}(P, Q) = -G_2\left(Q + \frac{2\mu}{m_1}P\right)G_1\left(-Q + \frac{2\mu}{m_2}P\right) \int \frac{d^4k'}{(2\pi)^4} \tilde{\Gamma}(p, q; p + q - k, k) \tilde{\chi}(P, k')$$

k' : shifted loop momentum

Tree-level amplitude:

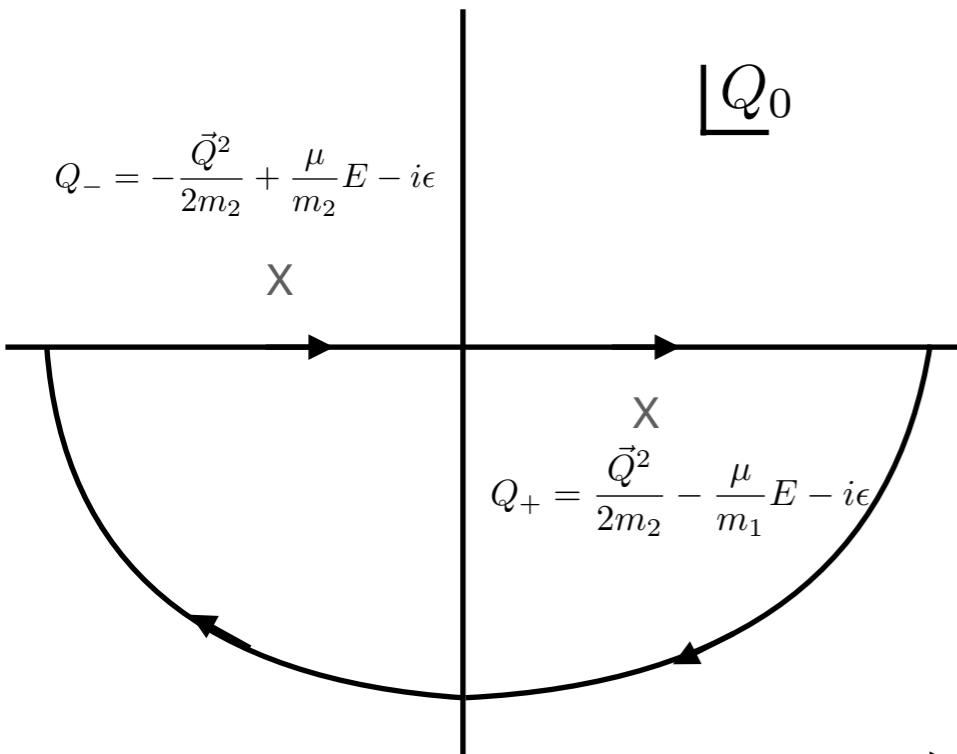
$$\tilde{\Gamma}(p, q; p + q - k, k) = \frac{4g^2 m_1^2}{\left(\sqrt{\frac{m_1}{m_2}}\vec{Q} + \sqrt{\frac{m_2}{m_1}}\vec{k}'\right)^2 + m_2(2m_1 - m_2)} \equiv U$$

BS w.f. in momentum space: $\tilde{\psi}_{BS}(\vec{Q}) = \int \frac{dQ_0}{2\pi} \tilde{\chi}(P, Q)$

$$\longrightarrow i\tilde{\psi}_{BS}(\vec{Q}) = - \int \frac{dQ_0}{2\pi} G_2\left(Q + \frac{2\mu}{m_1}P\right)G_1\left(-Q + \frac{2\mu}{m_2}P\right) \int \frac{d^3k'}{(2\pi)^3} U \tilde{\psi}_{BS}(\vec{k}')$$

Bethe-Salpeter equation

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$$P = \frac{1}{2}(m_1 + m_2 + E, 0), \quad Q = (Q_0, \vec{Q}):$$

$$G_2 = \frac{i}{(Q + \frac{2\mu}{m_1} P)^2 - m_2^2 + i\epsilon} \simeq \frac{i}{2m_2(Q_0 - Q_+)},$$

$$G_1 = \frac{i}{(-Q + \frac{2\mu}{m_2} P)^2 - m_1^2 + i\epsilon} \simeq \frac{i}{2m_1(Q_0 - Q_-)}$$

$$\int \frac{dQ_0}{2\pi} G_2\left(Q + \frac{2\mu}{m_1} P\right) G_1\left(-Q + \frac{2\mu}{m_2} P\right) = \frac{i}{4m_1 m_2 \left(E - \frac{\vec{Q}^2}{2\mu}\right)}$$

Bethe-Salpeter equation:

$$\left(-\frac{1}{2\mu} \nabla^2 - E\right) \psi_{BS}(\vec{x}) = -V(\vec{x}) \psi_{BS}\left(-\frac{m_2}{m_1} \vec{x}\right)$$

[S. Kim, HML, B. Zhu, 2021, 2022]

$$\begin{cases} V(\vec{x}) = -\frac{\alpha}{r} e^{-Mr} \\ \alpha \equiv \frac{g^2}{4\pi}, \quad M \equiv m_2 \sqrt{2 - \frac{m_2}{m_1}} \end{cases} \rightarrow$$

$m_2 \lesssim 2m_1 : M \ll m_2$

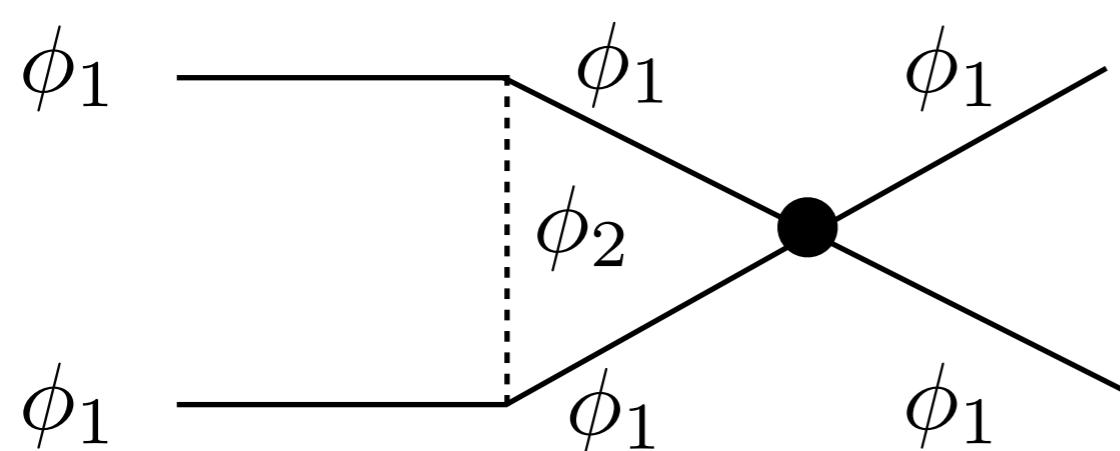
Effective light resonance

Difference from t-channel

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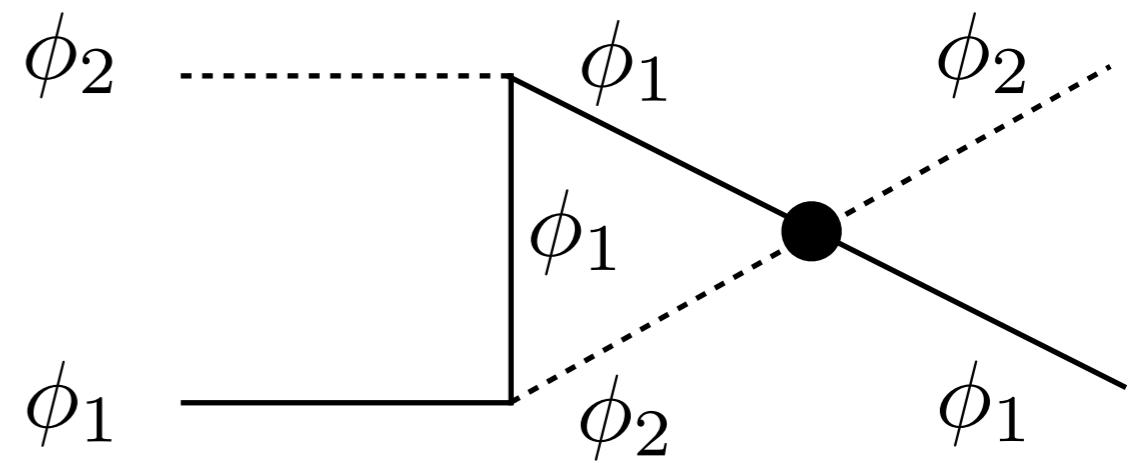
t-channel:

