



# An optimistic view on inflaton hunt

Mar. 7 2019@Tohoku University

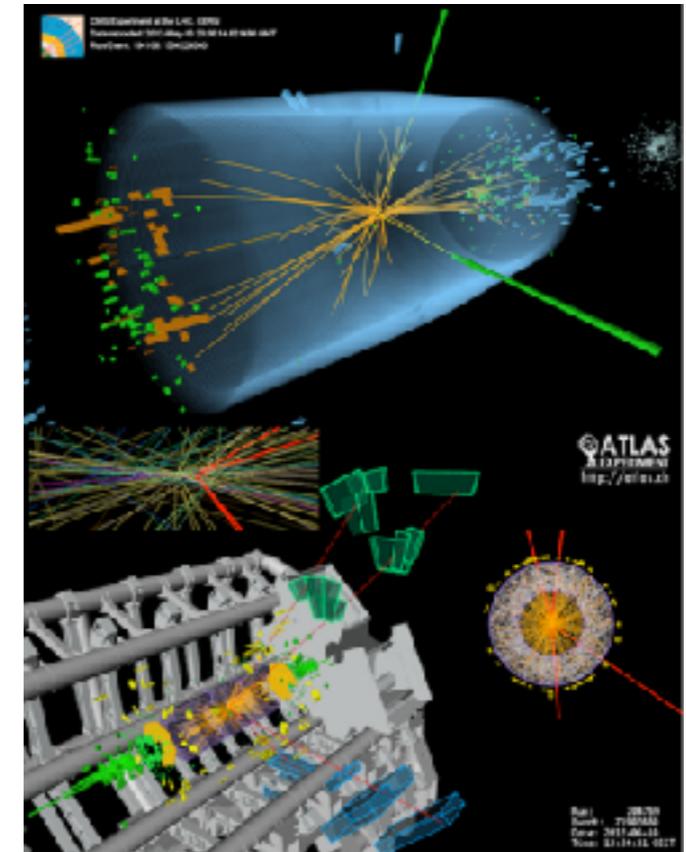
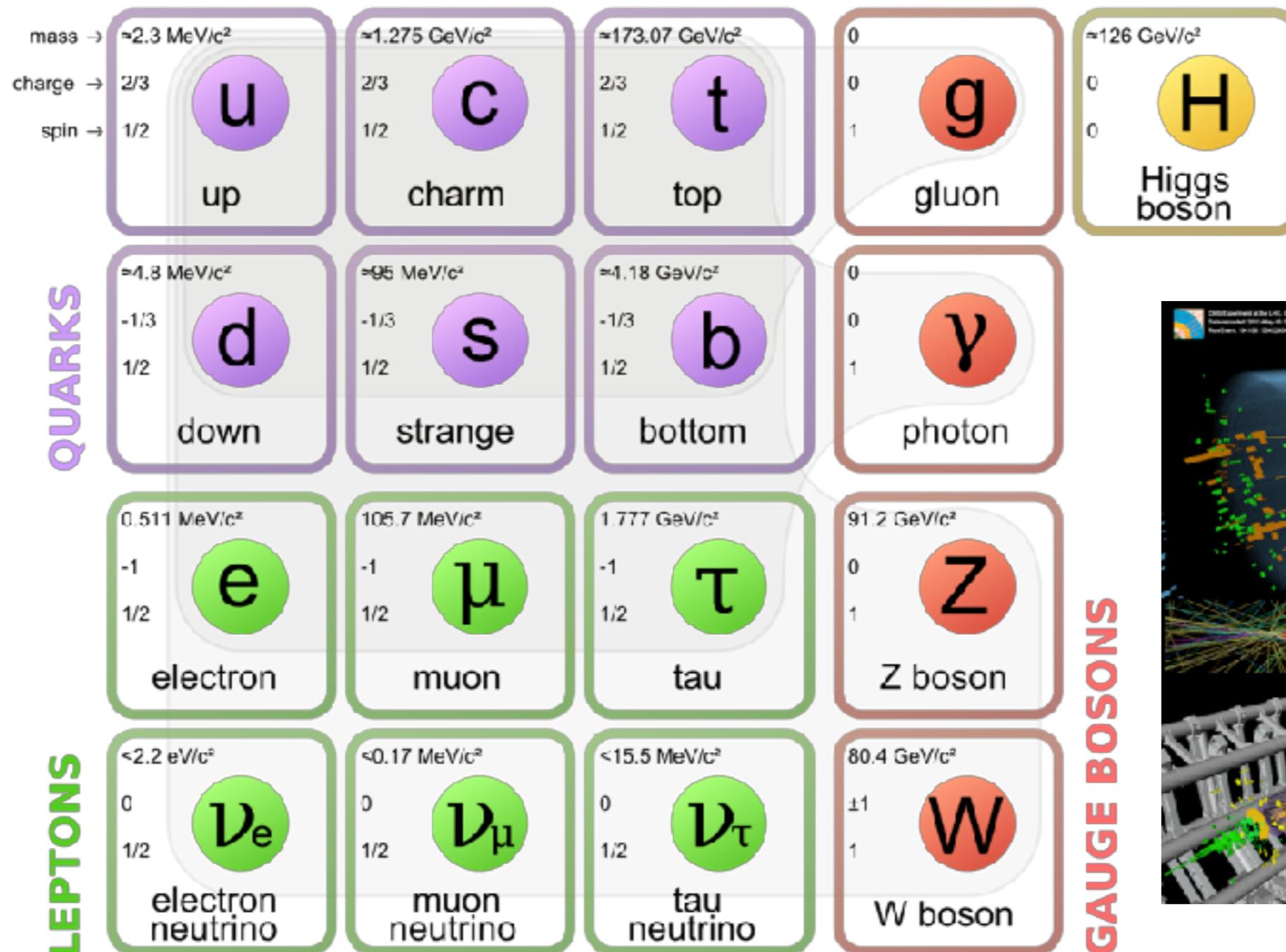
“Revealing the history of the universe with underground particle and nuclear research 2019” (March 7-9).

Fumi Takahashi  
(Tohoku)

Based on Daido, FT, Yin, 1702.03284, 1710.11107, FT and Yin, 1903.00462

# 1. Introduction

The standard model (SM) of particle physics has been tested by numerous experiments with great accuracy.



Is this the end of the story?



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*The End* ?

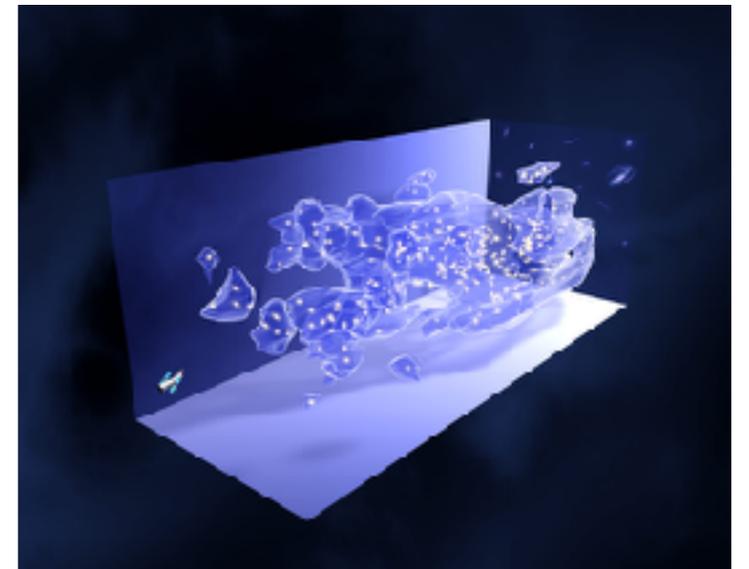
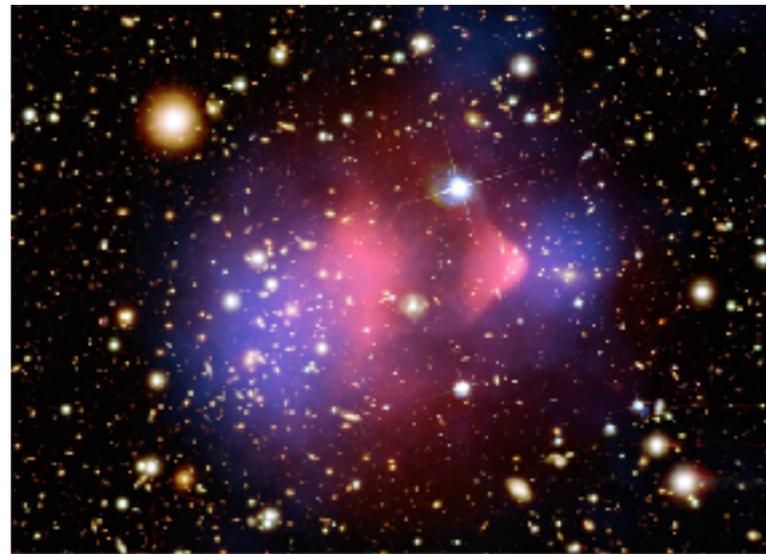
**No!**

# Known unknowns in Cosmology

Success of the  $\Lambda$ CDM model relies on the two unknown degrees of freedom:

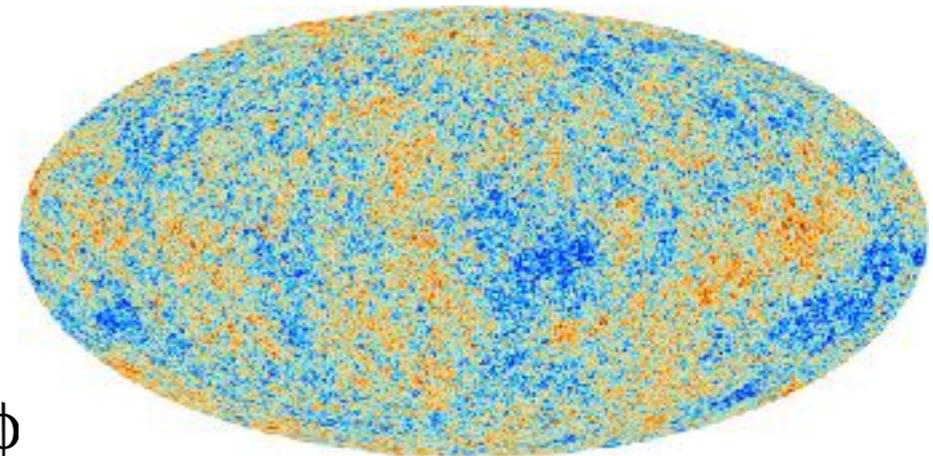
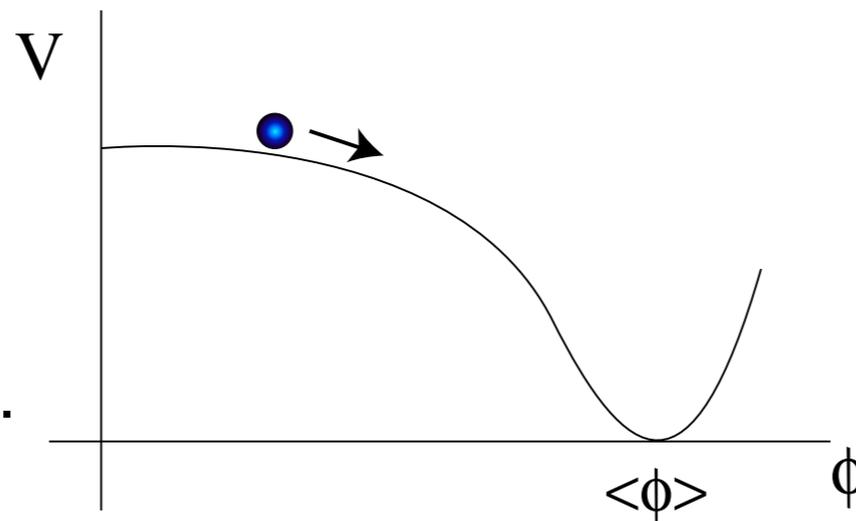
- Dark matter

Cold, neutral,  
and long-lived.



- Inflaton

Very flat potential  
for slow-roll inflation.



**Direct evidence for the physics beyond the SM!**

Then, where should we look for ?





Niels Bohr

**“We are all agreed that your theory is crazy. The question that divides us is **whether it is crazy enough to have a chance of being correct.**”**

(Said to Pauli after his presentation.)



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Steven Weinberg

**“...My advice is to **try crazy ideas and innovative experiments.** Something will come up.”**

(In answer to “Do you have any advice to offer the next generation?”)



F. K. Richtmyer

**“The whole history of physics proves that a new discovery is quite likely lurking at the next decimal place.”**



So, let us try a crazy idea, which might be lurking at the next decimal place.

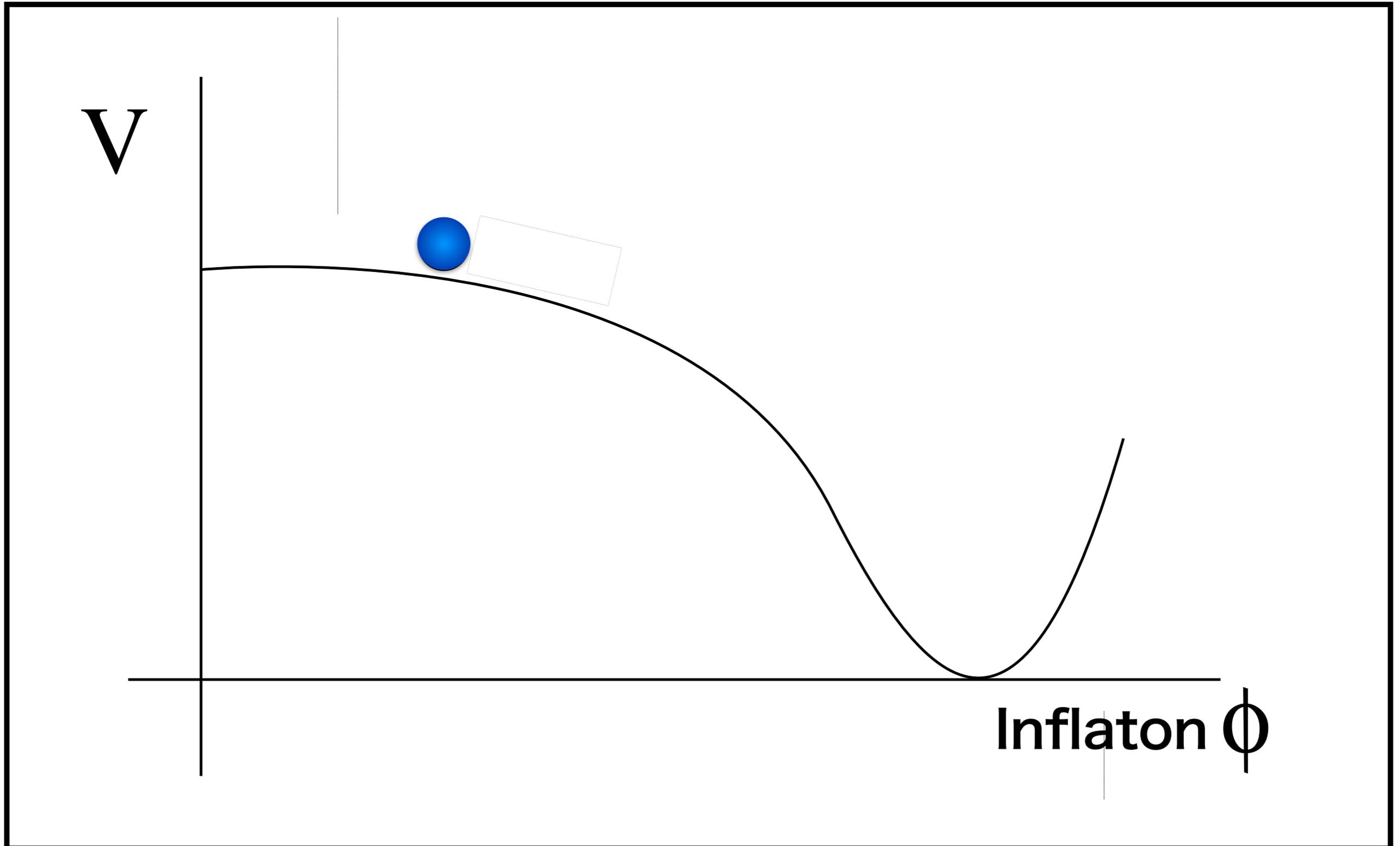
So, let us try a crazy idea, which might be lurking at the next decimal place.