$$\tilde{\Gamma}_t = \frac{4g^2 m_1^2}{|\vec{p} - \vec{p}'|^2 + m_2^2}$$



u-channel:

$$\tilde{\Gamma}_u = \frac{4g^2 m_1^2}{\left| \sqrt{\frac{m_1}{m_2}} \vec{p} - \sqrt{\frac{m_2}{m_1}} \vec{q}' \right|^2 + m_2(2m_1 - m_2)}$$



$$\chi(1, 1') \sim \tilde{\Gamma}_t \chi(1, 1')$$

$$\left(\frac{\nabla^2}{2\mu} + E \right) \psi(\vec{x}) = V(\vec{x}) \psi(\vec{x})$$

No DM exchange in loops =>
No flip for BS wave-function

$$\chi(1, 2) \sim \tilde{\Gamma}_u \underline{\chi(2, 1)}$$

$$\left(\frac{\nabla^2}{2\mu} + E \right) \psi(\vec{x}) = V(\vec{x}) \psi\left(-\frac{m_2}{m_1} \vec{x} \right)$$

DM exchange in loops =>
BS wave-function flips in the potential!

Delayed interactions

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BS w.f. in spherical coordinates:

$$\psi_{\text{BS}}(\vec{x}) = R_l(r)Y_l^m(\theta, \phi) \longrightarrow \psi_{\text{BS}}\left(-\frac{m_2}{m_1}\vec{x}\right) = (-1)^l R_l\left(\frac{m_2}{m_1}r\right)Y_l^m(\theta, \phi)$$

Radial equation : $R_l(x) = u_l(x)/x$, $a = \frac{2v_{\text{rel}}}{\alpha}$, $b = \frac{m_2}{m_1}$ and $c = \frac{2M}{\mu\alpha}$

$$\rightarrow \left(\frac{d^2}{dx^2} - \frac{l(l+1)}{x^2} \right) u_l(x) + \frac{4e^{-cx}}{bx} (-1)^l u_l(bx) + a^2 u_l(x) = 0$$

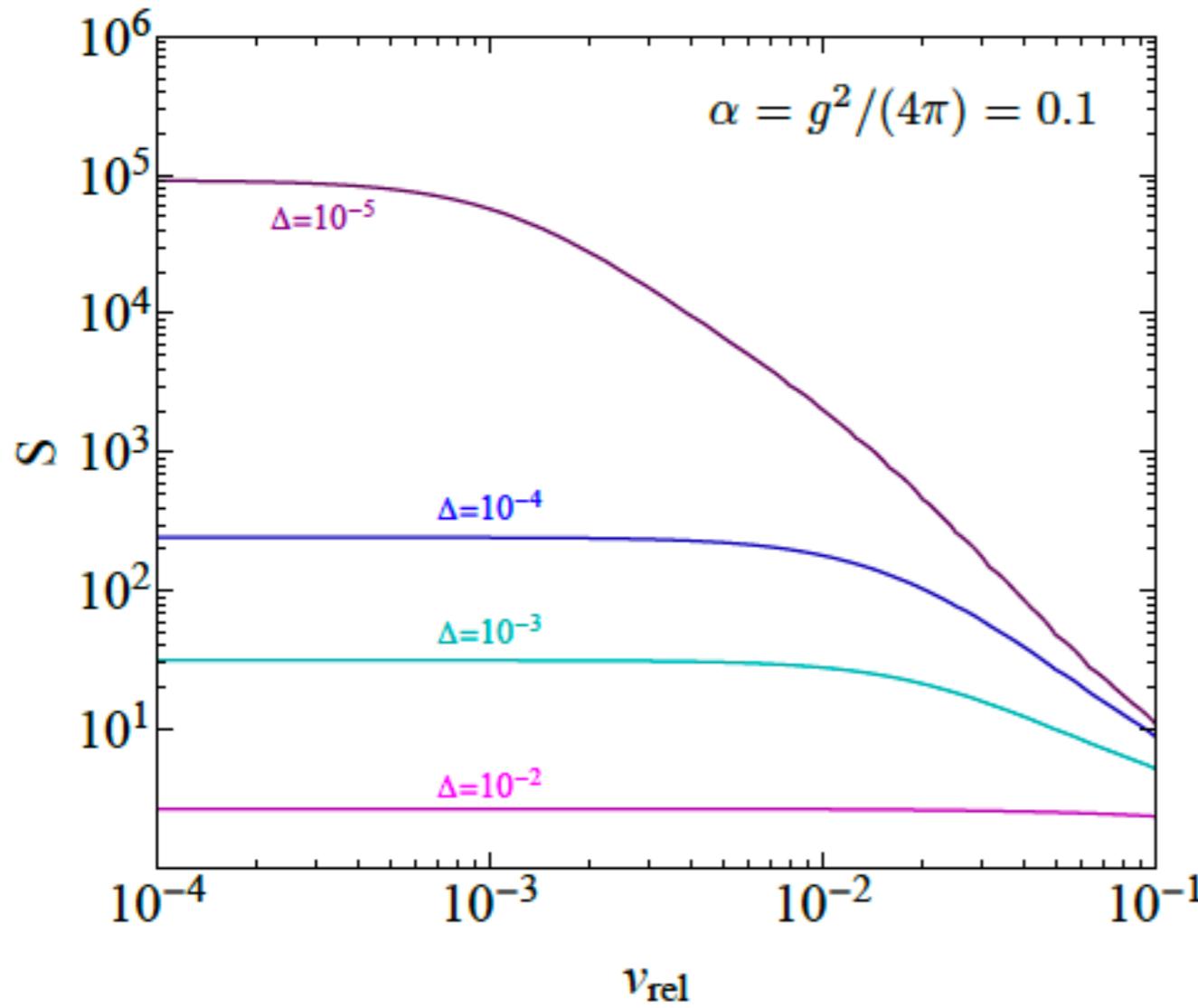
- Attractive for $l=\text{even}$; repulsive for $l=\text{odd}$.
- Effective mediator mass: $M \equiv m_2 \sqrt{2 - \frac{m_2}{m_1}} \rightarrow 0$, $m_2 \rightarrow 2m_1$.
- Delay differential eq:

$$x = e^{-\rho} \longrightarrow \tilde{u}_0''(\rho) + \tilde{u}_0'(\rho) + 2e^{-\rho} \tilde{u}_0(\rho - \ln 2) + a^2 e^{-2\rho} \tilde{u}_0(\rho) = 0$$

delay term

Sommerfeld factor

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Sommerfeld factor (s-wave):

$$S = \frac{|\psi_{\text{BS}}(0)|^2}{|\psi_{\text{pert}}(0)|^2} = A^2$$

Effective mediator mass

$$\leftrightarrow \quad \Delta = 1 - \frac{m_2}{2m_1} \geq 0$$

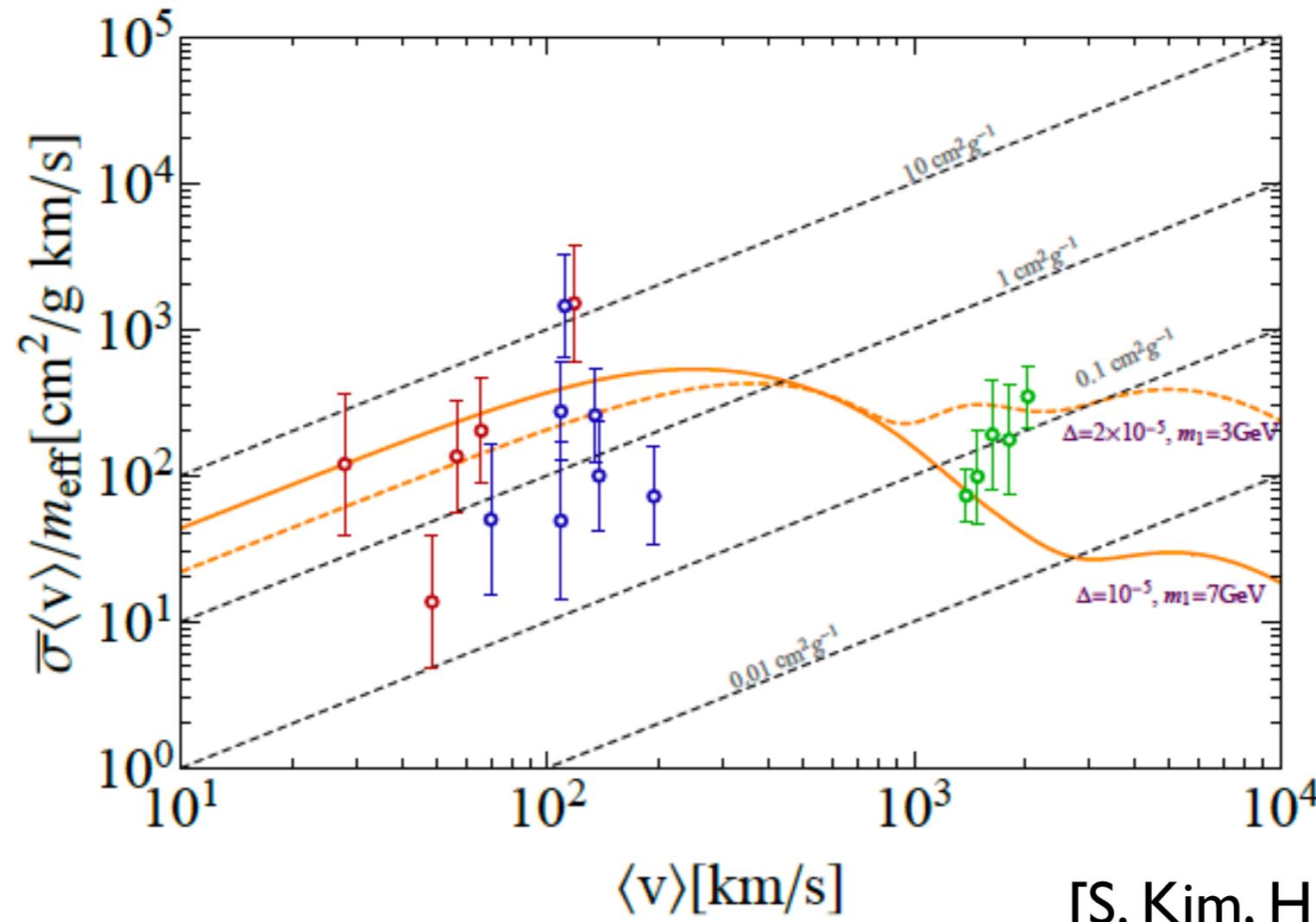
[S. Kim, HML, B. Zhu, 2021]

Boundary conditions (s-wave):

$$\tilde{u}_0(\rho) \rightarrow \frac{1}{a} \sin(a e^{-\rho} + \delta_0), \quad \rho \rightarrow -\infty, \quad \text{“plane-wave”}$$
$$\tilde{u}_0(\rho) \rightarrow A e^{-\rho}, \quad \rho \rightarrow +\infty \quad \text{“constant R”}$$

u-channel co-scattering

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$\phi_1 \phi_2 \rightarrow \phi_1 \phi_2 : \quad \sigma = \frac{4\pi}{k^2} \sin^2 \delta_0 \quad , \text{ total cross section}$

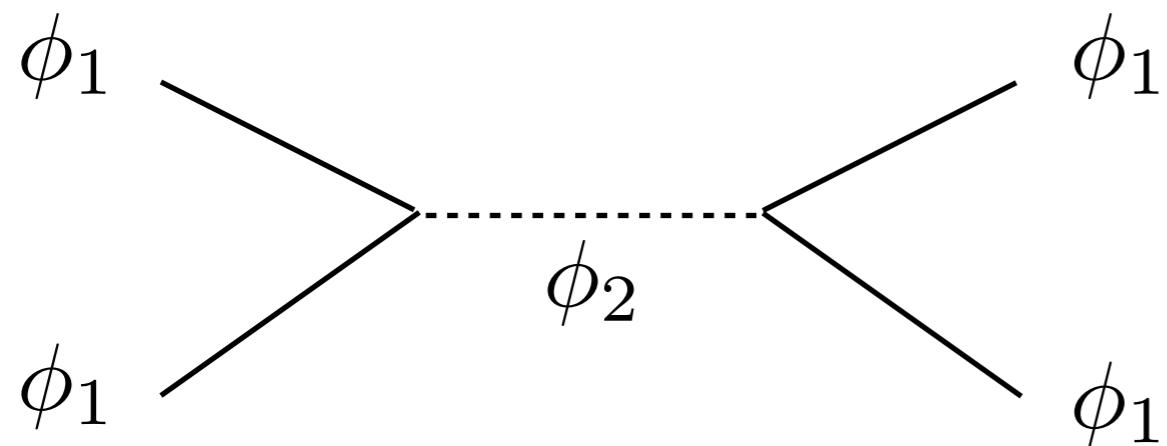
$\bar{\sigma} = \langle \sigma v_{\text{rel}}^3 \rangle / (24/\sqrt{\pi} v_0^3) : \text{energy-transfer average}$

→ Self-scattering for SRDM is velocity-dependent.

Other channels for SIDM

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s-channel

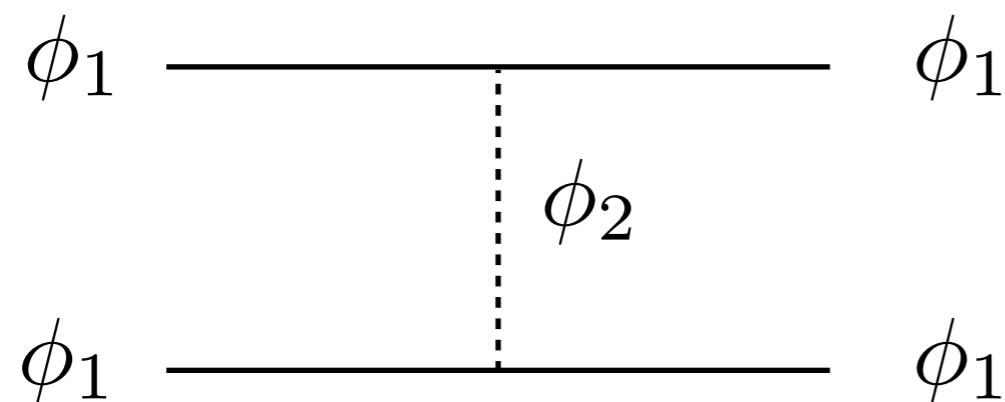


$$\sim \frac{1}{(m_1^2(4 + v_{\text{rel}}^2) - m_2^2)^2 + \Gamma_2^2 m_2^2}$$

u-channel mass: $M \equiv m_2 \sqrt{2 - \frac{m_2}{m_1}}$ $\longrightarrow m_2 < 2m_1$