**I want the inflaton (+DM)  
that can be probed by  
ground-based experiments.**

**2. What is the inflaton?**

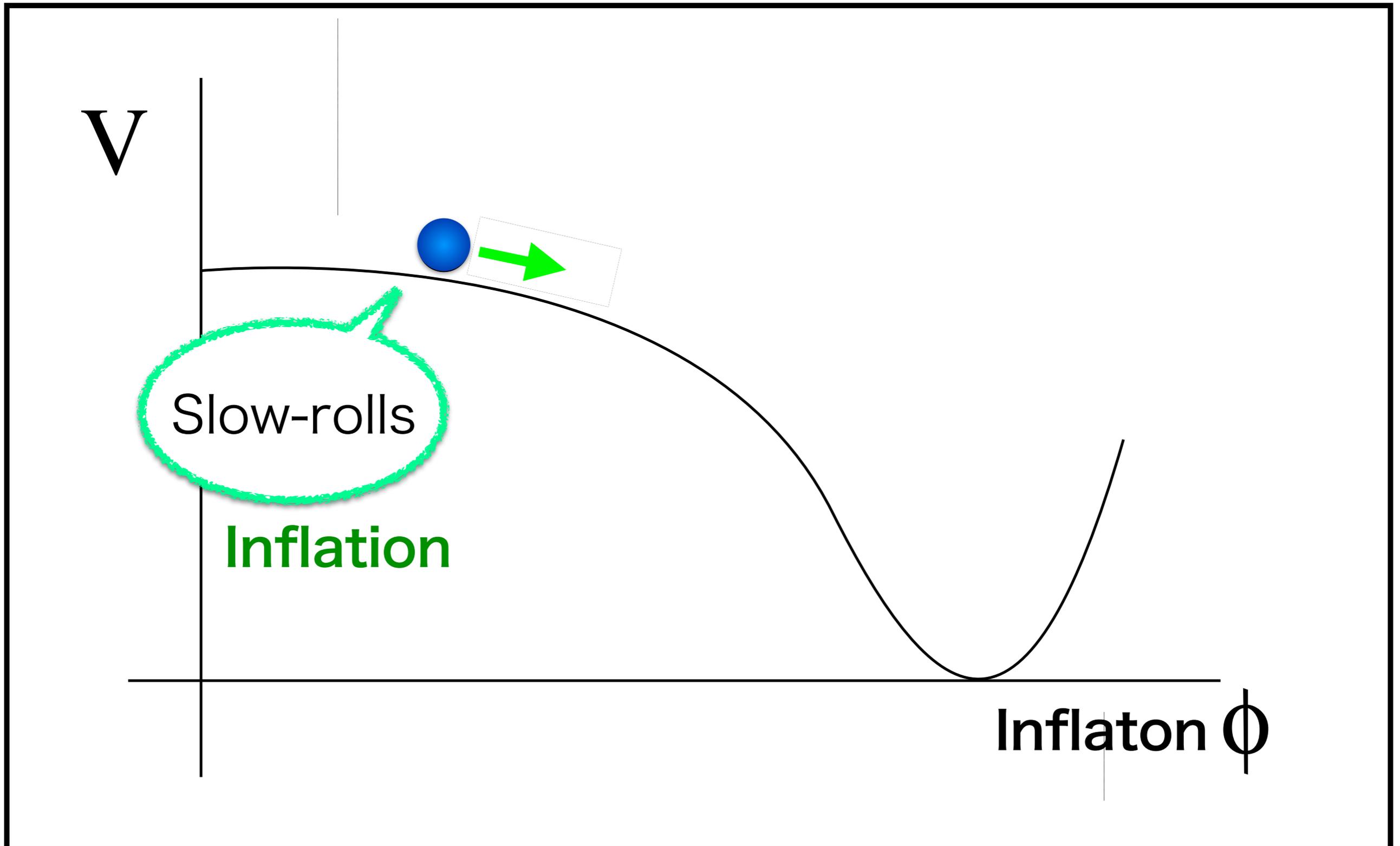
# Inflation

Guth '81, Sato '80, Starobinsky '80, Kazanas '80, Brout, Englert, Gunzig, '79  
Linde '82, Albrecht and Steinhardt '82



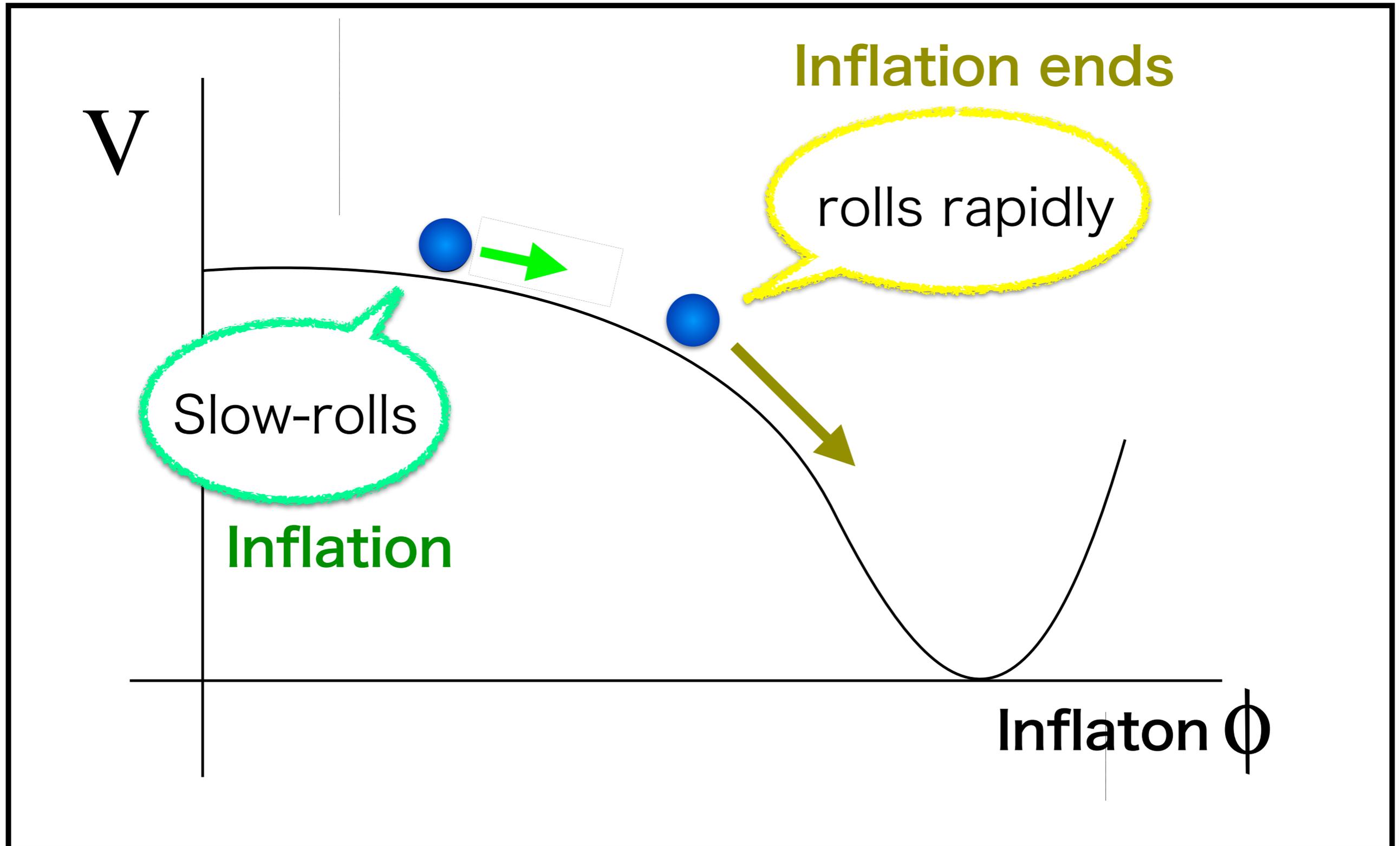
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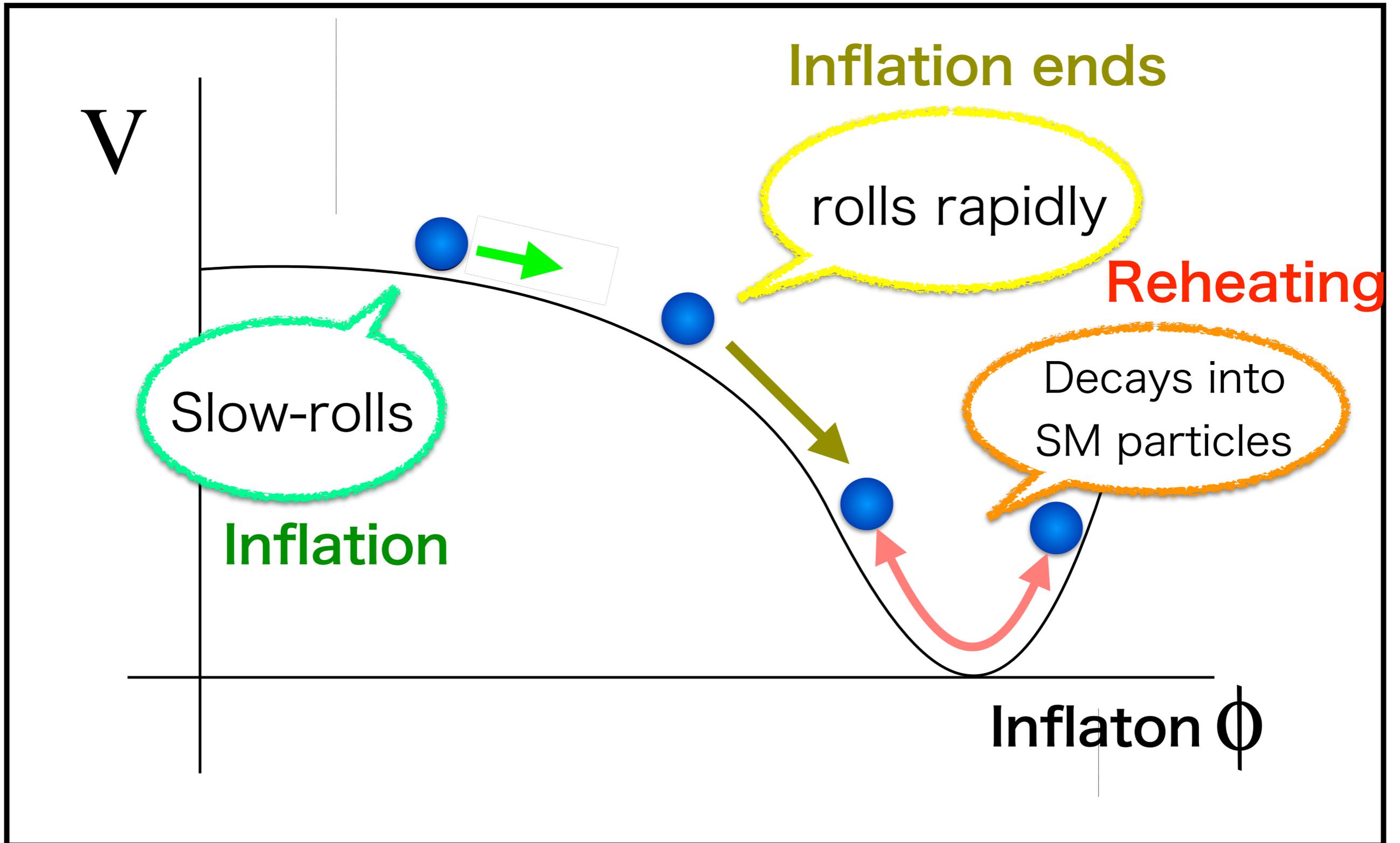
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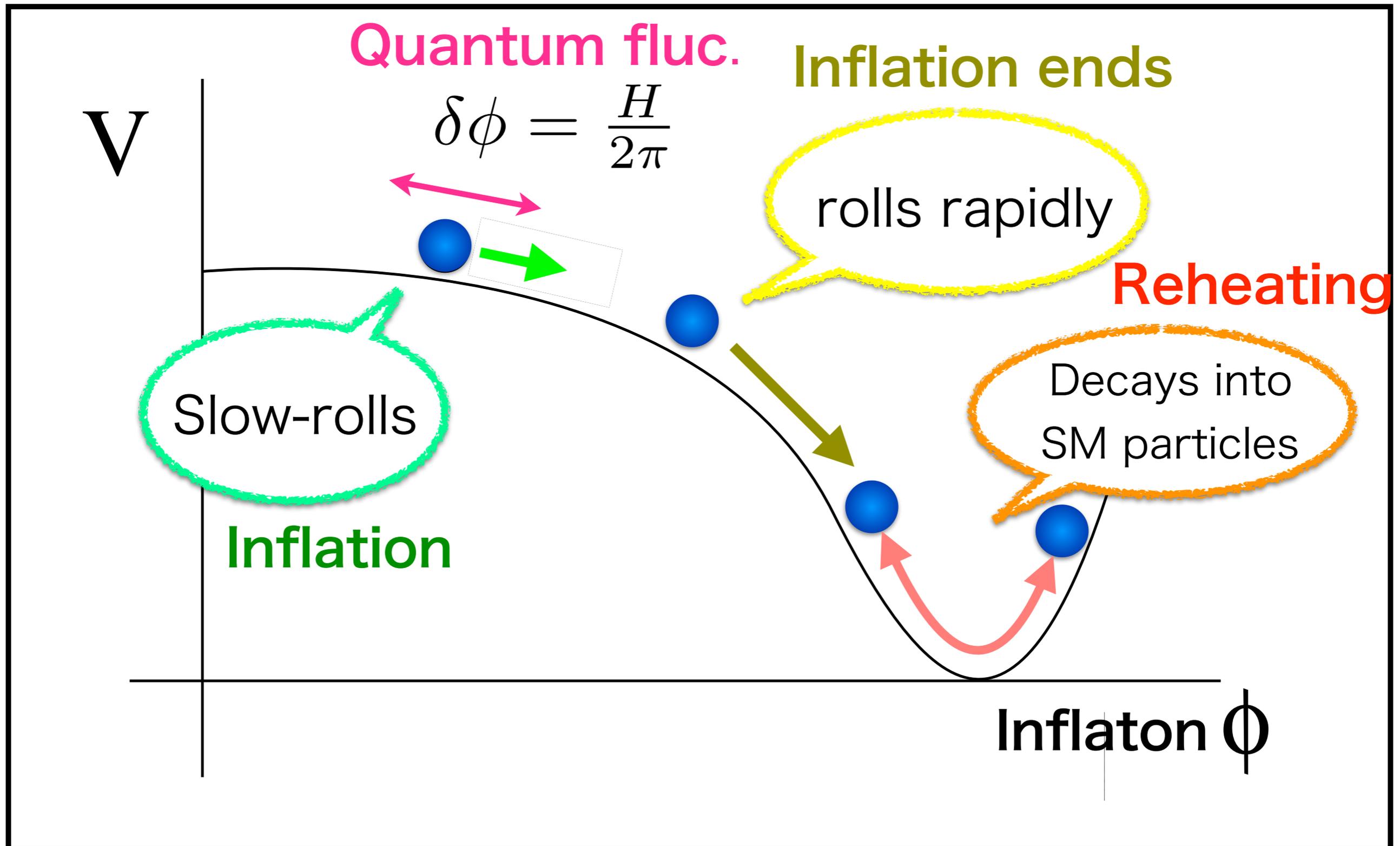
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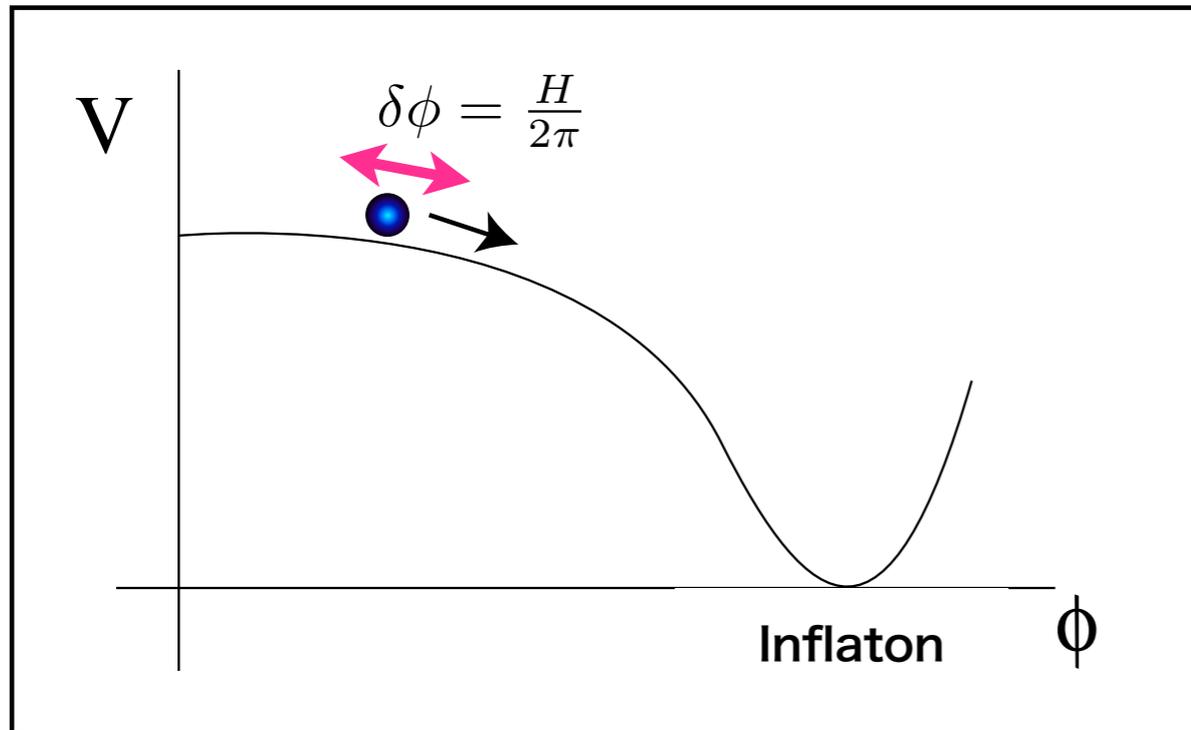


# Inflation

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# Inflation and density perturbations

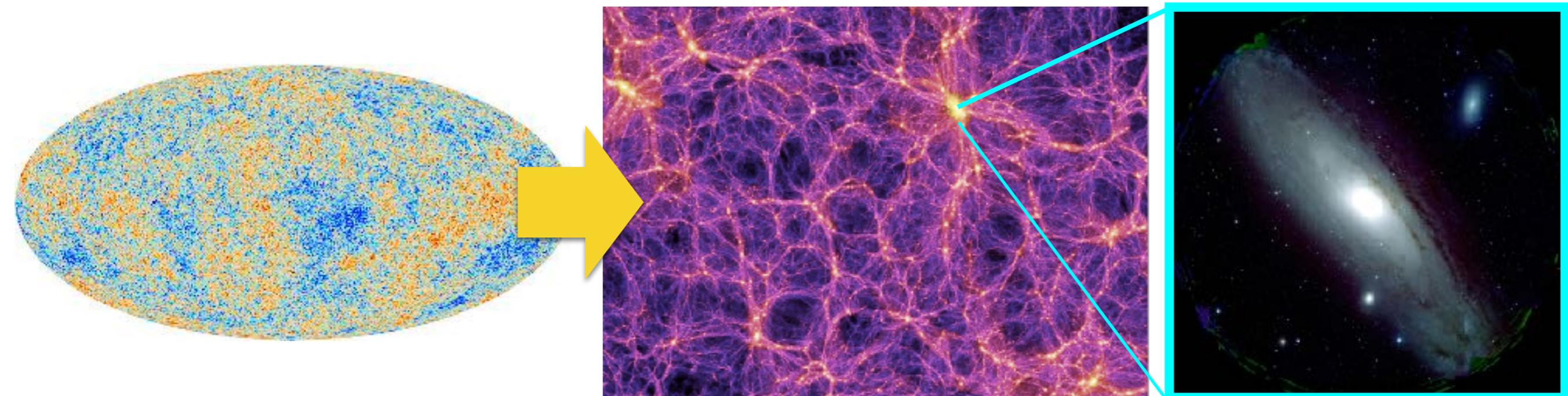


The quantum fluctuations lead to slightly different evolution at different points.