off resonance

t-channel



$$m_2 \approx 2m_1$$

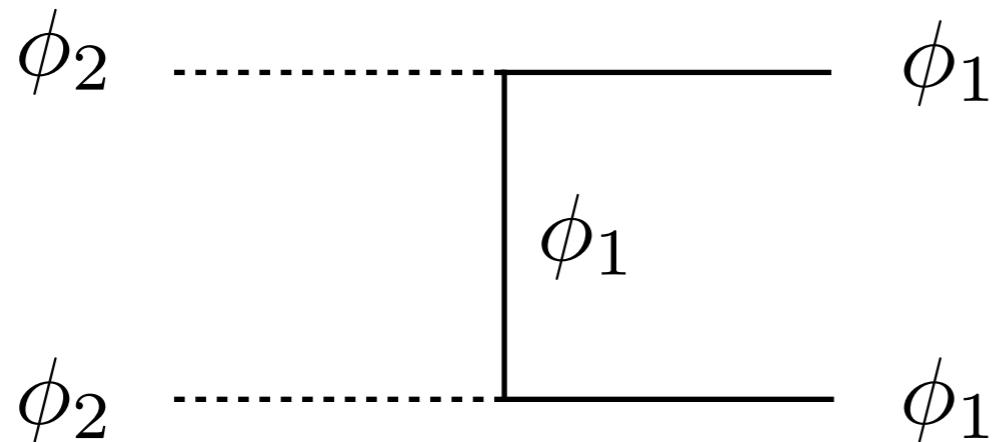
No enhancement

Models for u-channel resonances

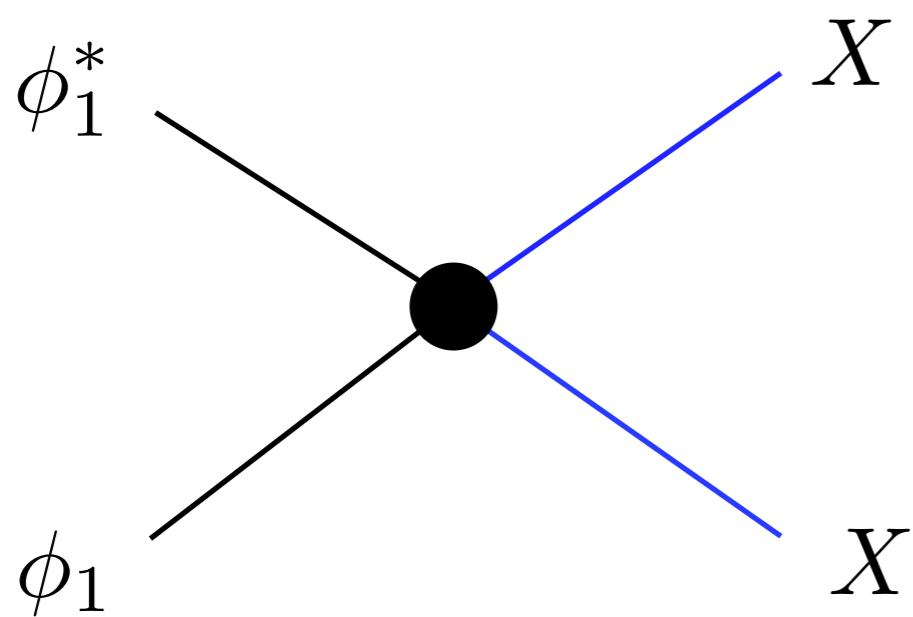
DM annihilation

-20-

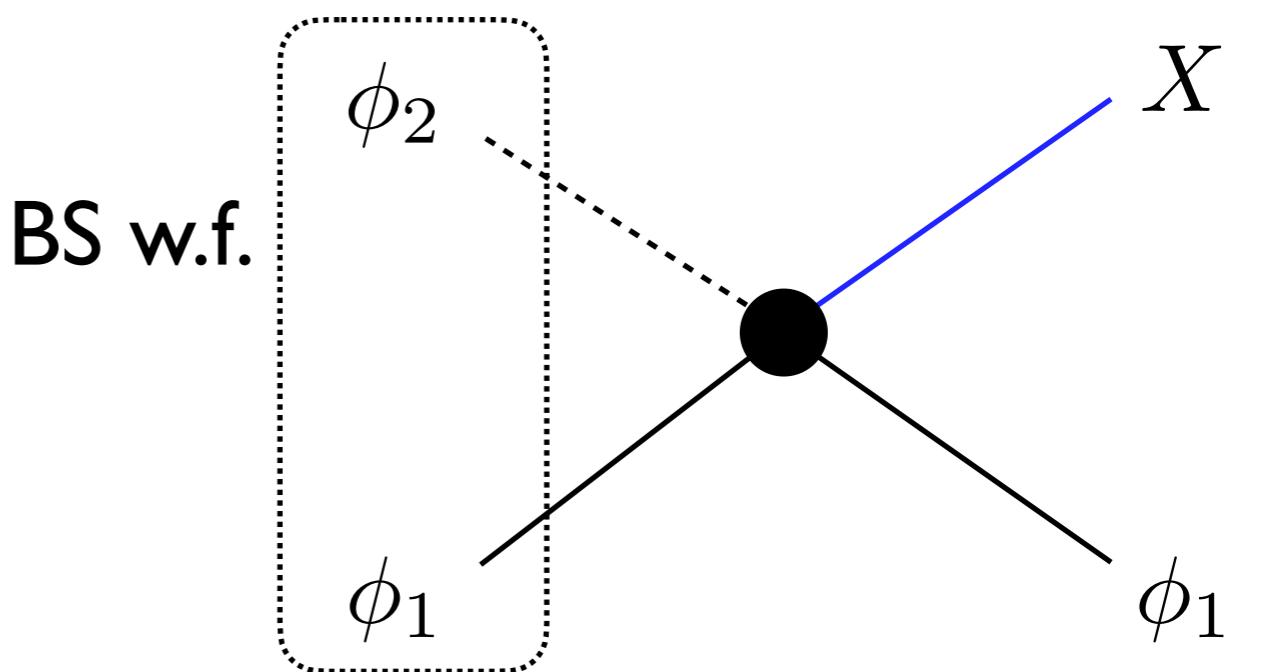
2→2 annihilation



Annihilation of heavier DM is always present in u-channel models.