Fluctuation in time

= Fluctuation in volume

= Density perturbations



# Scalar mode perturbations

Amplitude:

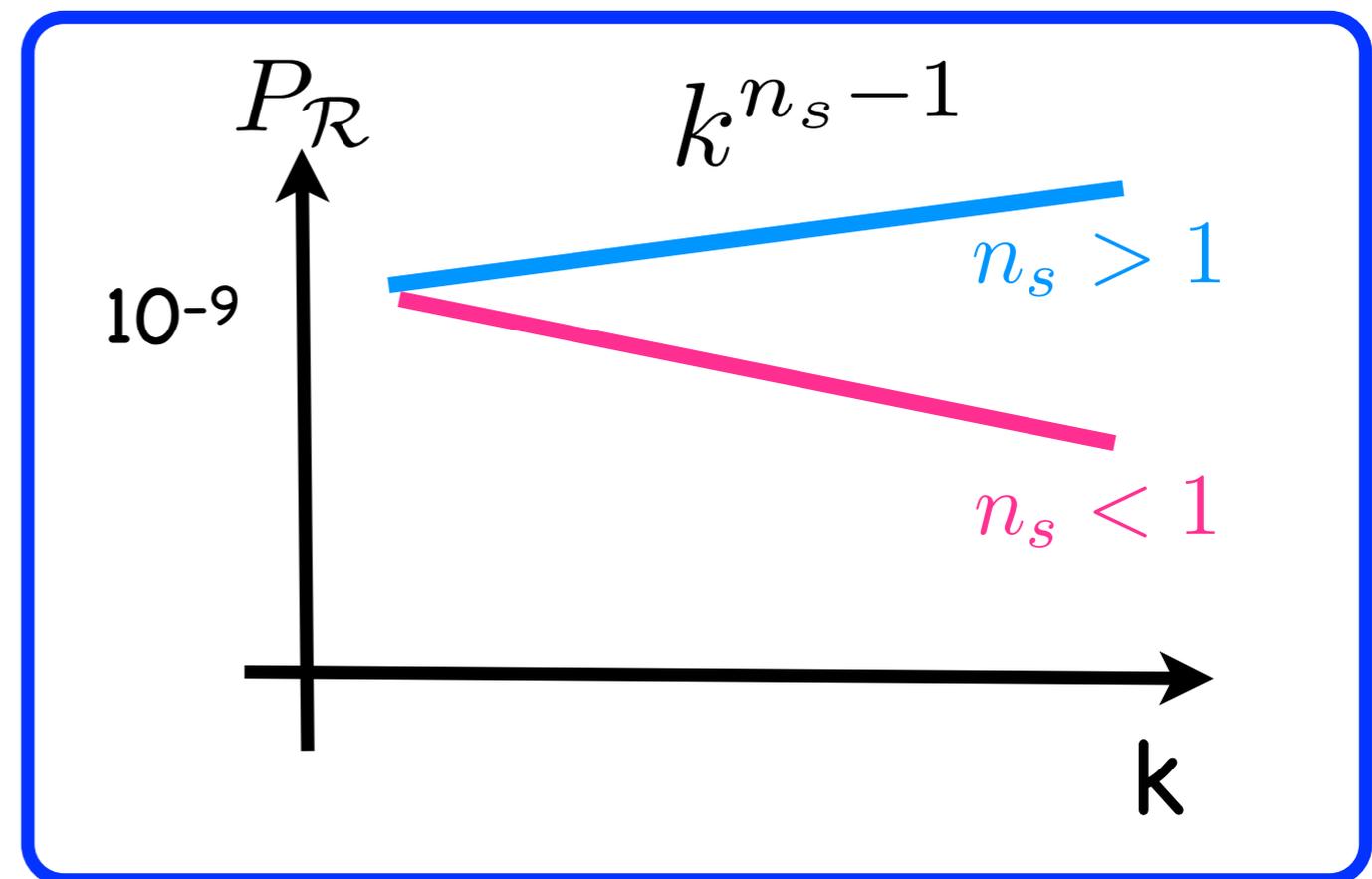
$$\frac{\delta\rho}{\rho} \sim \left| \frac{V^{3/2}}{V' M_P^3} \right| \sim 10^{-5} \quad : \text{CMB normalization}$$

The potential must be flatter for lower inflation scale.

**Spectral index:**  $n_s = 0.965 \pm 0.004$  [Planck 2018](#)

$$\begin{aligned} n_s - 1 &= \frac{d \ln(\delta\rho_k/\rho)^2}{d \ln k} \\ &\simeq -\frac{V'}{V} \frac{d}{d\phi} \ln \left( \frac{V^3}{V'^2} \right) \\ &= -3 \frac{V'^2}{V^2} + 2 \frac{V''}{V} \end{aligned}$$

$n_s$  is determined mainly by  $V''$  for low-scale inflation.



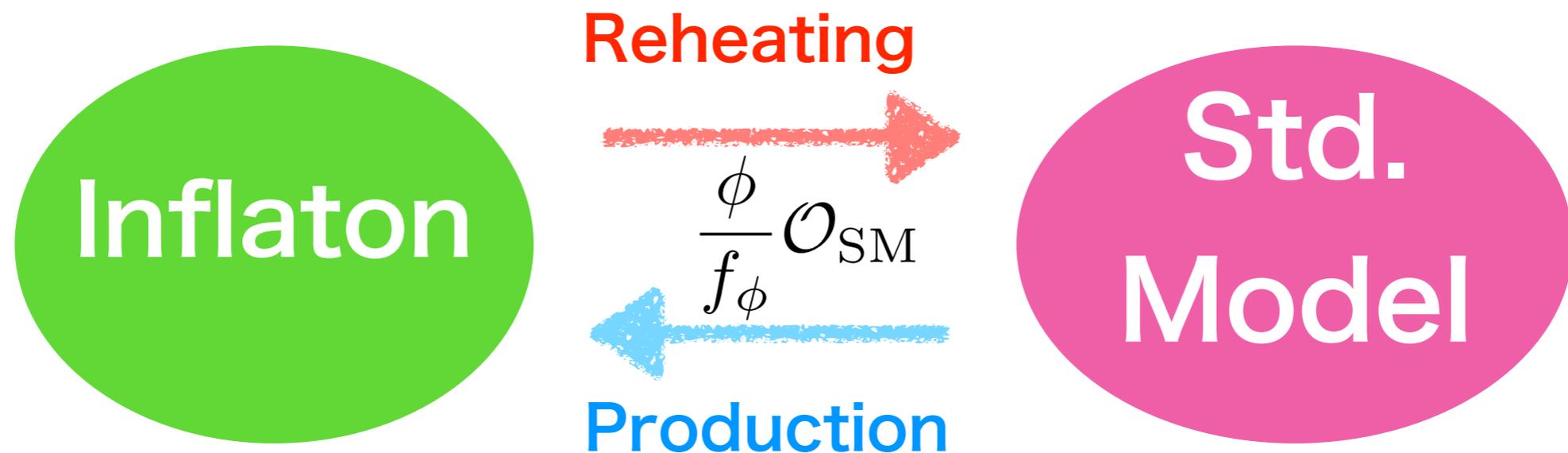
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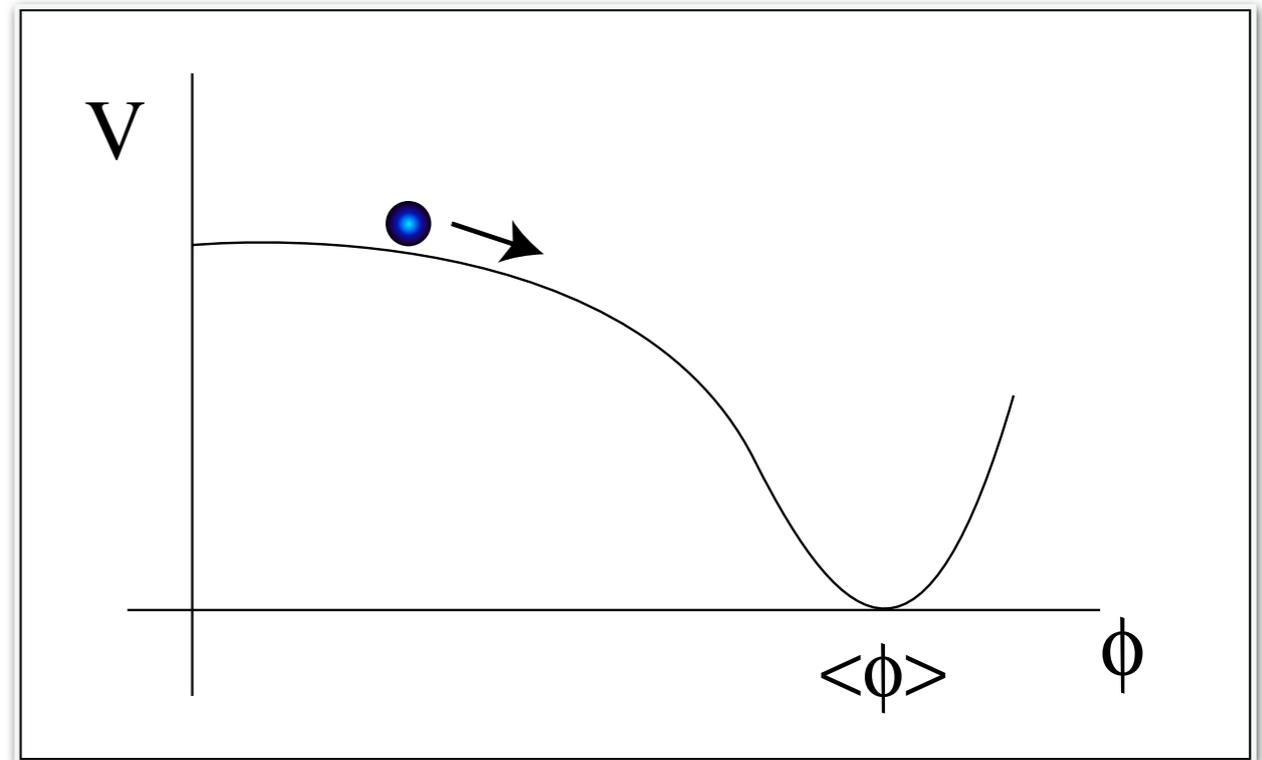


The inflaton may be produced at experiments or astrophysical environment (e.g. inside stars)

Suppose that the inflaton is so light that it is kinematically accessible for experiments.

- 2)** The inflaton potential is extremely flat, in spite of large couplings to the SM.

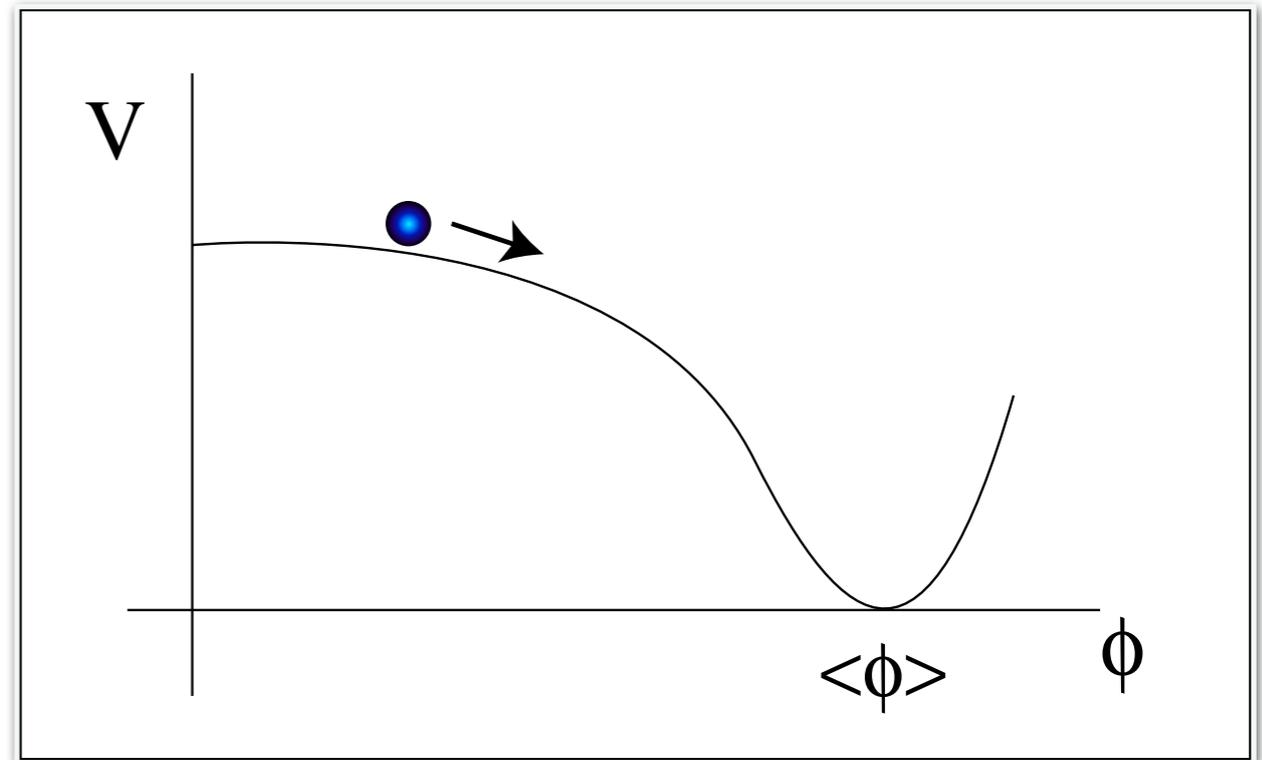
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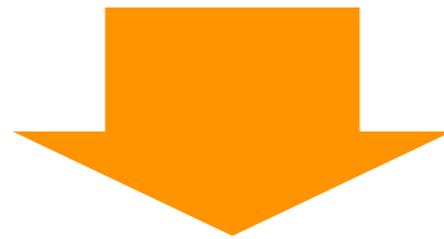
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The flatness of the inflaton potential can be ensured by shift symmetry, if it is an NG boson.

Suppose that the inflaton is so light that it is kinematically accessible for experiments.



The inflaton is likely **an axion/ALP with sizable couplings to the SM.**

**Do we have any testable predictions?**

See talks by Kawasaki, Ringwald, and Tokiyasu for axions.

# Inflaton = ALP

Let us suppose that the inflaton is an ALP which enjoys a (discrete) shift symmetry,

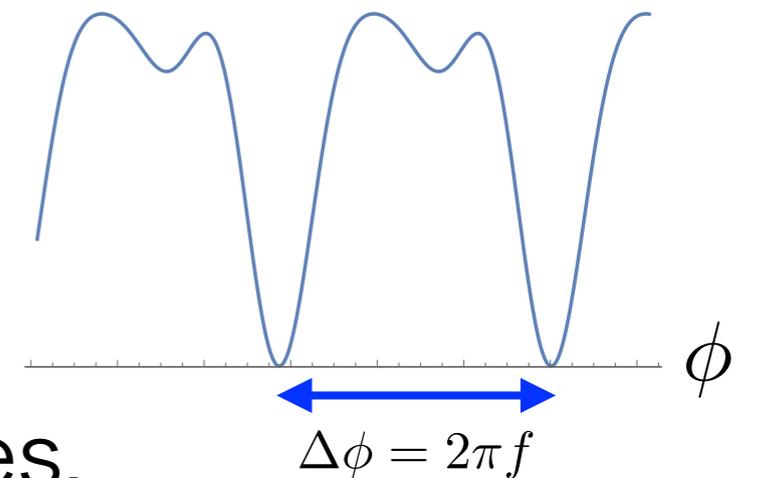
$$\phi \rightarrow \phi + 2\pi n f \quad n \in \mathbf{Z}$$

suppressing dangerous radiative correction. Then, the inflaton potential is periodic, i.e.,

$$V(\phi) = V(\phi + 2\pi f)$$

and can be expressed as Fourier series,

$$V(\phi) = \sum_{n \in \mathbf{Z}} c_n e^{in \frac{\phi}{f}}$$



# • Natural inflation

Freese, Frieman, Olinto '90

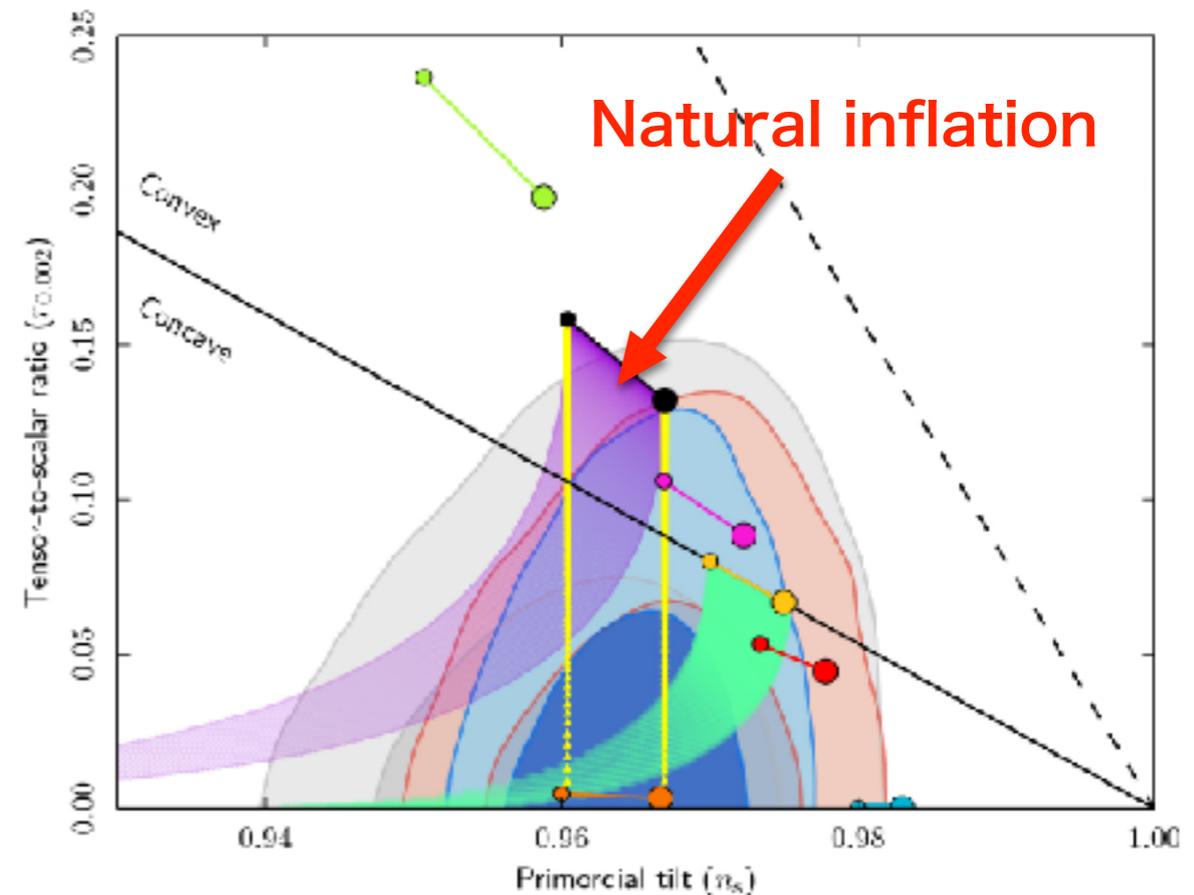
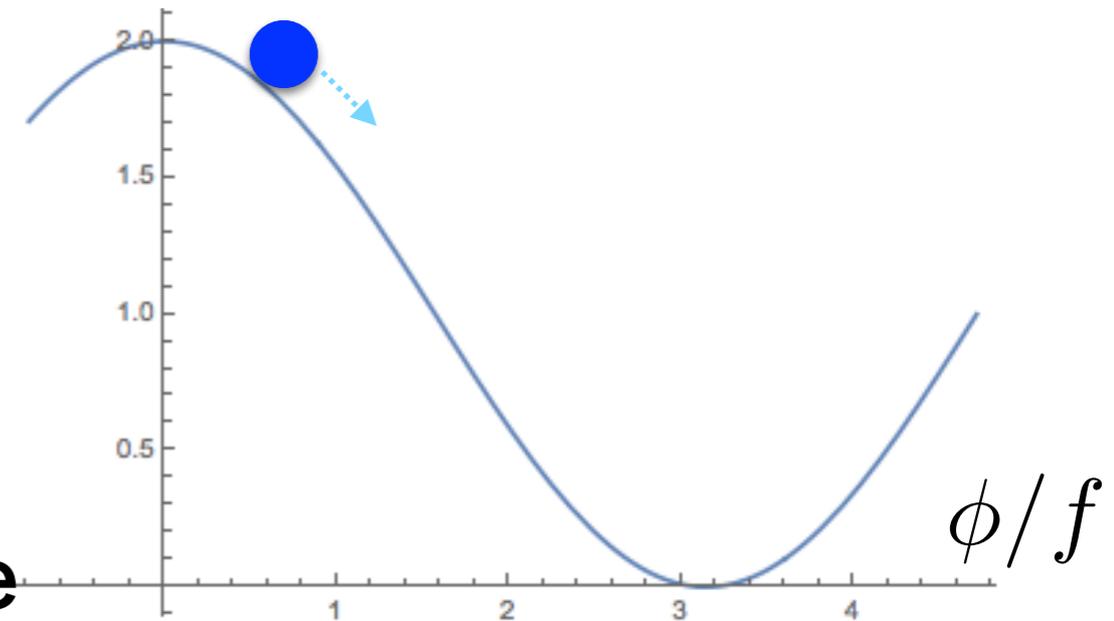
$$V = \Lambda^4 \left( 1 - \cos \left( \frac{\phi}{f} \right) \right)$$

Only large-field inflation is possible with a single cosine term.

- Super-Planckian decay constant required:

$$f \gtrsim 5M_P$$

- Predicted  $(n_s, r)$  are not favored by CMB obs. ☹️



# • Axion hilltop inflation

Low-scale axion inflation can be realized with **at least two cosine terms**: “*Multi-natural inflation*”

$$V_{\text{inf}}(\phi) = \Lambda^4 \left( \cos \left( \frac{\phi}{f} + \theta \right) - \frac{\kappa}{n^2} \cos \left( \frac{n\phi}{f} \right) \right) + \text{const.}$$

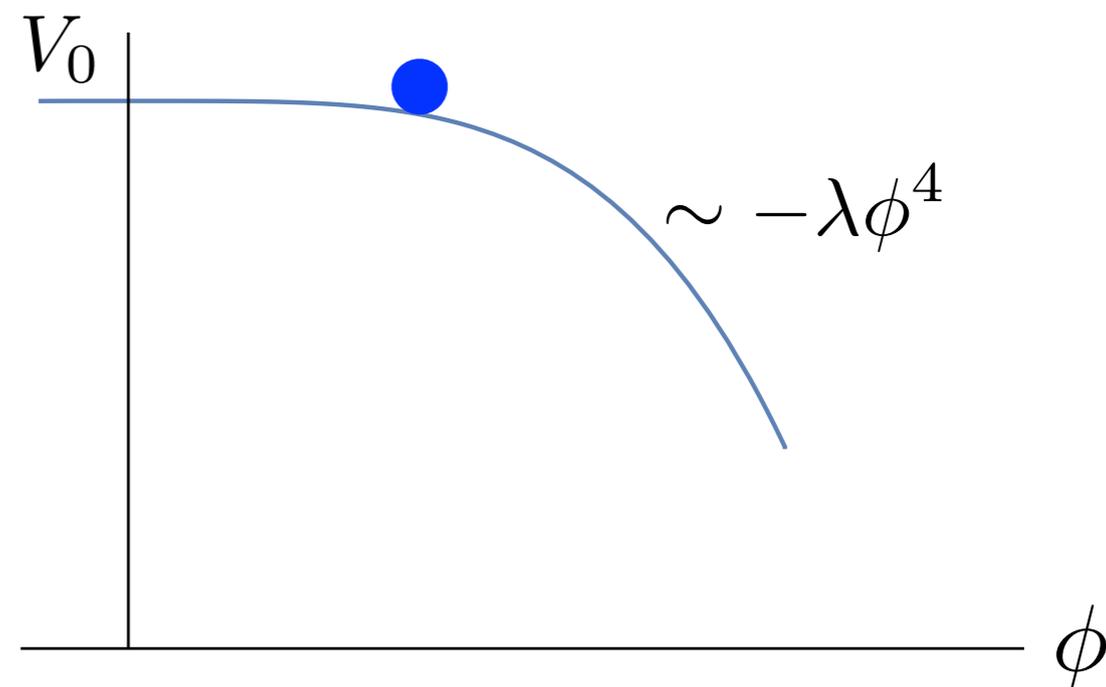
$$= \boxed{V_0 - \lambda\phi^4} - \theta \frac{\Lambda^4}{f} \phi + (\kappa - 1) \frac{\Lambda^4}{2f^2} \phi^2 + \dots \text{ where } \lambda \sim \frac{\Lambda^4}{f^4}$$

for  $|\theta| \ll 1$  and  $|\kappa - 1| \ll 1$

**CMB normalization:**

$$\lambda \sim \left( \frac{\Lambda}{f} \right)^4 \sim 10^{-13}$$

independent of  $V_0$

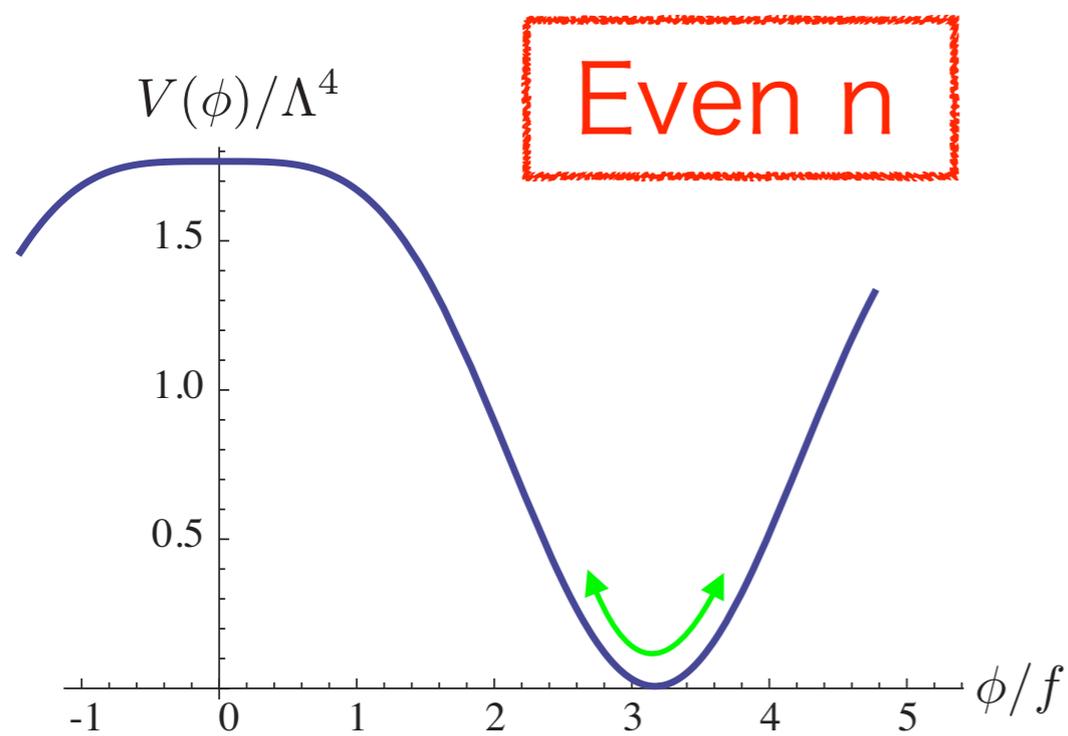


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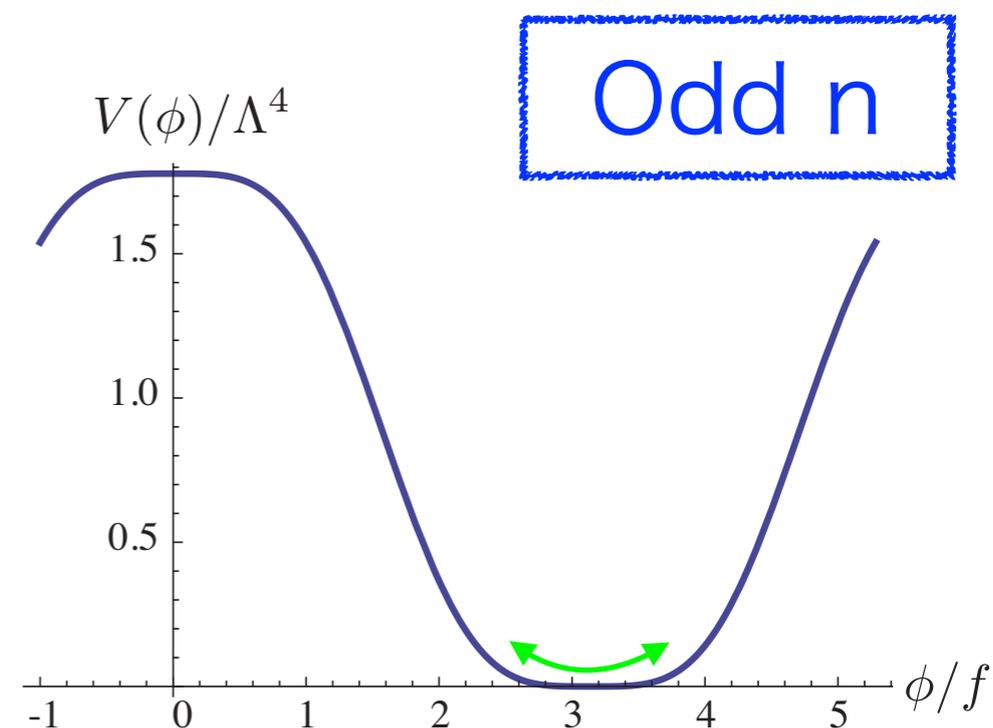
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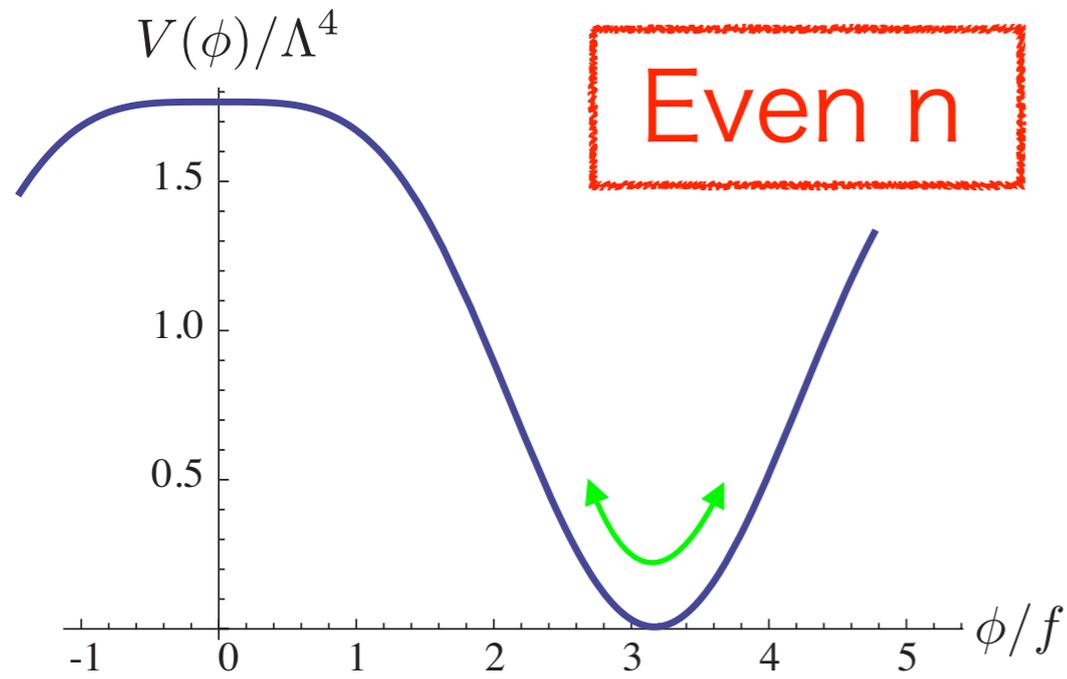
The inflaton mass at the minimum,  $m_\phi$ , depends on  $n$ .



$$m_\phi \sim \Lambda^2 / f$$



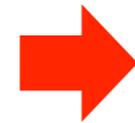
$$m_\phi \ll \Lambda^2 / f$$



The potential is flat only around the potential maximum.

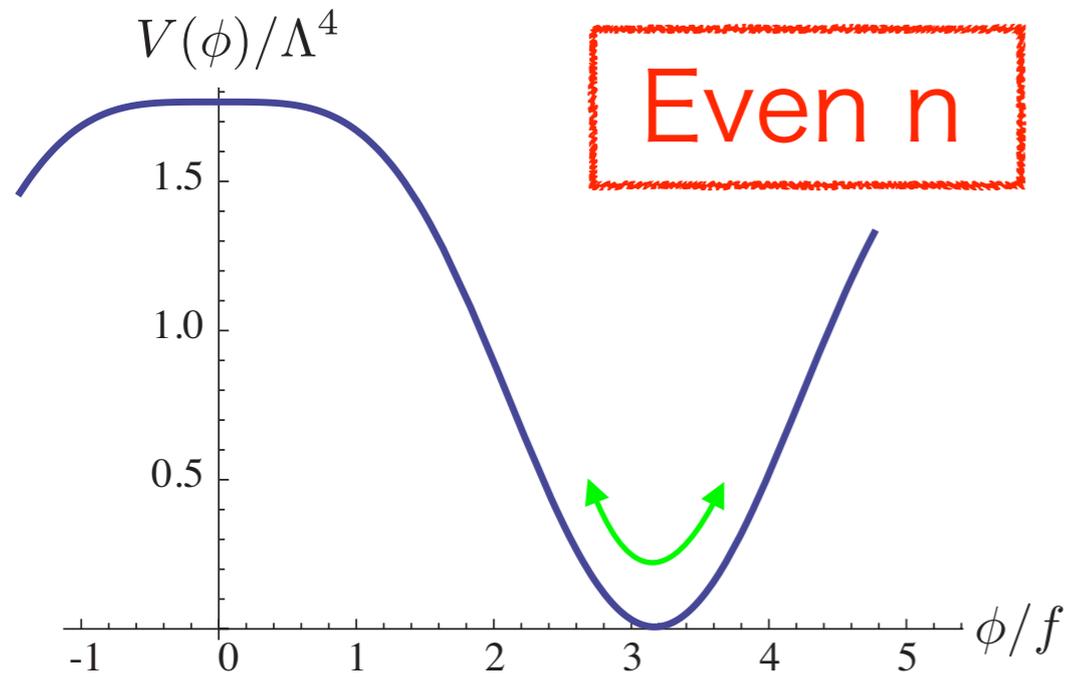
$$m_\phi \sim \frac{\Lambda^2}{f}$$

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$$f \sim 10^6 m_\phi$$

Czerny, Higaki, FT 1403.0410, FT and Yin, 1903.00462



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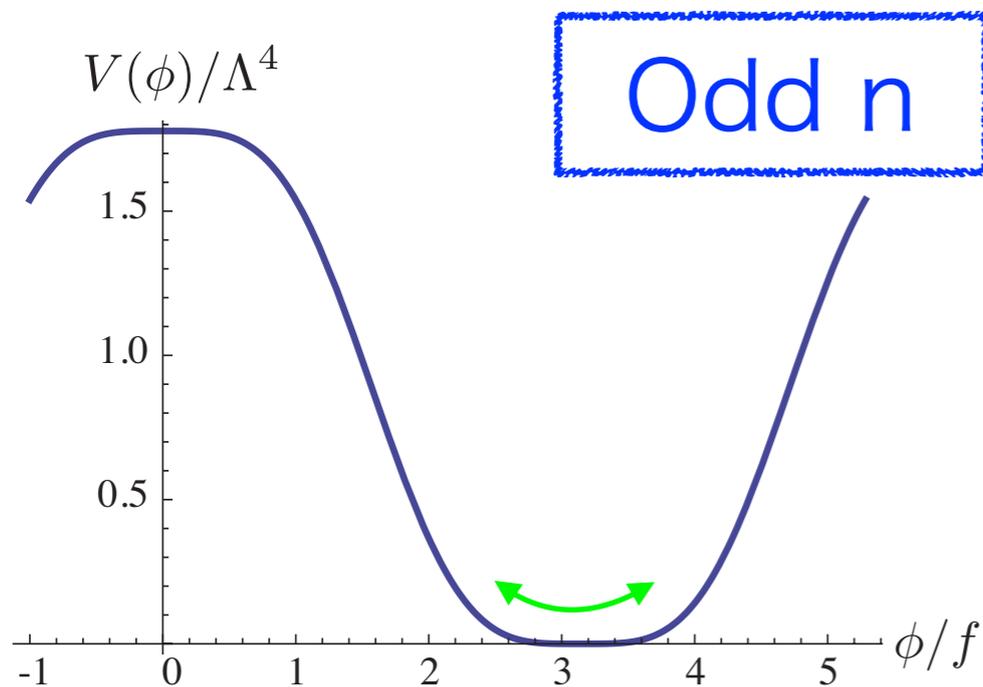
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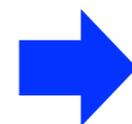
Czerny, Higaki, FT 1403.0410, FT and Yin, 1903.00462



The potential is flat both around the maximum and minimum.

$$1 - n_s = -2M_p^2 \frac{V''}{V} \simeq \frac{2}{3} \frac{m_\phi^2}{H_{\text{inf}}^2} \simeq 0.04$$

So  $m_\phi \sim 0.1 H_{\text{inf}} \sim 0.1 \frac{\Lambda^2}{M_p}$  + CMB norm.