Need to annihilate lighter DM
 X : extra mediator

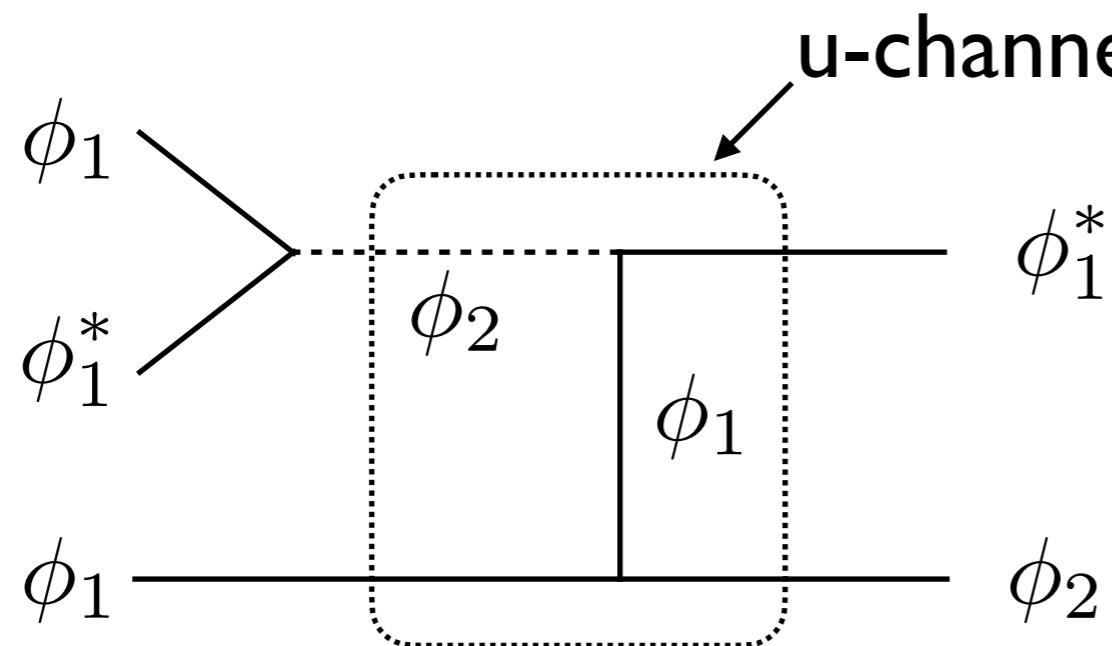


u-channel
Sommerfeld enhancement

DM annihilation

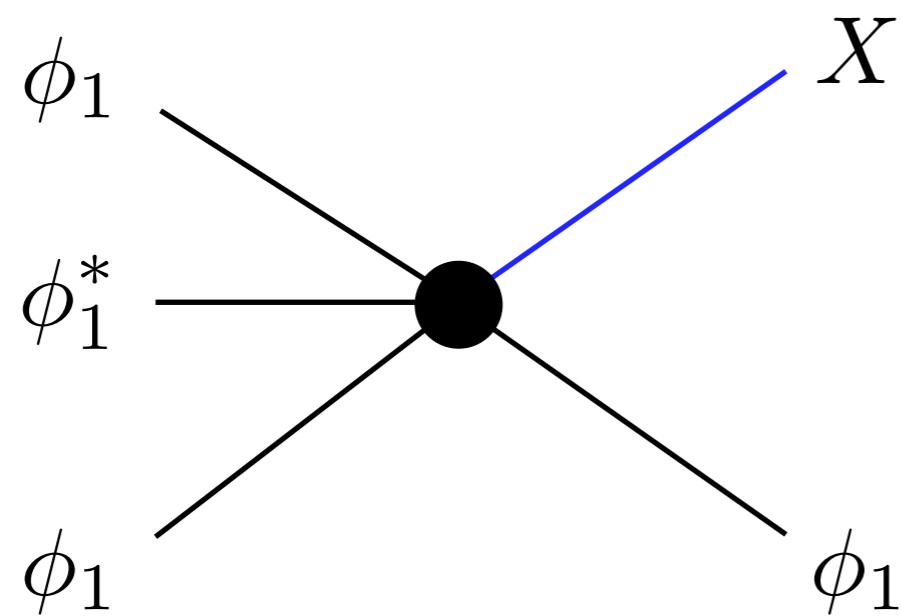
-21-

$3 \rightarrow 2$ annihilation



$$\sim \frac{1}{(4m_1^2 - m_2^2)^4}$$

s-, u-channels enhanced
at tree level.



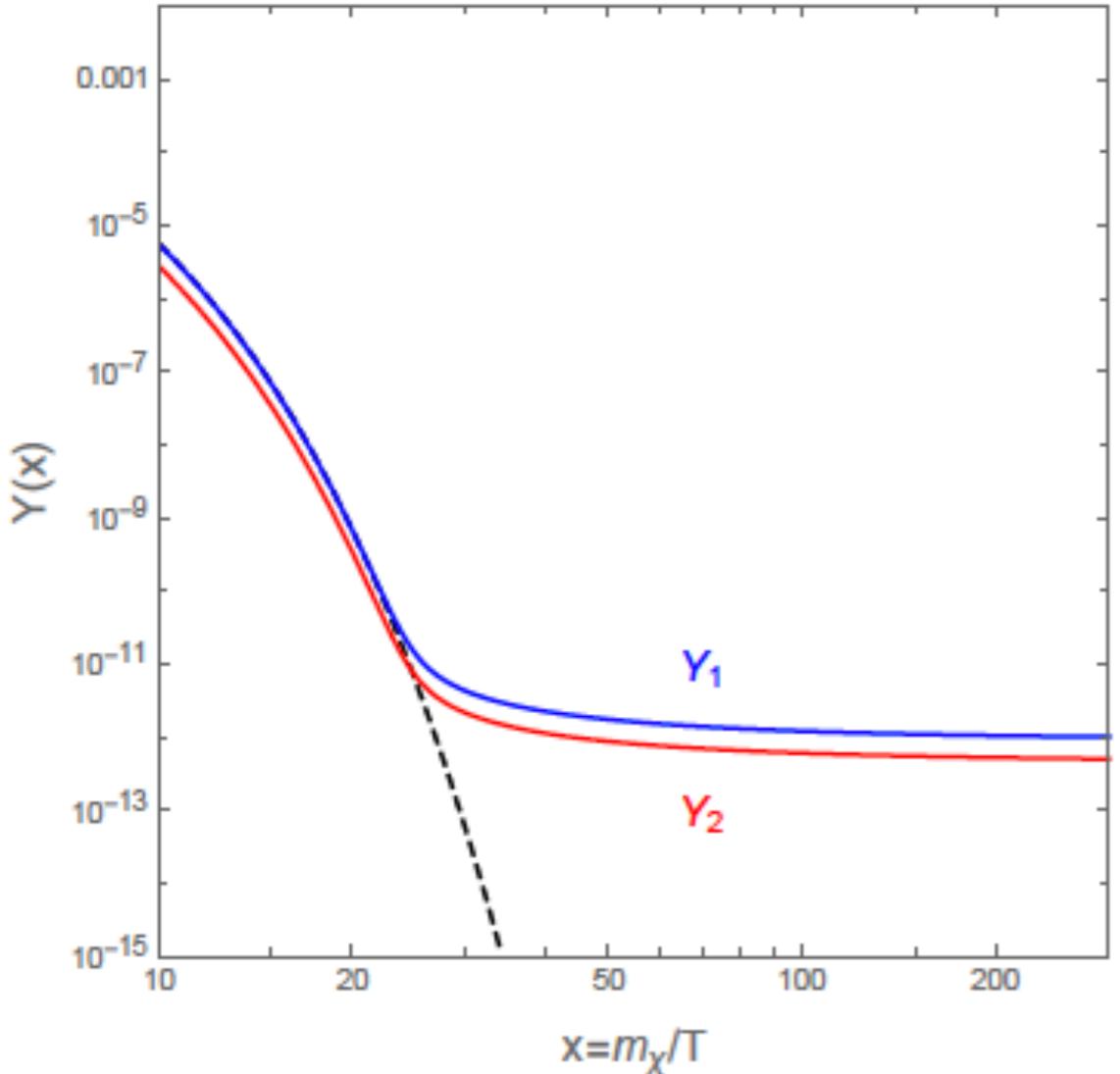
No enhancement

Focus on $2 \rightarrow 2$ annihilation for
WIMP-like DM.

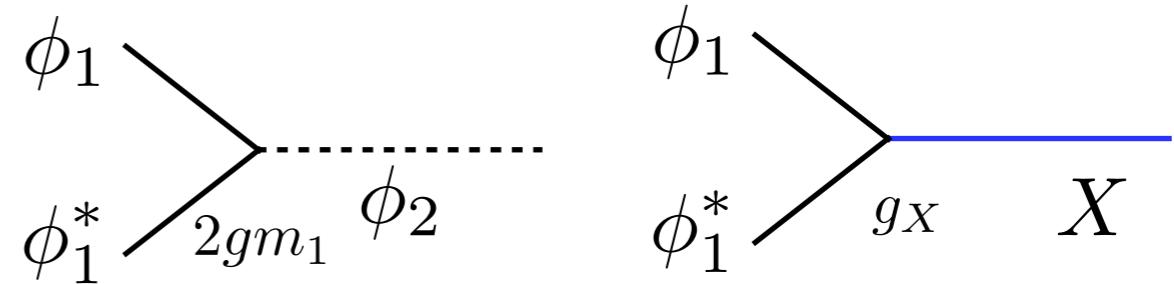
DM relic density

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$m_1 = 200 \text{ GeV} = m_2/2 = 2m_X$, $\alpha = 0.1$, $\alpha_X = 0.009$



Dark photon portal:



Dark photon in thermal equilibrium with SM plasma

$\alpha \gg \alpha_X$: large self-coupling

$$\rightarrow \langle\sigma v\rangle_{\phi_2\phi_2 \rightarrow \phi_1\phi_1^*} \gg \langle\sigma v\rangle_{\phi_1\phi_1^* \rightarrow XX}$$

$$\begin{aligned} \frac{dY_1}{dx} &= \lambda_1 x^{-2} (4Y_2^2 - Y_1^2) - \lambda_2 x^{-2} (Y_1^2 - (Y_1^{\text{eq}})^2) \\ &\quad - \rho_1 x^{-5} Y_1 \left(Y_1^2 - \frac{(Y_1^{\text{eq}})^2}{Y_2^{\text{eq}}} Y_2 \right) - \rho_2 x^{-5} Y_1 (Y_1^2 - (Y_1^{\text{eq}})^2), \end{aligned}$$

$$\begin{aligned} \frac{dY_2}{dx} &= -\lambda_1 x^{-2} (4Y_2^2 - Y_1^2) - \lambda_3 x^{-2} Y_1 (Y_2 - Y_2^{\text{eq}}) \\ &\quad + \frac{1}{4} \rho_1 x^{-5} Y_1 \left(Y_1^2 - \frac{(Y_1^{\text{eq}})^2}{Y_2^{\text{eq}}} Y_2 \right) \end{aligned}$$