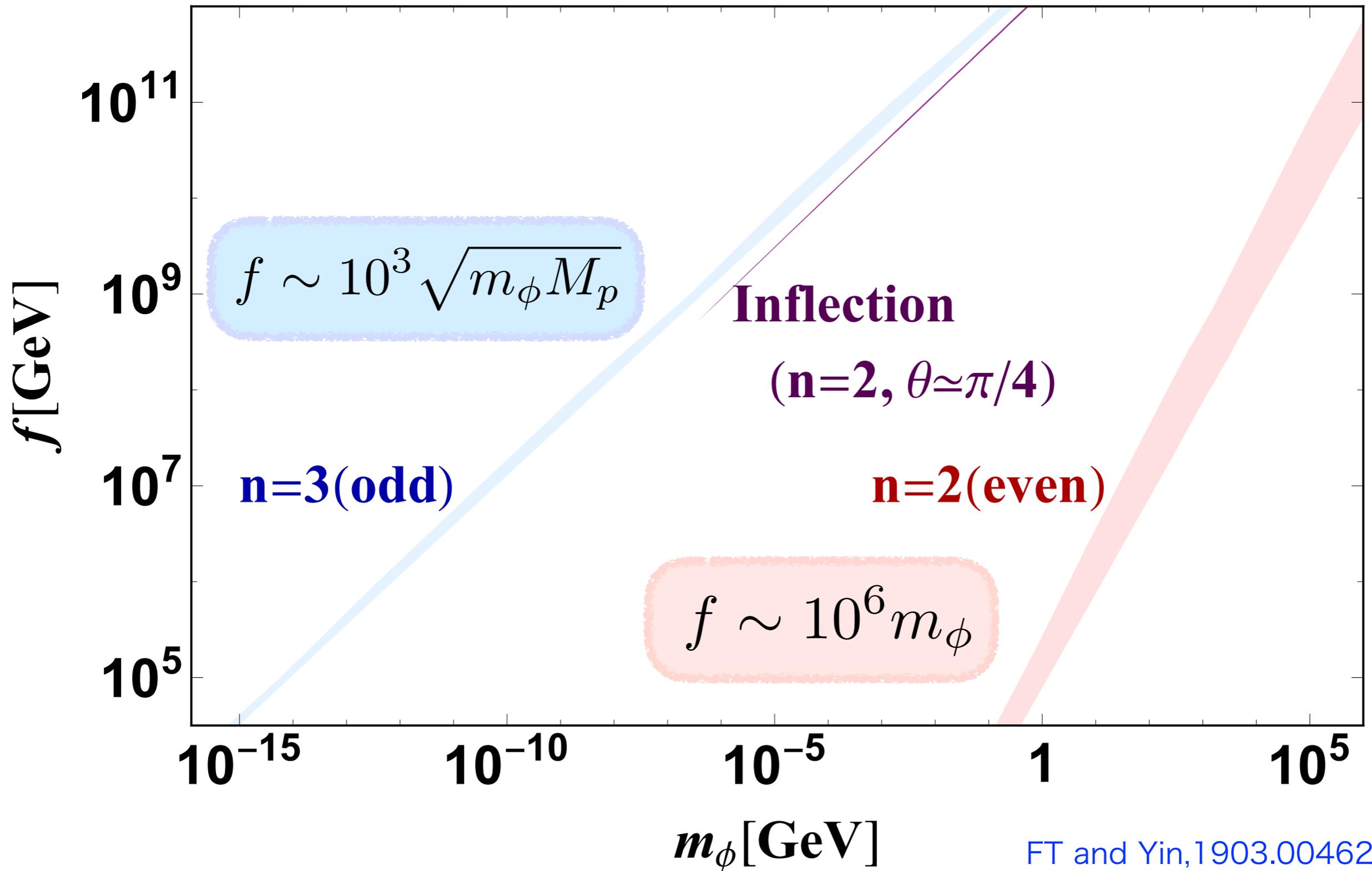


$$f \sim 10^3 \sqrt{m_\phi M_p}$$

Daido, FT, Yin, 1702.03284, 1710.11107

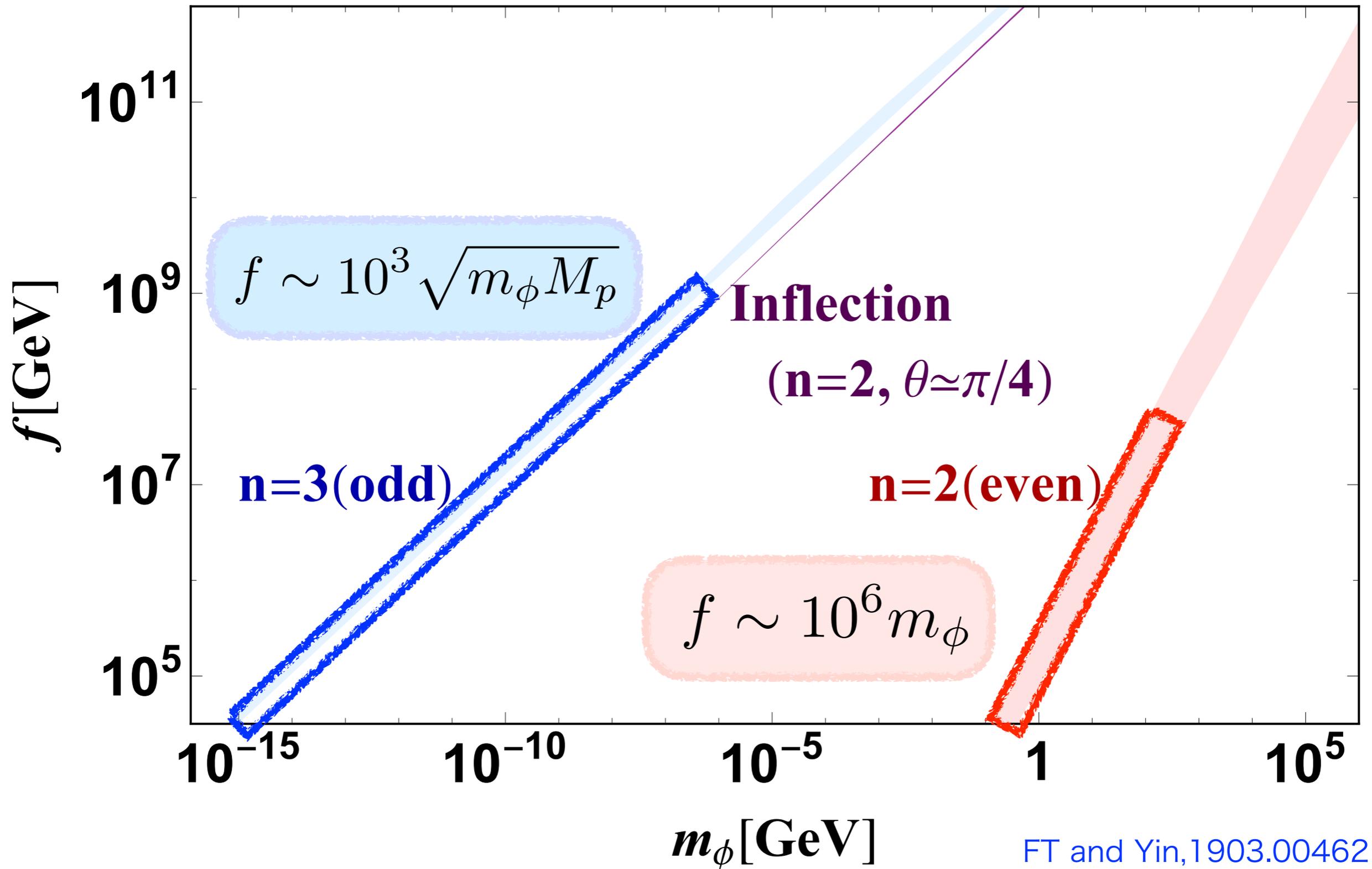
# ALP mass and decay constant

cf.  $f \sim 10^{12} \text{ GeV} (m_a/6 \mu\text{eV})^{-1}$  for QCD axion



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# ALP mass and decay constant

In the case of the ALP coupled to photons

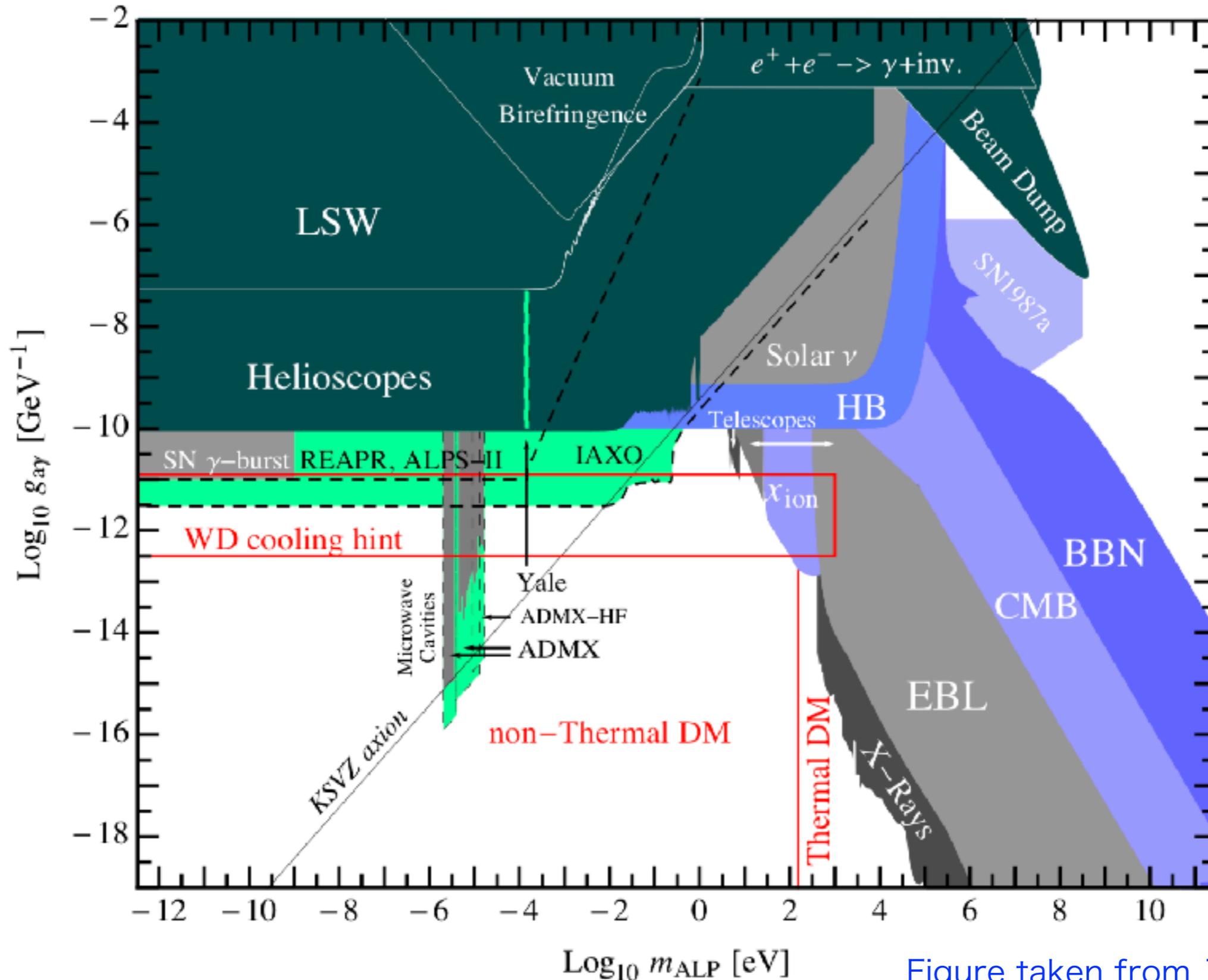


Figure taken from 1205.2671

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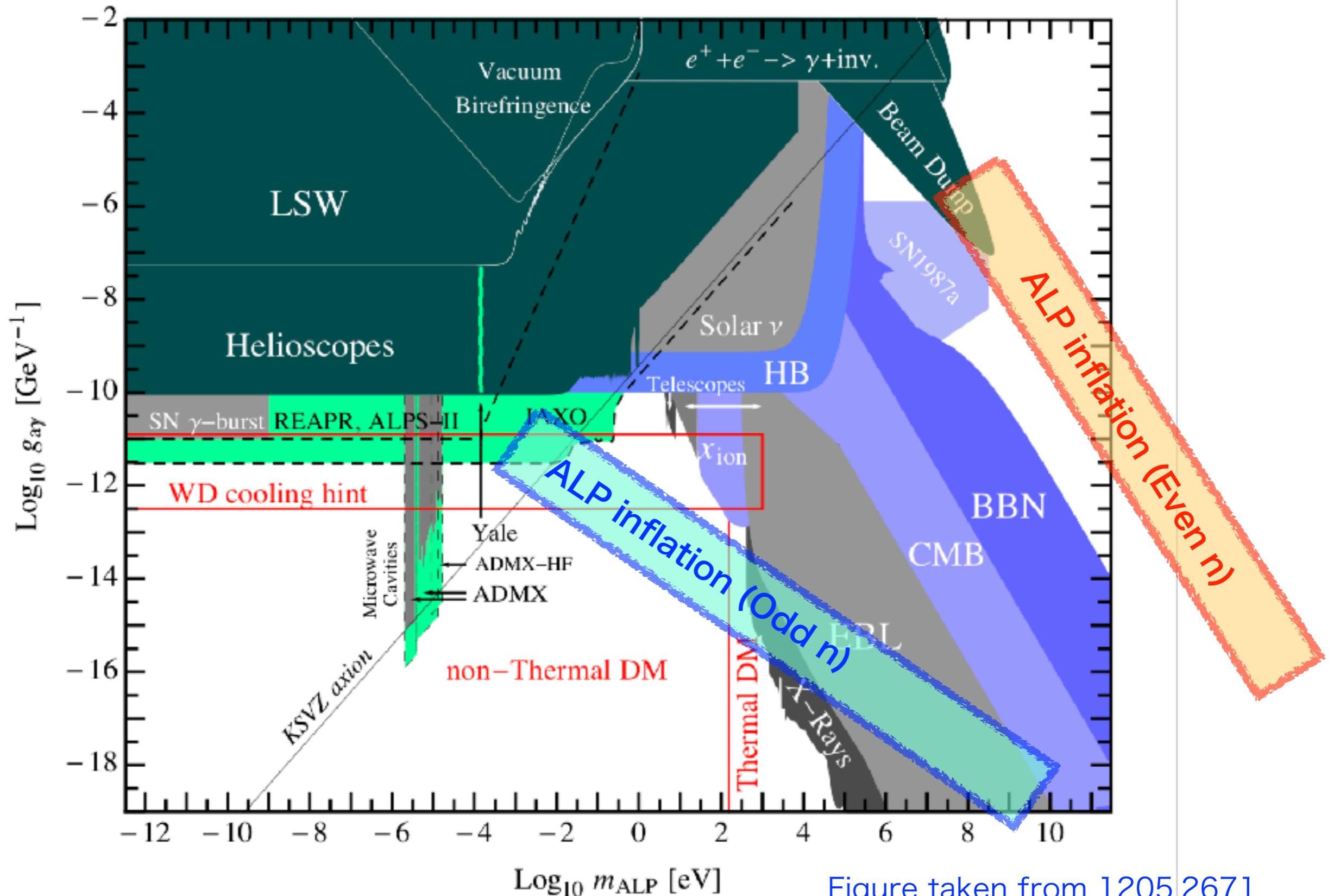