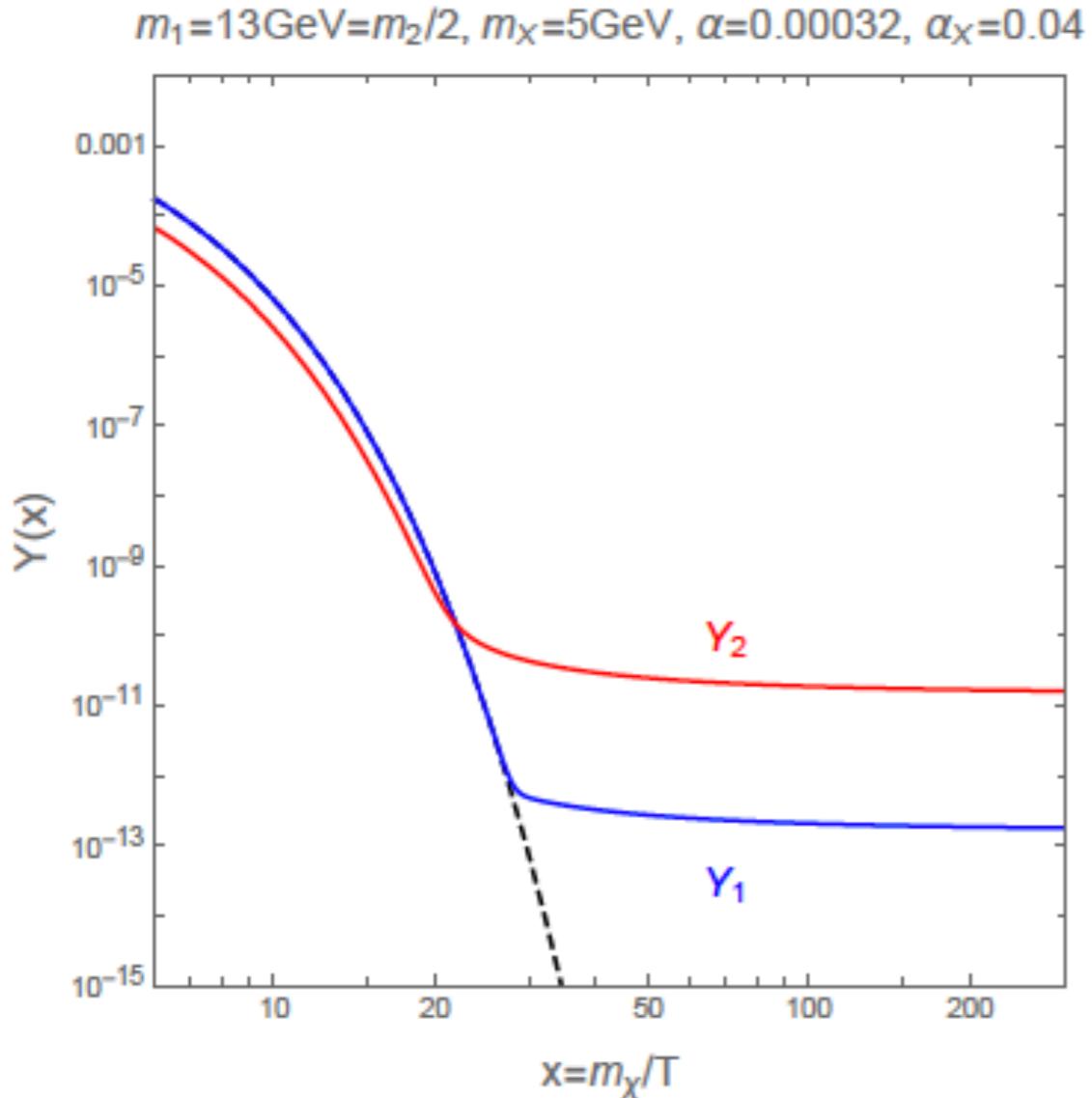
$Y_1 \simeq 2Y_2$: equal abundances

$m_2 \simeq 2m_1$: strong u-channel resonance

[S. Kim, HML, B. Zhu, 2022]

DM relic density

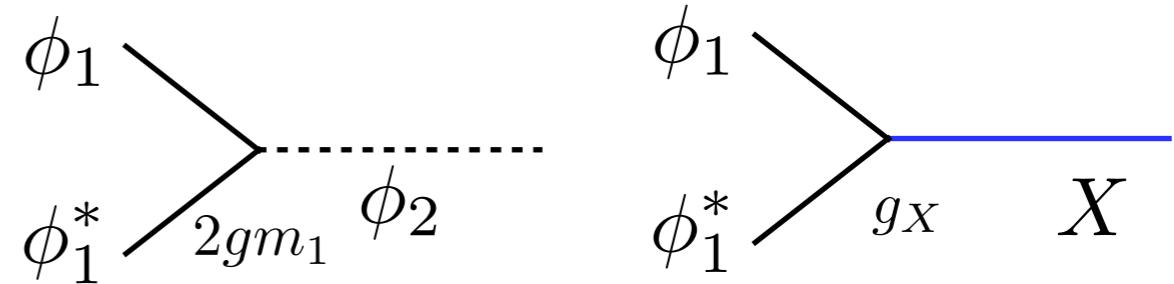
-23-



$$\begin{aligned} \frac{dY_1}{dx} &= \lambda_1 x^{-2} (4Y_2^2 - Y_1^2) - \lambda_2 x^{-2} (Y_1^2 - (Y_1^{\text{eq}})^2) \\ &\quad - \rho_1 x^{-5} Y_1 \left(Y_1^2 - \frac{(Y_1^{\text{eq}})^2}{Y_2^{\text{eq}}} Y_2 \right) - \rho_2 x^{-5} Y_1 (Y_1^2 - (Y_1^{\text{eq}})^2), \end{aligned}$$

$$\begin{aligned} \frac{dY_2}{dx} &= -\lambda_1 x^{-2} (4Y_2^2 - Y_1^2) - \lambda_3 x^{-2} Y_1 (Y_2 - Y_2^{\text{eq}}) \\ &\quad + \frac{1}{4} \rho_1 x^{-5} Y_1 \left(Y_1^2 - \frac{(Y_1^{\text{eq}})^2}{Y_2^{\text{eq}}} Y_2 \right) \end{aligned}$$

Dark photon portal:



Dark photon in thermal equilibrium with SM plasma

$\alpha \ll \alpha_X$: small self-coupling

→ $\langle \sigma v \rangle_{\phi_2 \phi_2 \rightarrow \phi_1 \phi_1^*} \ll \langle \sigma v \rangle_{\phi_1 \phi_1^* \rightarrow XX}$

$Y_1 \ll Y_2$: hierarchical abundances

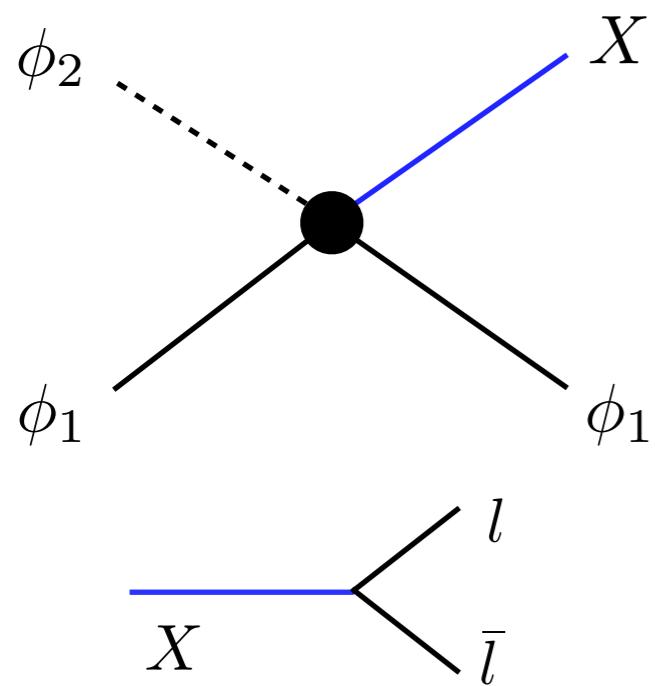
$m_2 \simeq 2m_1$: mild u-channel resonance

[S. Kim, HML, B. Zhu, 2022]

Indirect detection

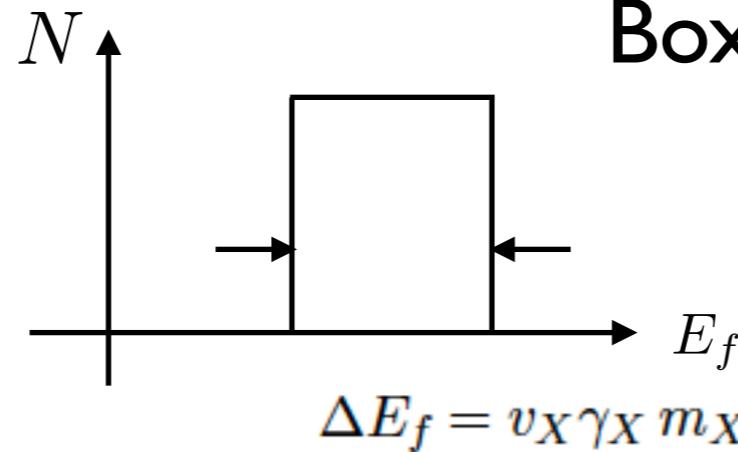
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Cosmic ray from semi-annihilation:



Leptons boosted in galactic center frame

$$E_f = \frac{1}{\gamma_X} \bar{E}_f (1 - v_X \cos \theta)^{-1}, \quad \bar{E}_f = \frac{m_X}{2}$$

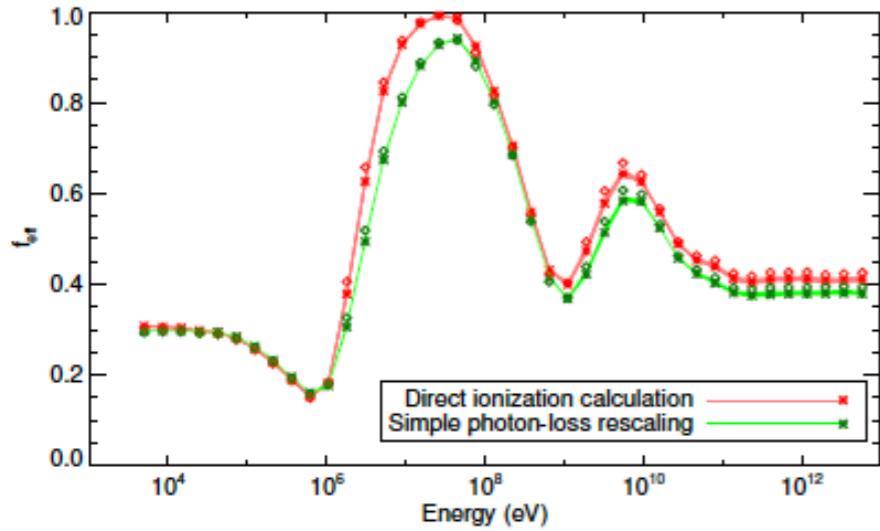


Box-shaped positron energy
Fermi-LAT & AMD-02

cf. gamma-ray from
Fermi-LAT, HESS, etc.

CMB recombination & semi-annihilation:

[S. Kim, HML, B. Zhu, 2022]



Leptons injects energy to CMB photons

$$\langle \sigma v \rangle_{\phi_1 \phi_2 \rightarrow \phi_1 X} < 4 \times 10^{-25} \text{ cm}^3/\text{s} \left(\frac{f_{\text{eff}}}{0.1} \right)^{-1} \cdot \frac{1}{r_1(1-r_1)} \cdot \left(\frac{m_2}{100 \text{ GeV}} \right)$$

Efficient factor: $f_{\text{eff}}(m_2) = \frac{\int_0^{m_2/2} dE_e E_e 2f_{\text{eff}}^{e^+e^-} \frac{dN_e}{dE_e}}{m_2}, \quad r_1 = \Omega_1/\Omega_{\text{DM}}$

[T. Slatyer, 2015]

Indirect detection

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Benchmark models

[S. Kim, HML, B. Zhu, 2022]

	$m_2 \simeq 2m_1$ [GeV]	m_X [GeV]	$\alpha = \frac{g^2}{4\pi}$	$\alpha_X = \frac{g_X^2}{4\pi}$	$\langle \sigma v \rangle_{\phi_1 \phi_2 \rightarrow \phi_1 X}^0$ [cm ³ /s]	$r_1 = \frac{\Omega_1}{\Omega_{\text{DM}}}$	S_0	$\Delta = 1 - \frac{m_2}{2m_1}$	$\sigma_{\text{self}}/m_{\text{eff}}$ [cm ² /g]
B1	200	50	0.05	0.0045	9.9×10^{-27}	0.5	444.7	7.75×10^{-4}	0.014
B2	400	100	0.1	0.009	9.9×10^{-27}	0.5	889	10^{-4}	0.002
B3	26	5	0.00032	0.04	2.0×10^{-26}	0.005	1336	5×10^{-10}	0.003
B4	240	60	0.0032	0.03	2.9×10^{-27}	0.075	7379	$10^{-7.7}$	0.086

Consistency with CMB bound (& other indirect bounds)

→ Either sizable mass splitting or small self-coupling.

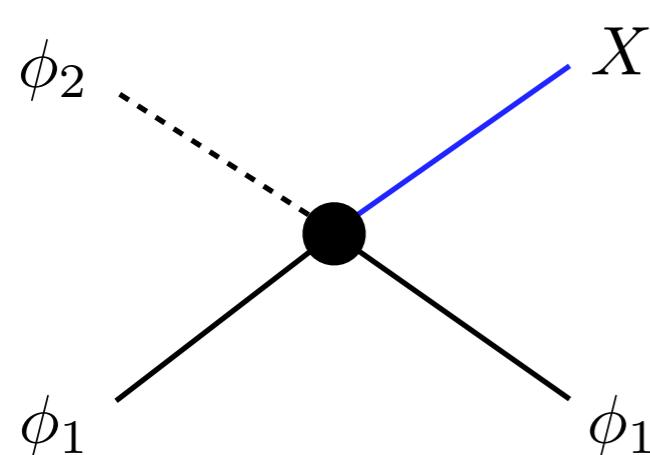
Large u-channel resonances

→ B4 marginally solves the small-scale problems.

Direct detection

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Boosted DM from semi-annihilation: [S. Kim, HML, B. Zhu, 2022]