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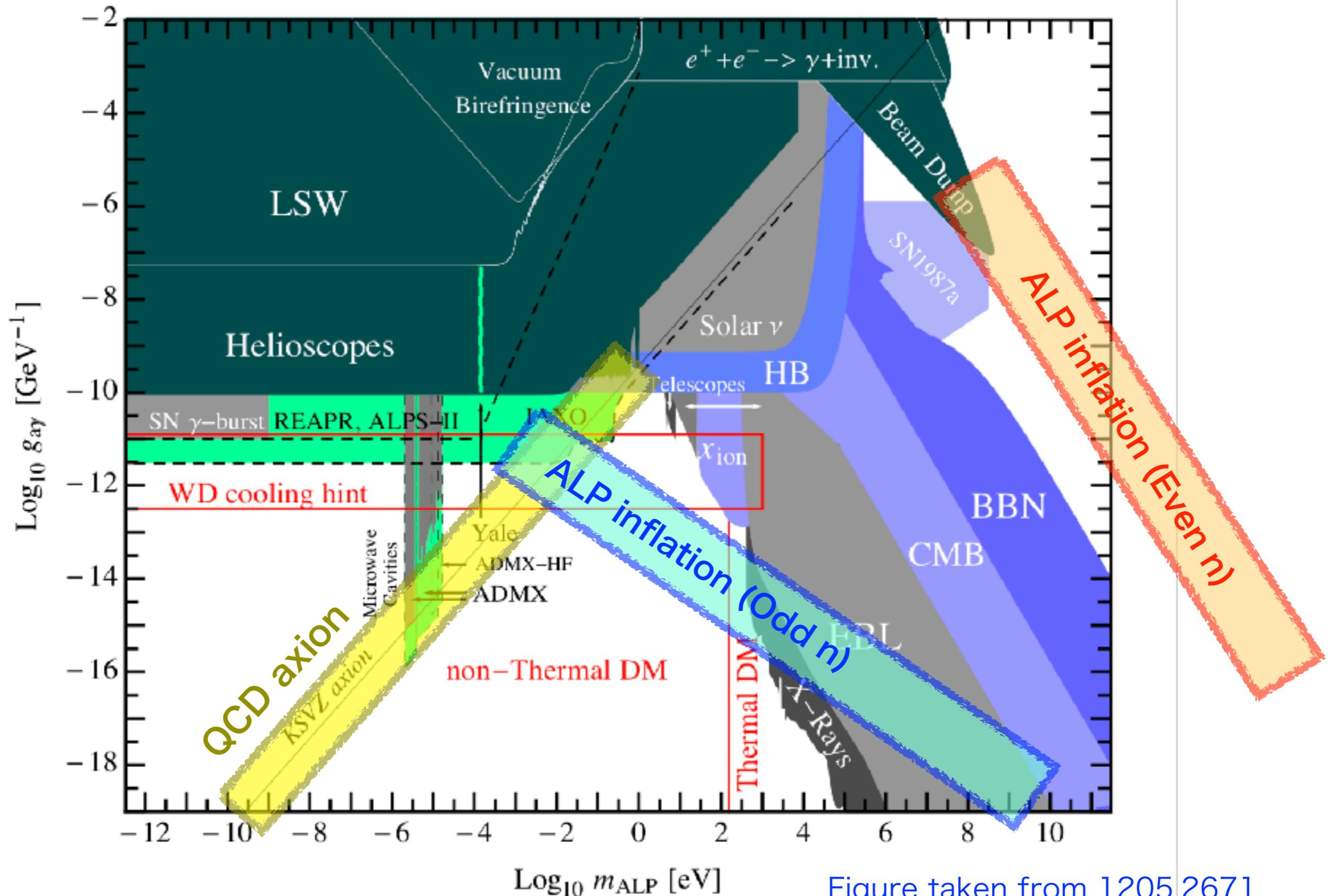
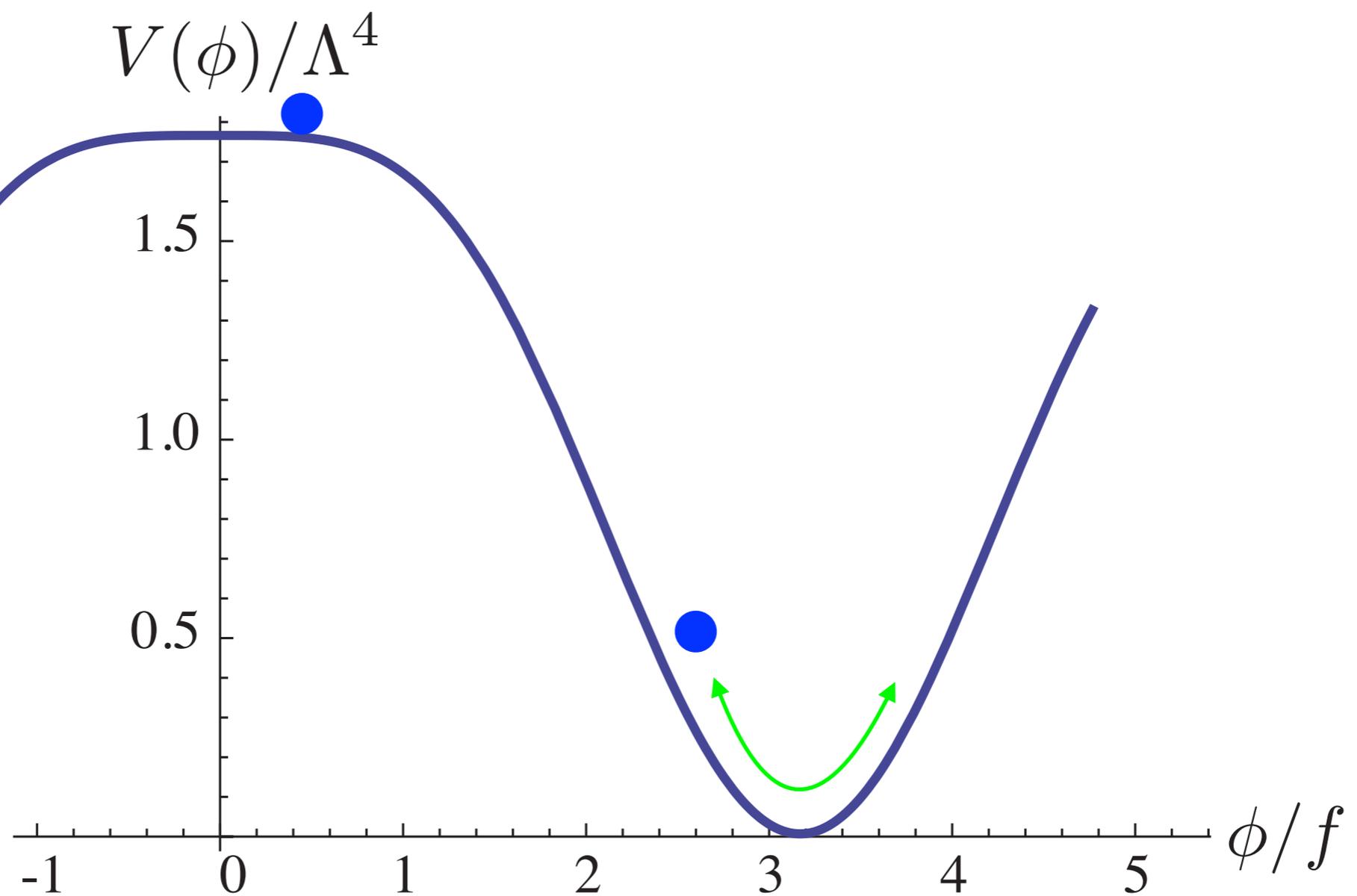


Figure taken from 1205.2671

# **3. Inflaton hunt by ground-based experiments**

# The case of even n



We consider the following ALP inflaton couplings to the SM:

**(1) Coupling to photons (or weak gauge bosons at high T)**

$$\mathcal{L} = c_\gamma \frac{\alpha}{4\pi} \frac{\phi}{f} F_{\mu\nu} \tilde{F}^{\mu\nu} \equiv \frac{1}{4} g_{\phi\gamma\gamma} \phi F_{\mu\nu} \tilde{F}^{\mu\nu},$$

**(2) Couplings to the SM fermions**

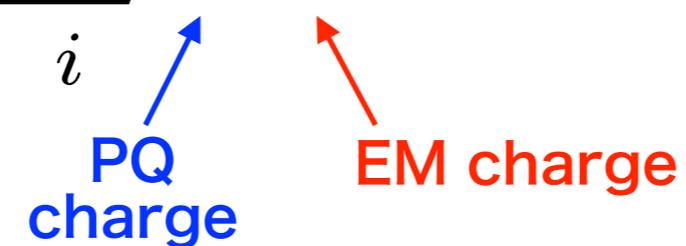
$$\mathcal{L} = \sum_k i \frac{c_k m_k}{f} \phi \bar{\psi}_k \gamma_5 \psi_k,$$

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$$g_{\phi\gamma\gamma} = \frac{c_\gamma \alpha}{\pi f}$$

where the anomaly coefficient is related to charges of the extra fermions  $\Psi_i$  as

$$c_\gamma = \sum_i q_i Q_i^2$$

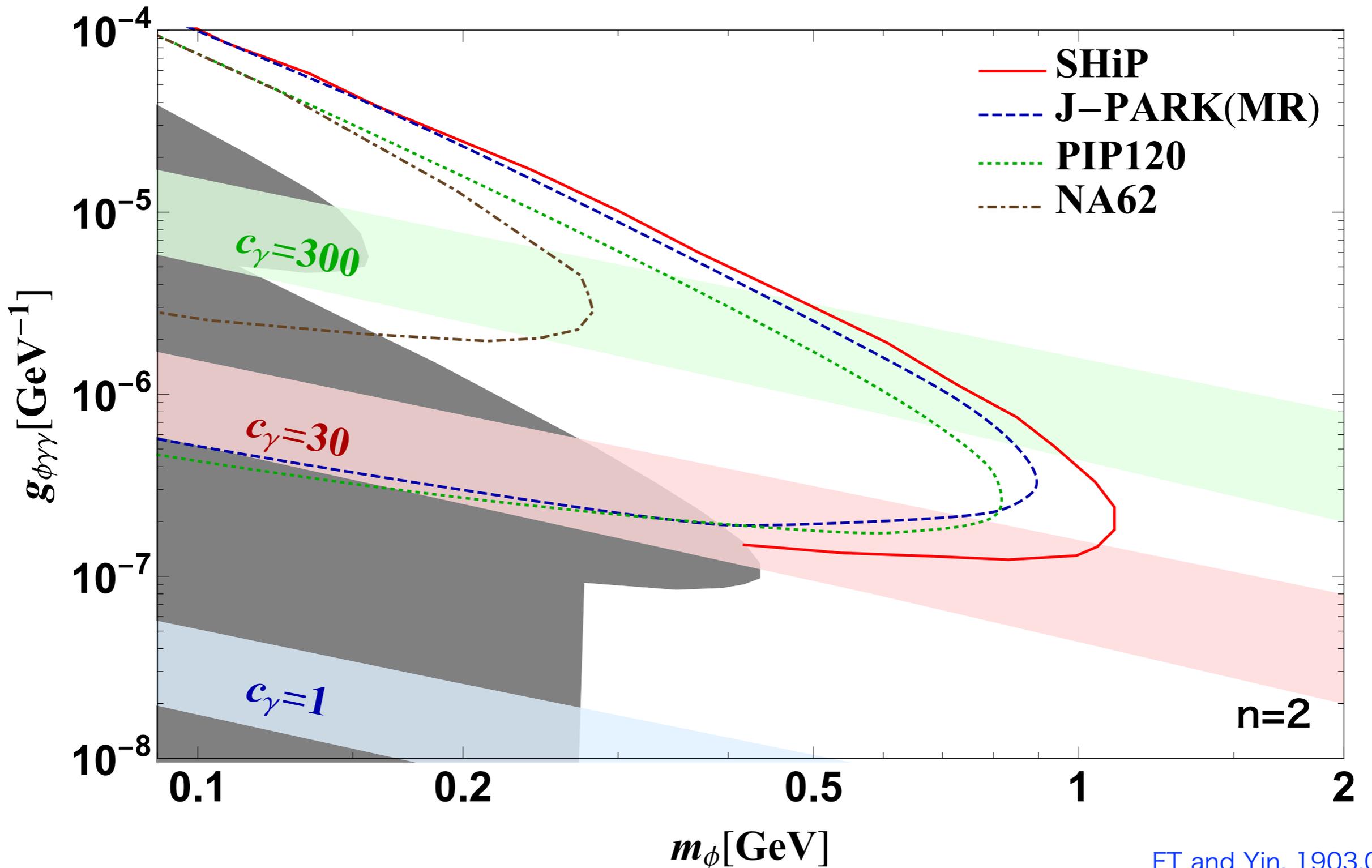


PQ charge      EM charge

$$\Psi_i \rightarrow e^{i\beta q_i \gamma_5 / 2} \Psi_i$$
$$\phi \rightarrow \phi + \beta f$$

The precise value of  $c_\gamma$  is model-dependent, and it can be of order  $10^{-2} - 10^2$  without invoking a contrived set-up.

# Parameter regions predicted by ALP inflation (with even n)



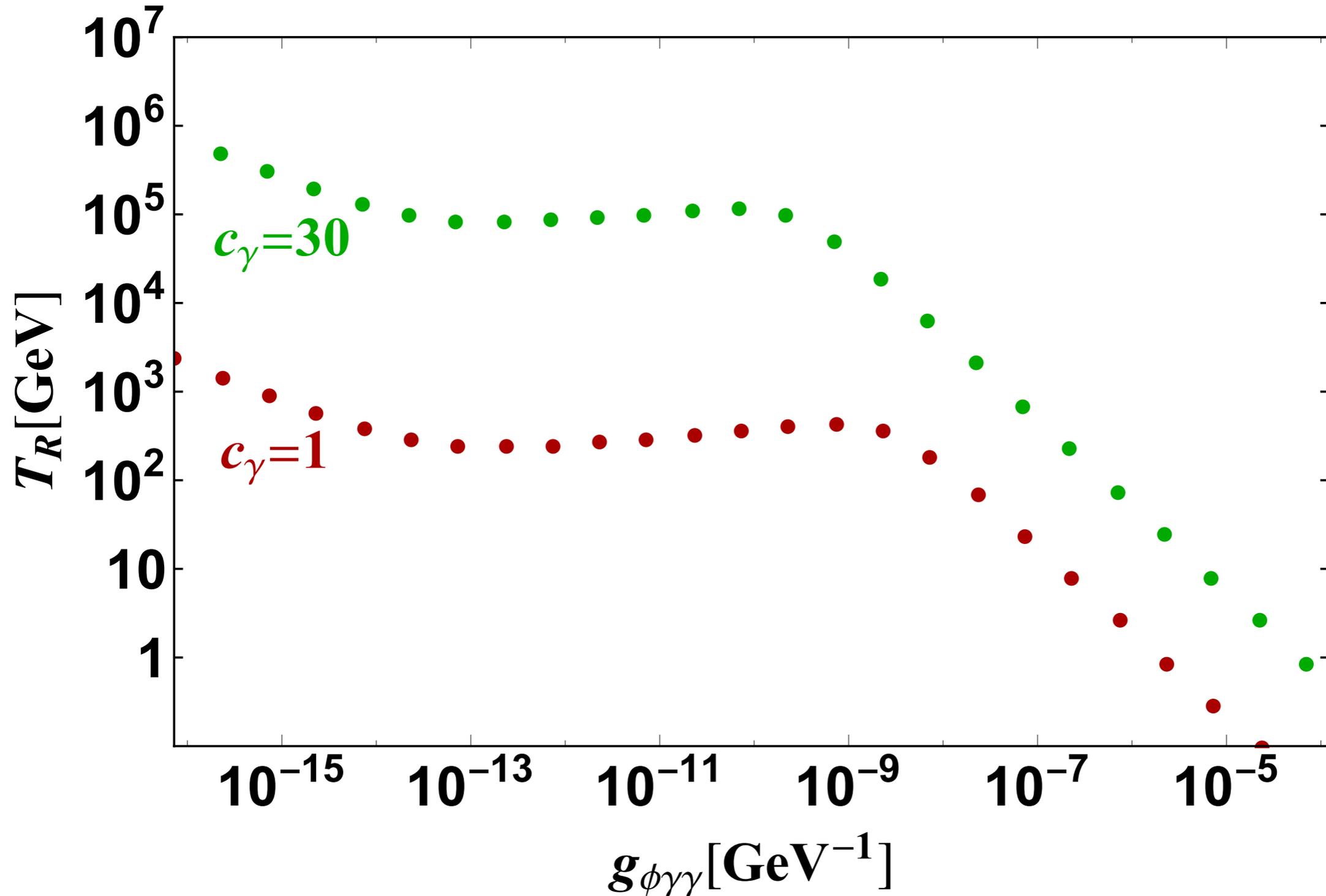
FT and Yin, 1903.00462,

Limits adopted from Harland-Land et al 1902.04878.

For  $c_{\gamma} \gtrsim 10$ , the predicted region overlaps with the SHiP sensitivity.

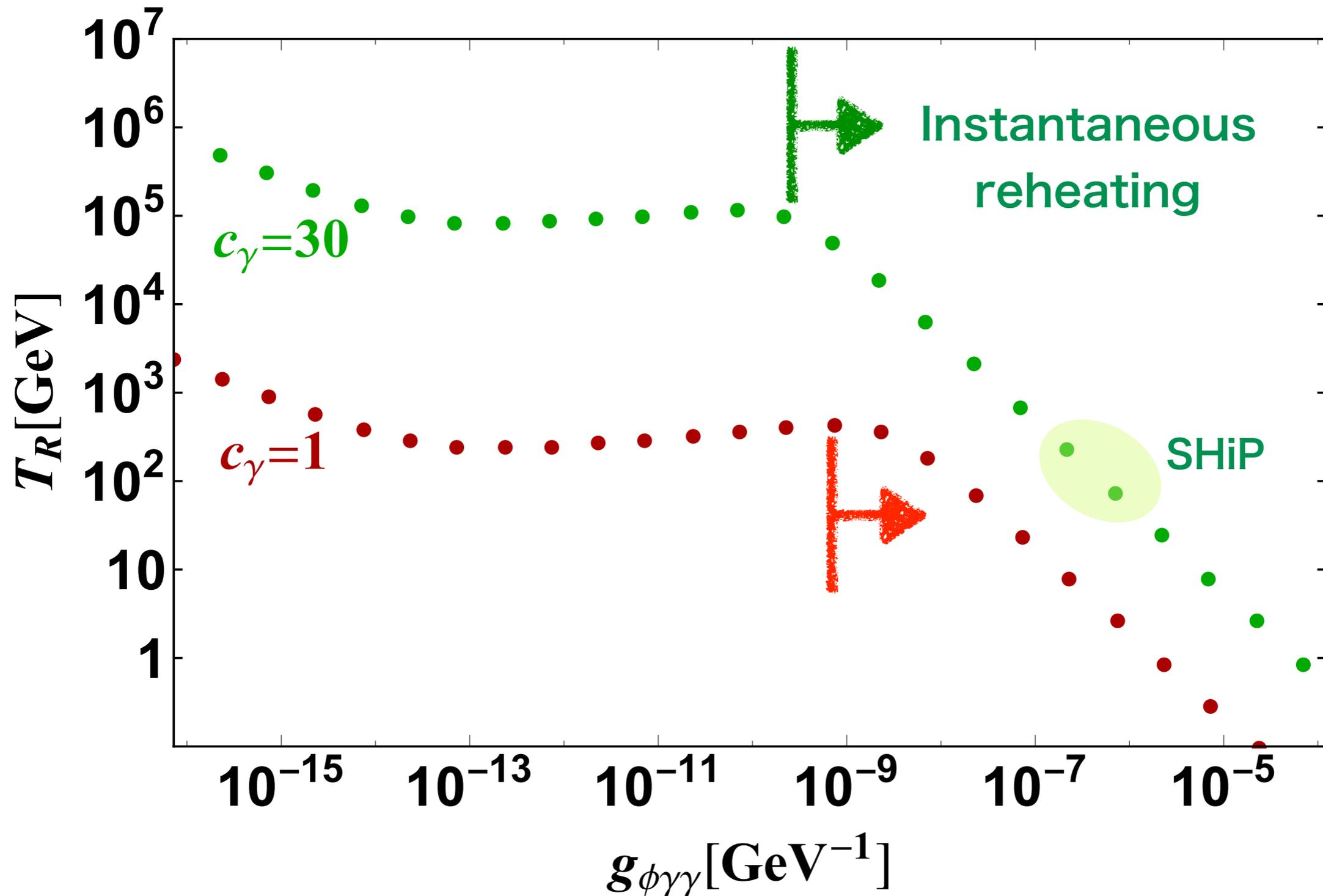
# Reheating thru ALP-photon coupling

The ALP inflaton decays into photons,  $\phi \rightarrow \gamma\gamma$ , and also dissipate through scattering, e.g.,  $\phi + \gamma \rightarrow e^+ + e^-$ .