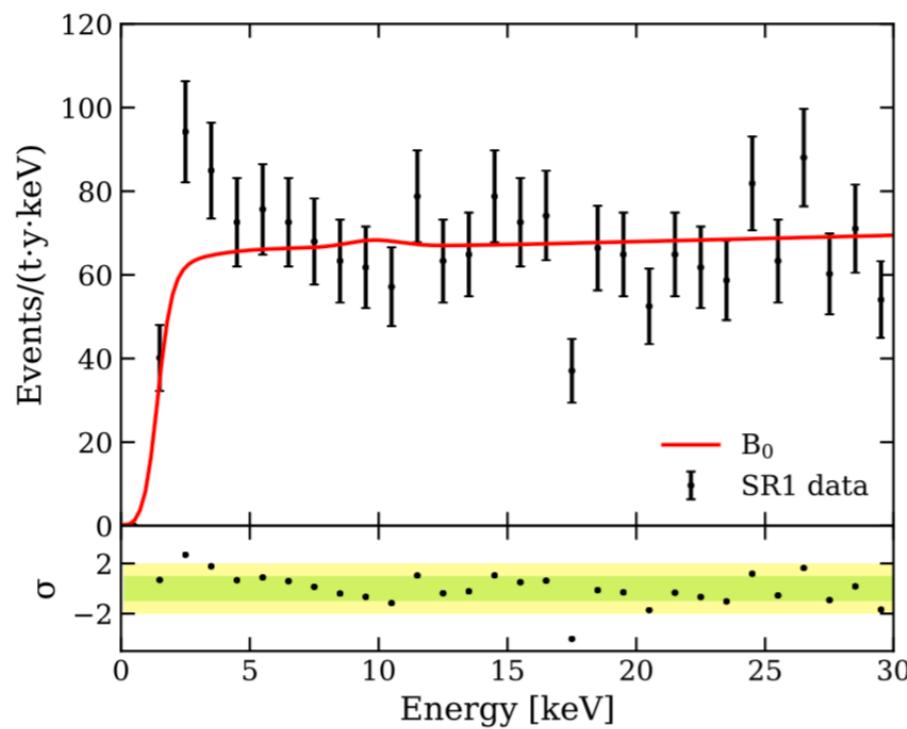


Light DM boosted from semi-annihilation

$$m_2 \simeq 2m_1 \longrightarrow \gamma_1 = (10m_1^2 - m_X^2)/(6m_1^2)$$

Flux for boosted DM (galactic center, NFW)

$$\Phi_1^{\text{G.C.}} = 1.6 \times 10^{-4} \text{cm}^{-2}\text{s}^{-1} \left(\frac{\langle \sigma v \rangle_{\phi_1\phi_2 \rightarrow \phi_1 X}}{5 \times 10^{-26} \text{cm}^3/\text{s}} \right) \left(\frac{(1 \text{GeV})^2}{m_1 m_2} \right) r_1 (1 - r_1)$$



XENON1T excess

Detection by DM-electron scattering:

$$\sigma_e = 10^{-33} \text{cm}^2 \left(\frac{10^{-1} \text{cm}^{-2}\text{s}^{-1}}{\Phi_1^{\text{G.C.}}} \right) \left(\frac{N_{\text{sig}}}{10} \right)$$

$$E_e = 2m_e v_1^2 = 3.6 \text{ keV}, \quad m_1 = 2m_2 \sim 1 \text{ GeV} \text{ and } r_1 \simeq \frac{1}{2}$$

$$\longrightarrow m_X = 1.99729 m_1$$

Sommerfeld factor: $S_0 \sim 10^4$

In tension with indirect bounds.

EFT for SRDM

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u-channel amplitudes for general self-resonant dark matter:

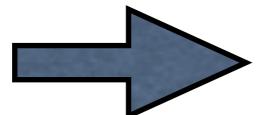
dark matter	scalar	pseudo-scalar	fermion	vector	axial-vector
scalar(ϕ)	$+4g^2 m_\phi^2$	$+4g^2 m_\phi^2$	$\pm 2y_\chi^2 m_\chi (2m_\chi - m_\phi)$	NA	NA
N	—	—	$\mp 2\lambda_\chi^2 m_\chi m_a$	NA	NA
	—	—	NA	$\mp 2g_{Z'}^2 m_\chi m_{Z'}$	$\pm 2g_{A'}^2 m_\chi (2m_\chi - m_{A'})$
	NA	NA	—	$-6g_X^2 m_X (2m_X - m_{X_3})$	NA
	NA	NA	—	—	NA

\pm : fermion or anti-fermion

$$\tilde{\Gamma}_u(p, q; p', q') = \frac{N}{\left(\sqrt{\frac{m_1}{m_2}} \vec{p} - \sqrt{\frac{m_2}{m_1}} \vec{q}\right)^2 + m_2(2m_1 - m_2)}$$

[S. Kim, HML, B. Zhu, 2022]

Scalar-(pseudo)scalar DM, fermion-pseudoscalar(vector) DM



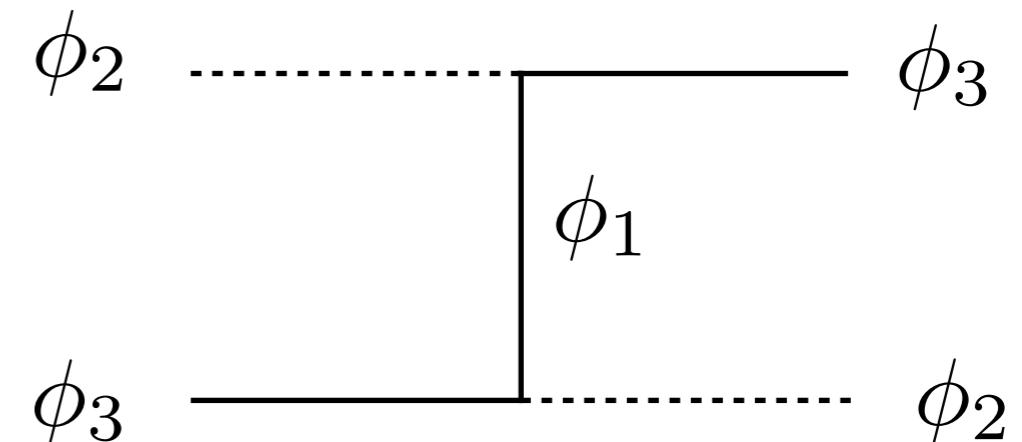
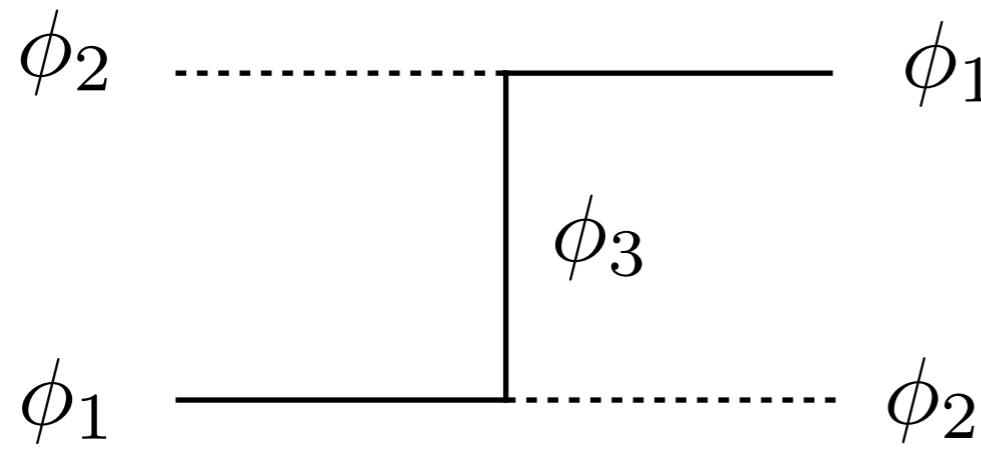
co-scattering enhanced by u-channel resonances

Triple SRDM

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- Take three component dark matter with masses, m_i ($i=1,2,3$).

$$\mathcal{L}_{\text{int}} = -2g m_1 \phi_1 \phi_2 \phi_3^* + \text{h.c.}$$



u-channel resonance masses:

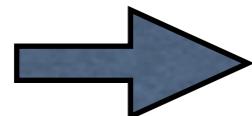
[S. Kim, HML, B. Zhu, 2022]

$$M = \sqrt{\frac{m_2}{m_1}} \sqrt{m_3^2 - (m_1 - m_2)^2}$$

$$M = 0 : m_3 = |m_1 - m_2|$$

$$M = \sqrt{\frac{m_2}{m_3}} \sqrt{m_1^2 - (m_3 - m_2)^2}$$

$$M = 0 : m_1 = |\textcolor{brown}{m}_3 - m_2|$$



u-channel resonance conditions are generalized.

Conclusions

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- Non-perturbative effects are important for precise calculations for dark matter self-scattering and annihilation.
- Dark matter co-scattering undergoes a delayed interaction due to u-channel resonance, being enhanced without a light mediator.
- Non-perturbative scattering amplitude for two-component dark matter is obtained a la Bethe-Salpeter.
- Multi-component dark matter models with u-channel resonances are identified; interesting signatures for DM co-scattering, indirect and direct detection.