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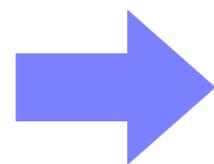


## (2) Couplings to the SM fermions

$$\mathcal{L} = \sum_k i \frac{c_k m_k}{f} \phi \bar{\psi}_k \gamma_5 \psi_k,$$

Such couplings arise if we introduce two Higgs doublets as in the DFSZ axion model. After integrating out the heavy degrees of freedom, we obtain

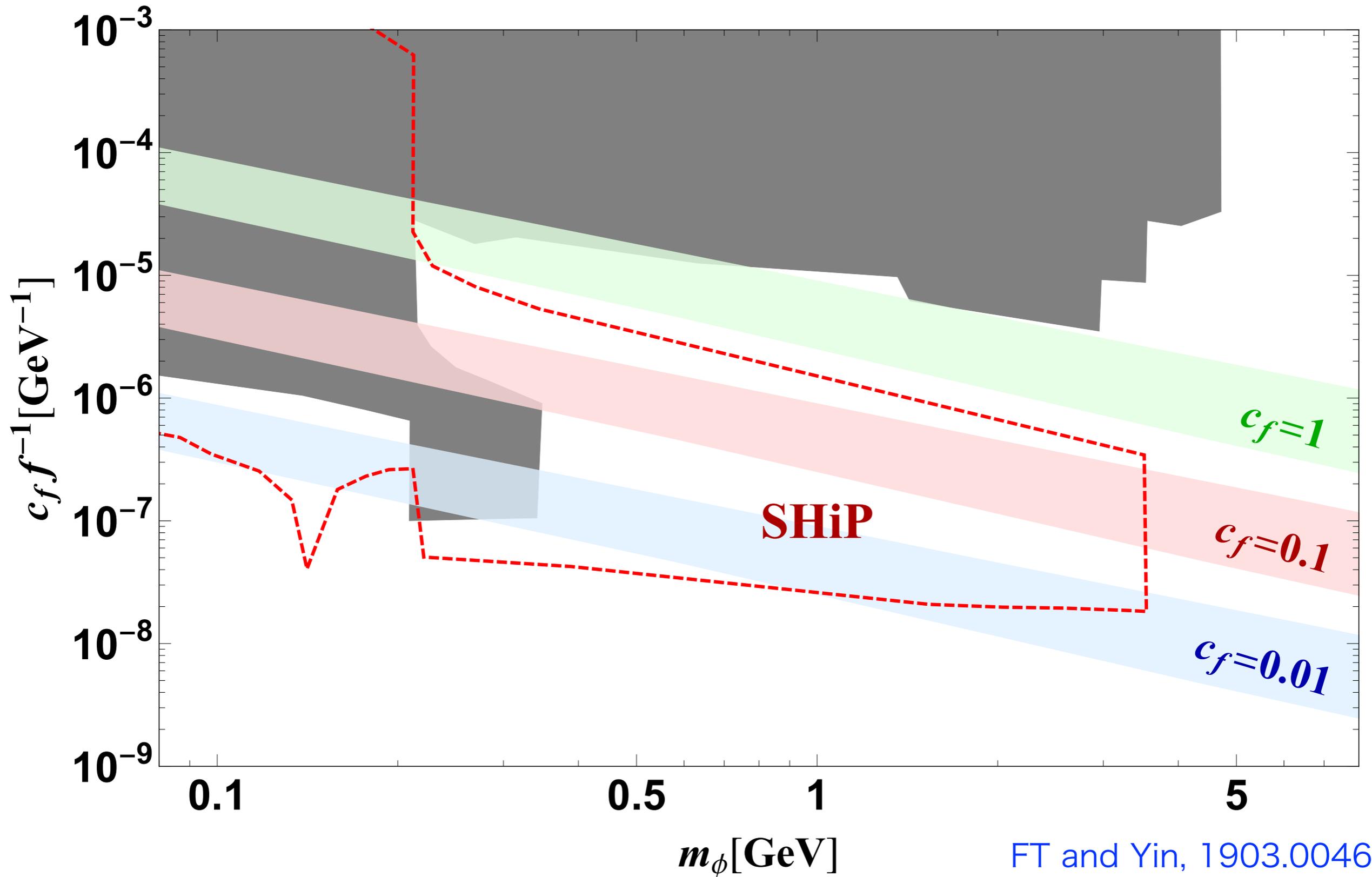
$$\begin{aligned} H_1 &= \overset{\text{SM Higgs}}{\downarrow} H \cos \beta \exp \left[ \overset{\text{PQ charge}}{\downarrow} i Q_{H_1} \frac{\phi}{f} \right], \\ H_2 &= \tilde{H} \sin \beta \exp \left[ i Q_{H_2} \frac{\phi}{f} \right], \end{aligned} \quad \tan \beta \equiv \frac{\langle H_2^0 \rangle}{\langle H_1^0 \rangle}$$



$$c_i = Q_{H_1} \text{ or } Q_{H_2}$$

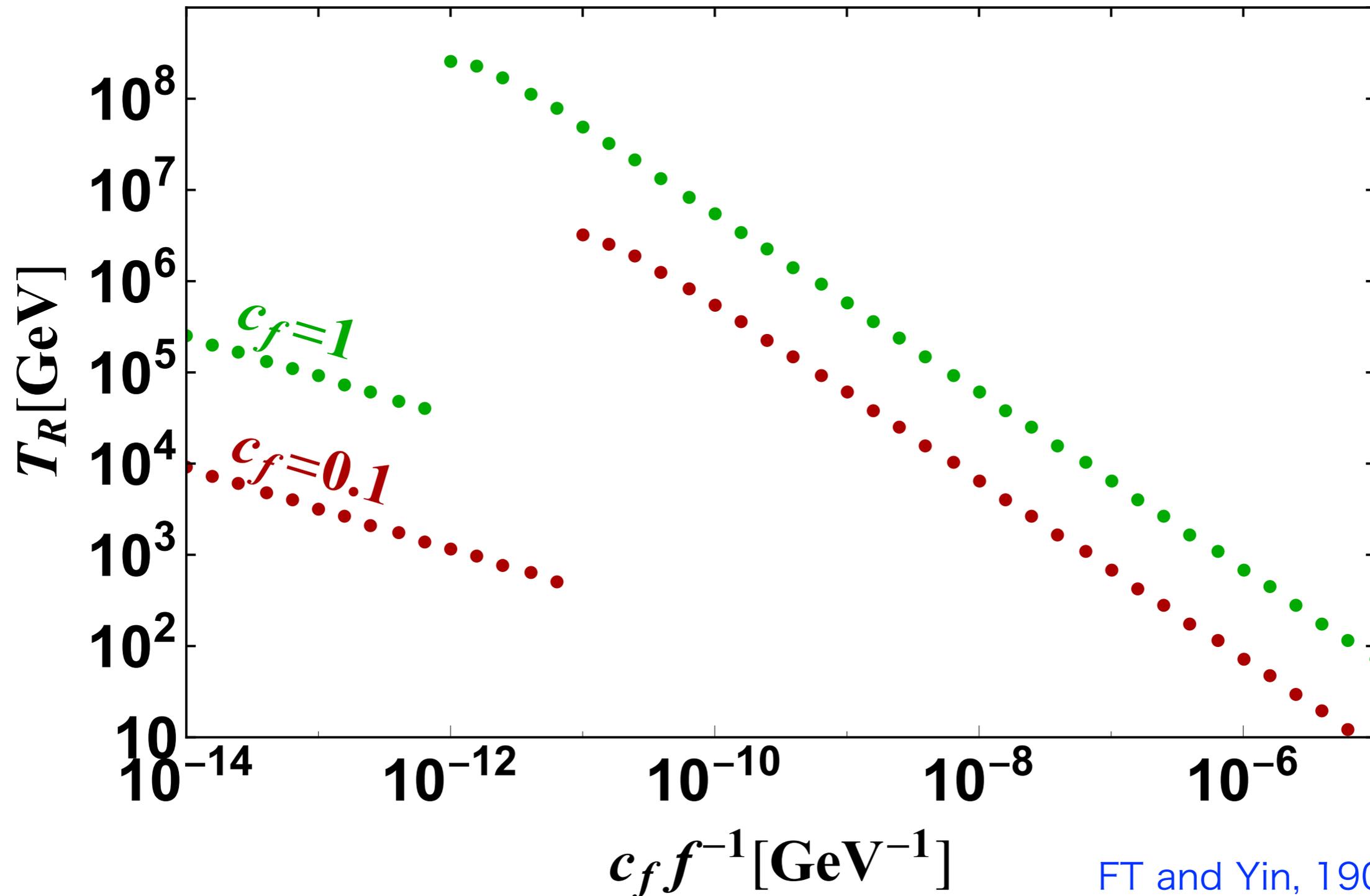
(i.e. PQ charge of the Higgs that it is coupled to.)

In the case that the inflaton has (universal) Yukawa-like interactions, i.e.,  $c_i = c_f$



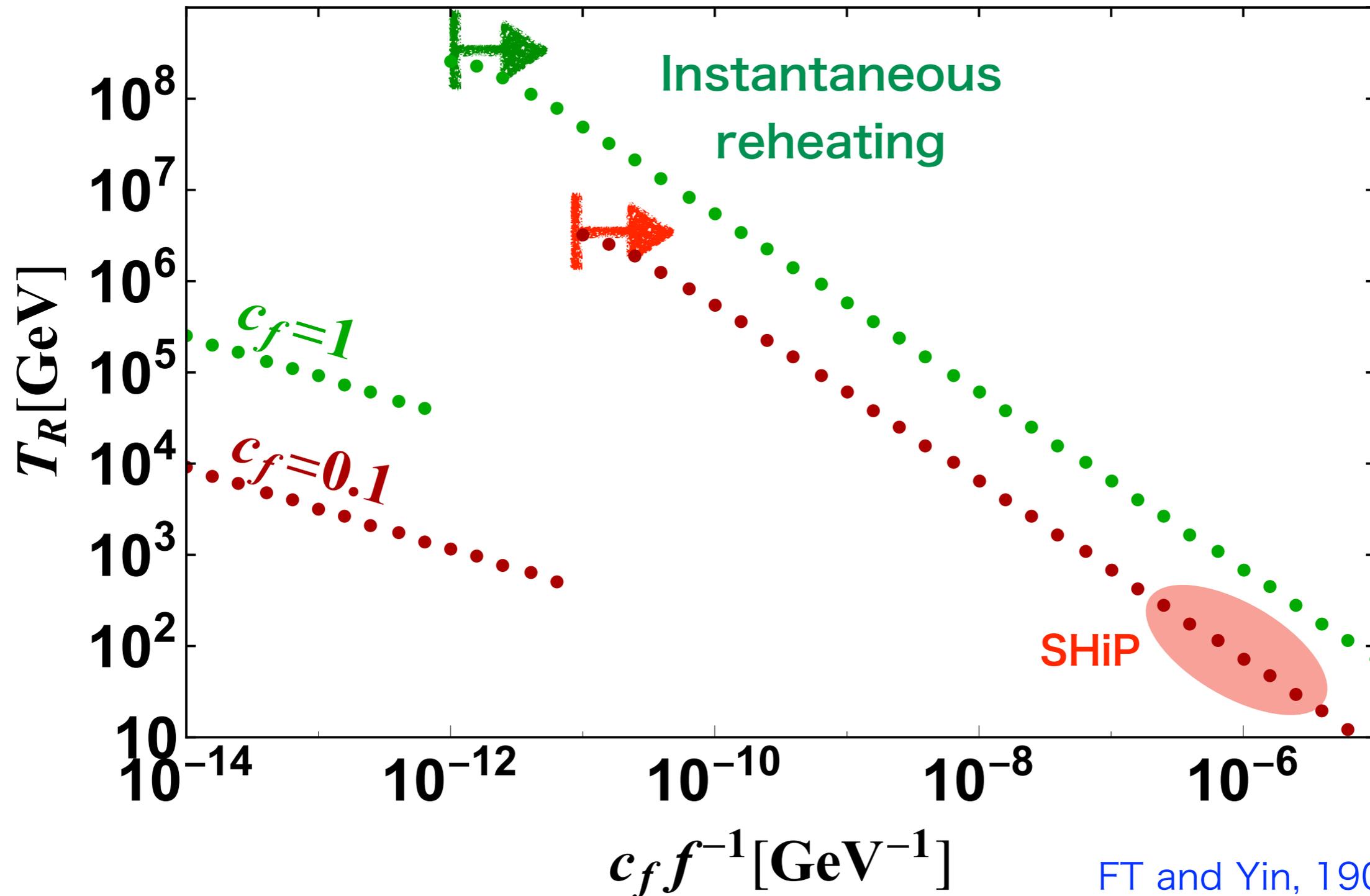
# Reheating thru Yukawa-like couplings

The ALP inflaton decays into the SM fermions (+Higgs if kinematically allowed), and dissipate through thermal scattering.

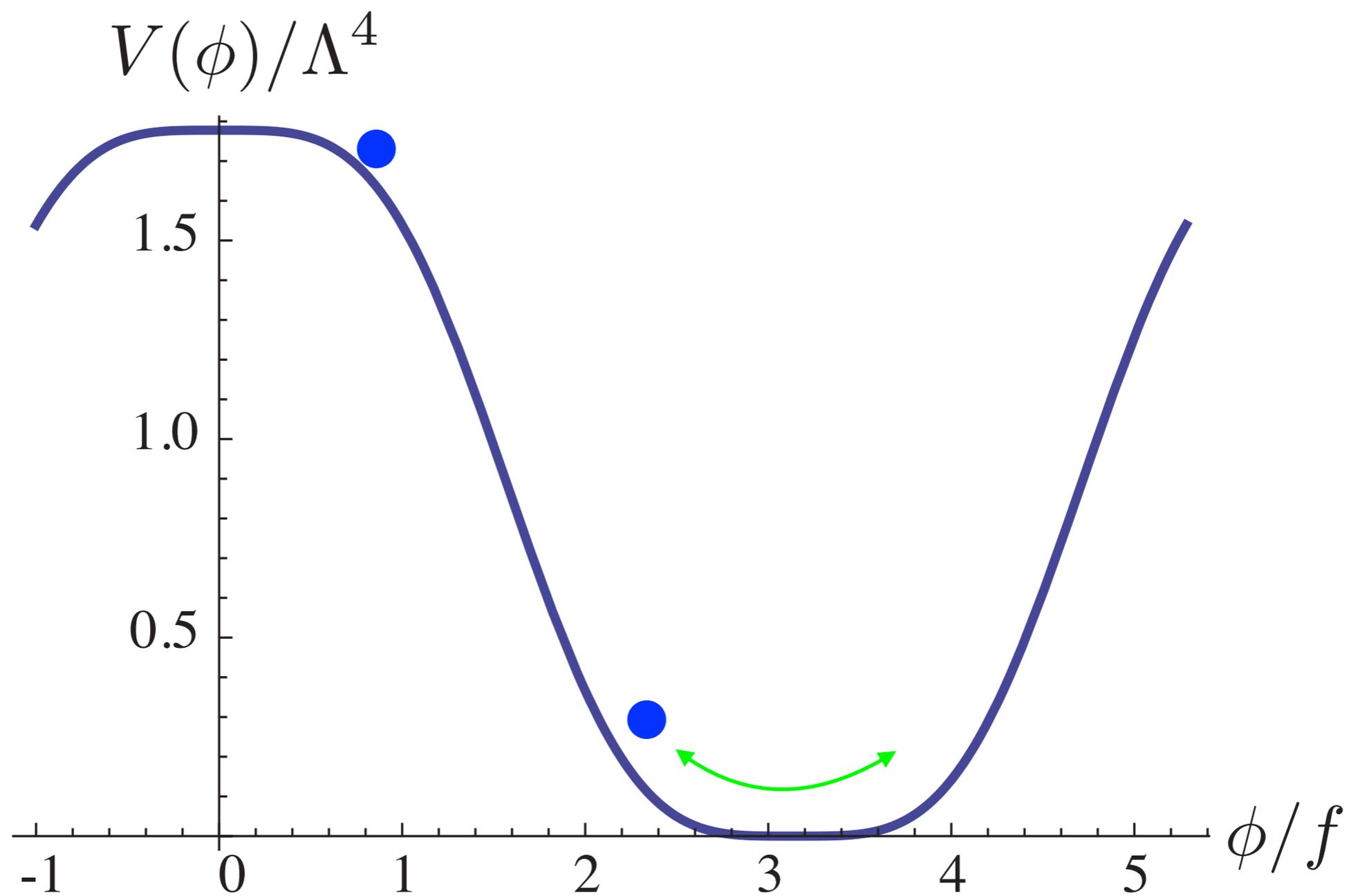


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# The case of odd $n$



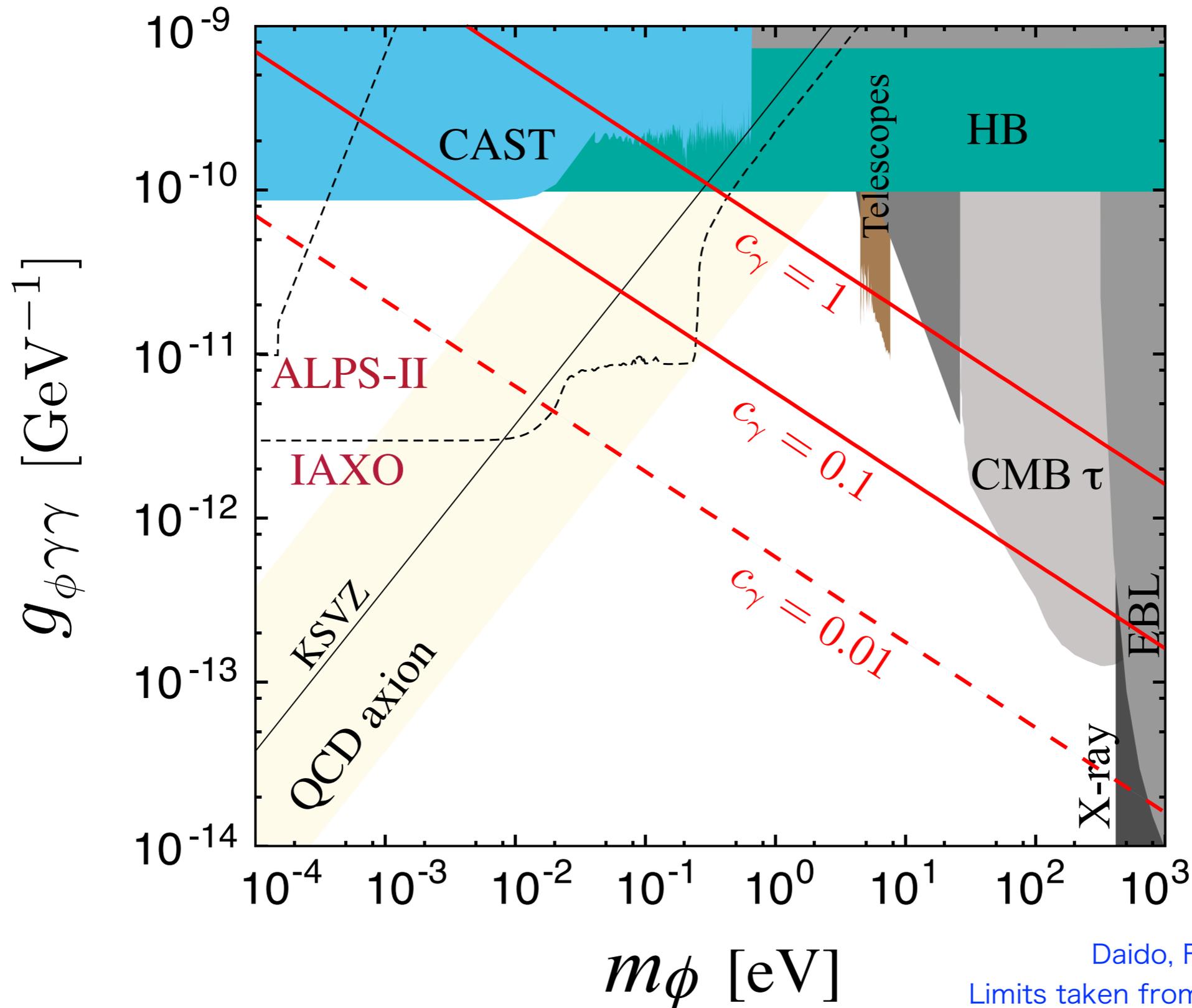
# • Inflaton (ALP) mass and coupling to photons

$$\mathcal{L} = \frac{g_{\phi\gamma\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu} \quad g_{\phi\gamma\gamma} = \frac{c_\gamma \alpha}{\pi f}$$

$$c_\gamma = \sum_i q_i Q_i^2$$

$$\psi_i \rightarrow e^{i\beta q_i \gamma_5 / 2} \psi_i$$

$$\phi \rightarrow \phi + \beta f$$



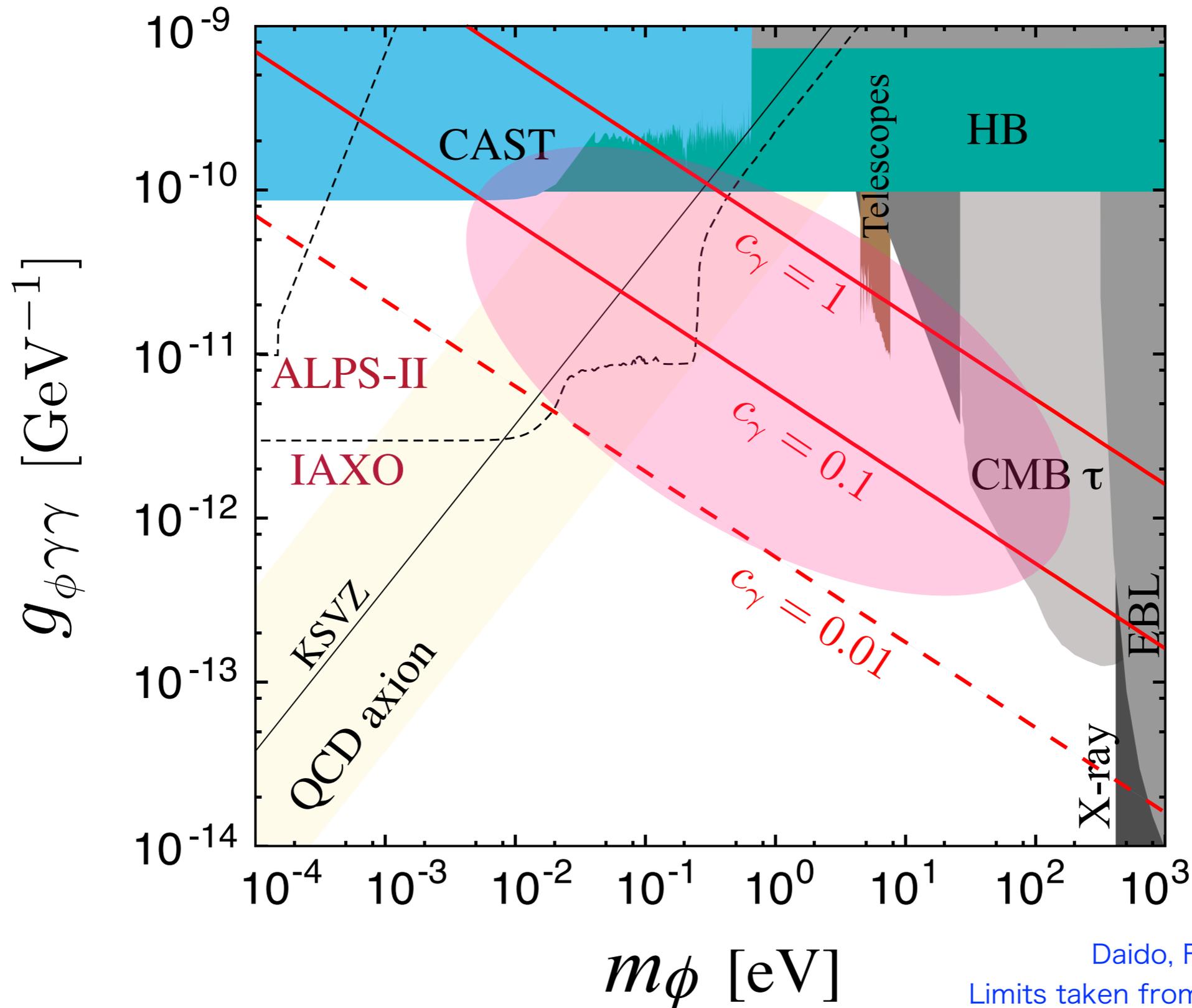
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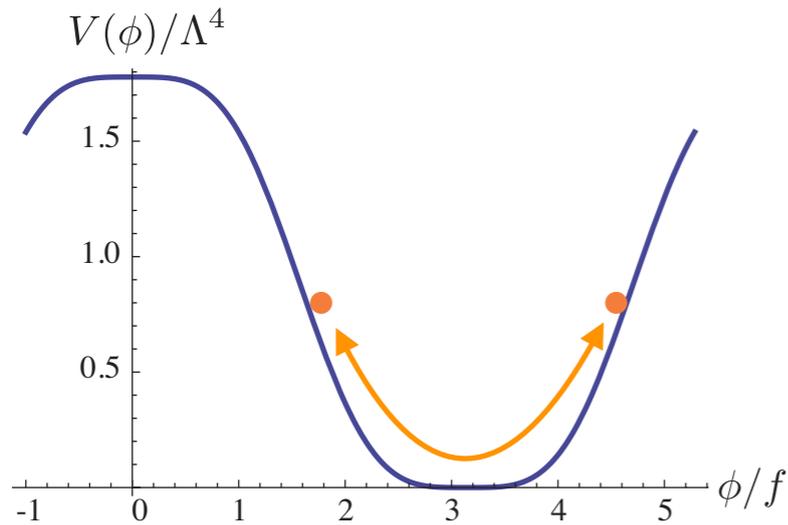
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$$\phi \rightarrow \phi + \beta f$$



ALP inflation  
w/ odd n

# Reheating and ALP DM



Inflaton (ALP)  
condensate

$$\mathcal{L} = \frac{g_{\phi\gamma\gamma}}{4} \phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$\xi \equiv \left. \frac{\rho_\phi}{\rho_\phi + \rho_R} \right|_{\text{after reheating}}$$

Decay &  
dissipation

Photons,  
SM particles

Thermalized

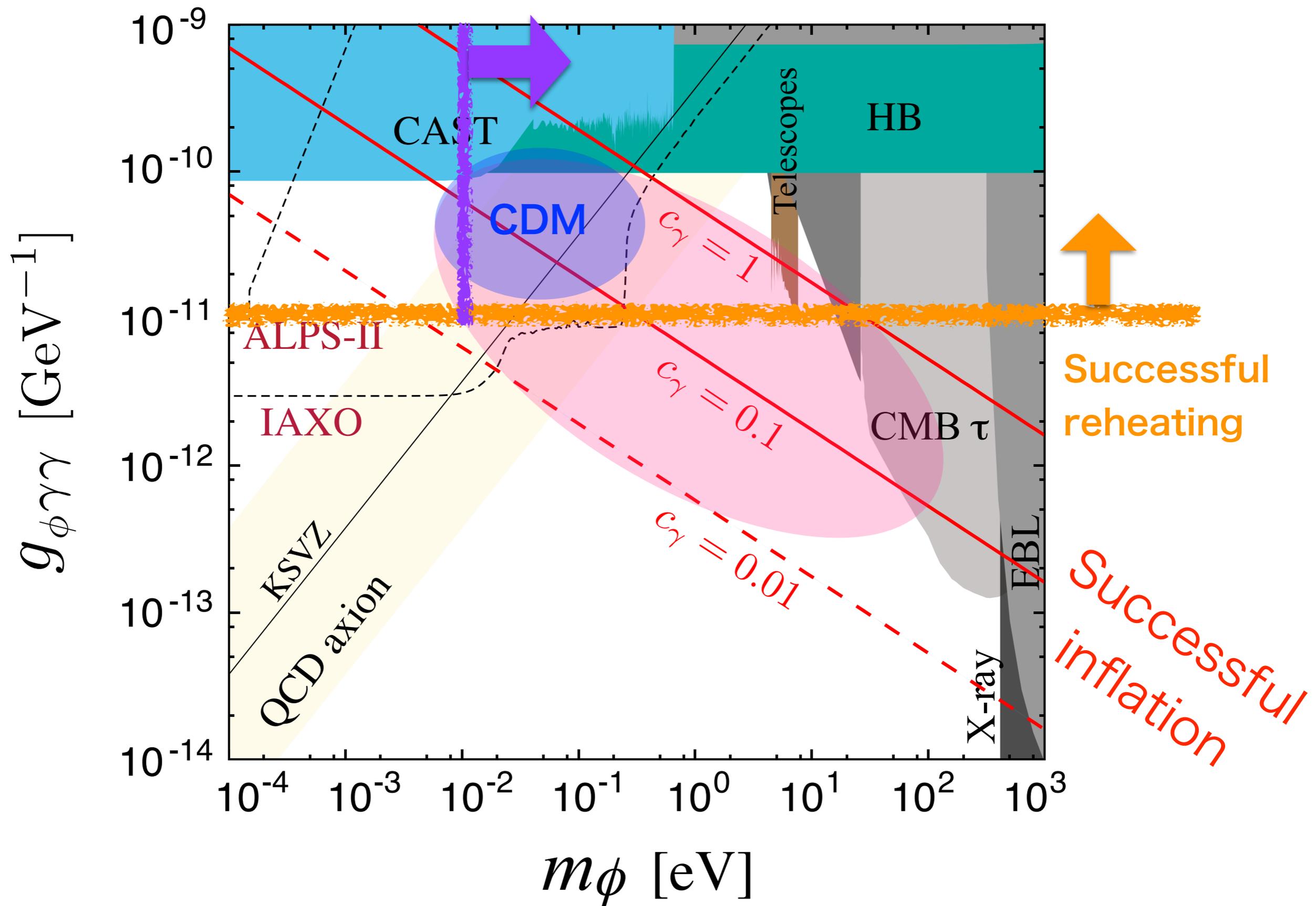
ALP Dark Radiation  
or HDM

Remnant

ALP Dark Matter

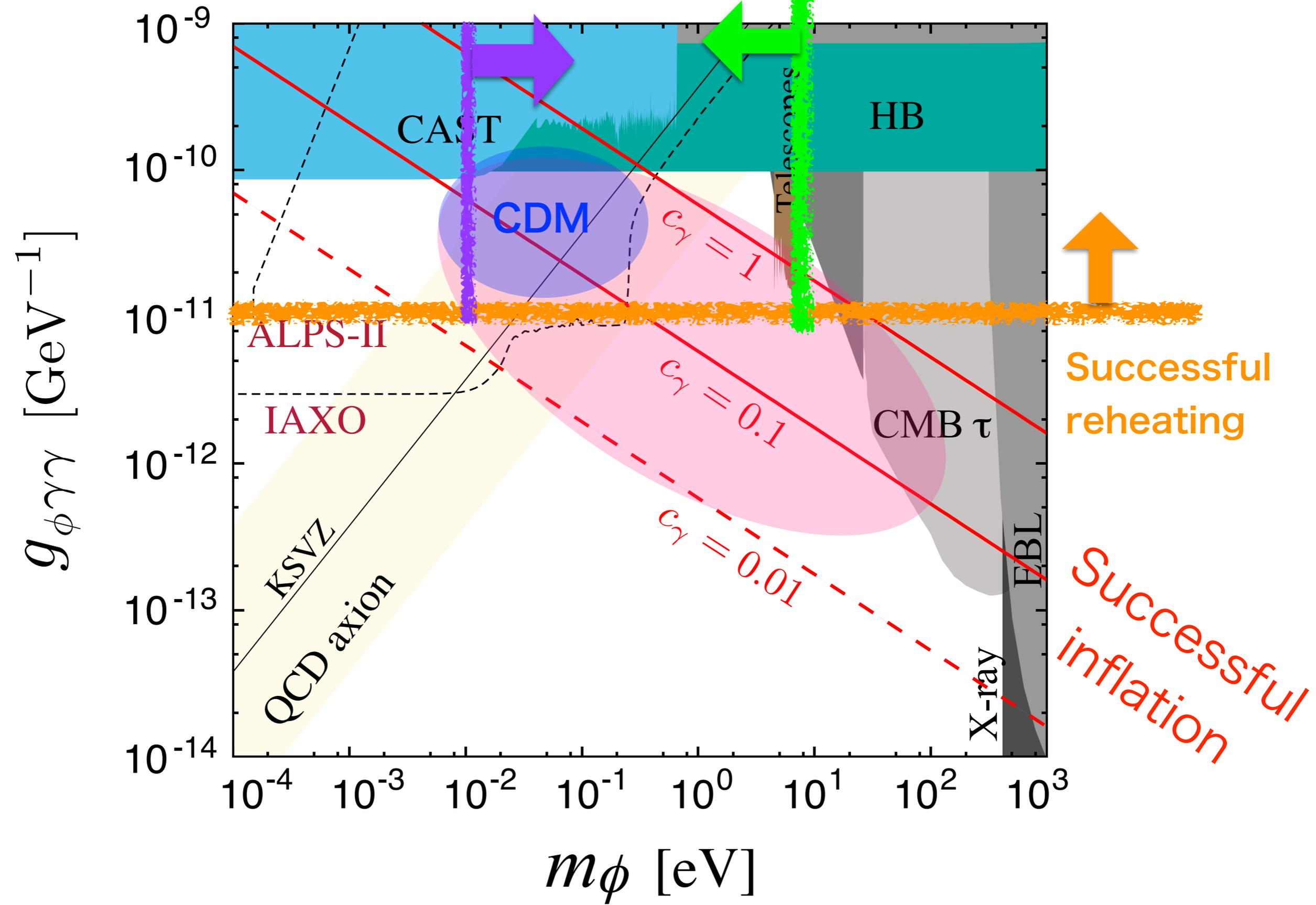
As we shall see,  $\xi = \mathcal{O}(0.01)$  is required to explain DM.

# Small-scale structure constraint on ALP CDM



Small-scale structure  
constraint on ALP CDM

HDM constraint on  
thermalized ALP

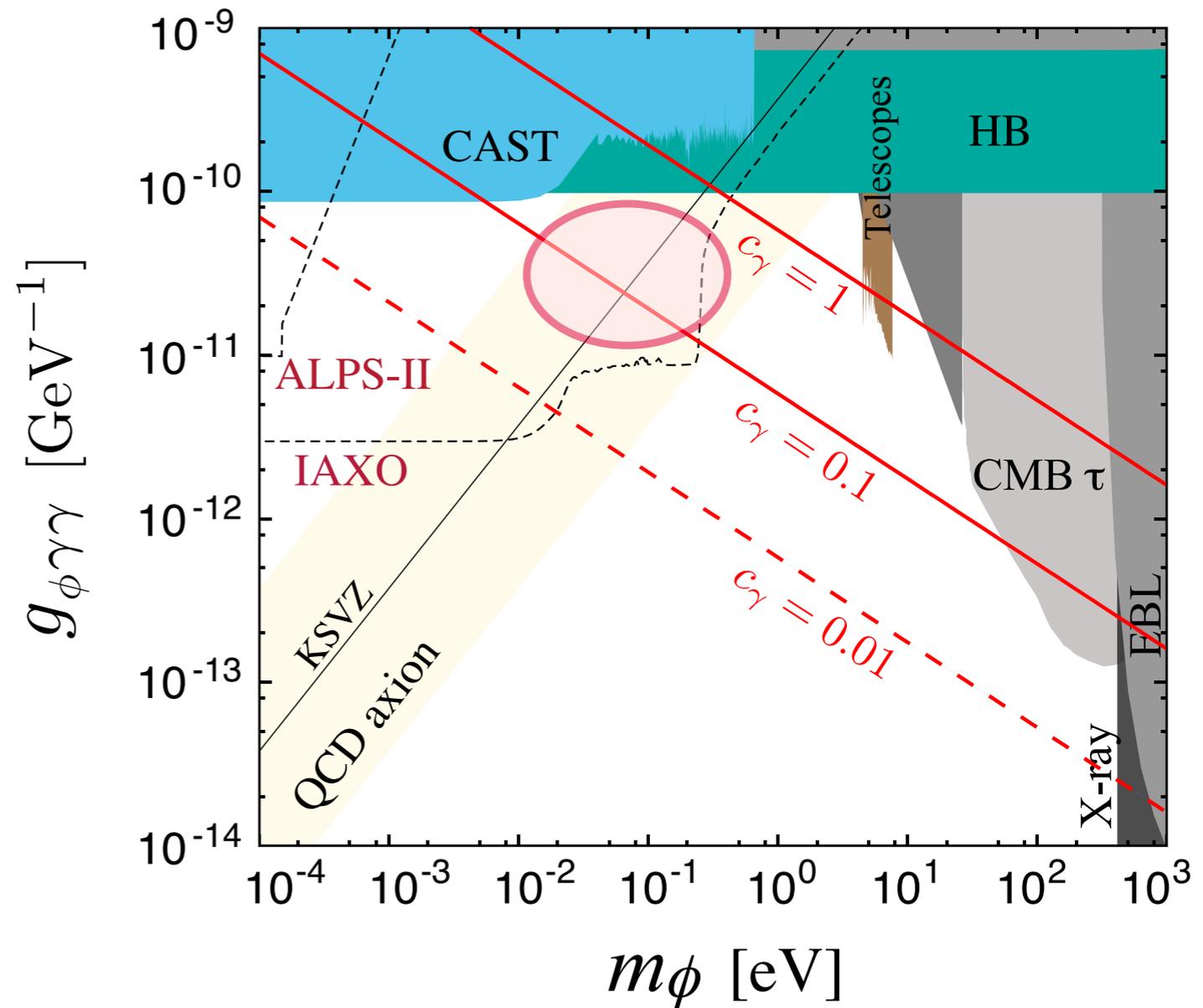


# Inflaton = DM = ALP



$$m_\phi = \mathcal{O}(0.01 - 1) \text{ eV}$$
$$g_{\phi\gamma\gamma} = \mathcal{O}(10^{-11}) \text{ GeV}^{-1}$$

within the reach of future axion helioscopes and laser experiments.



*“An ALP miracle”*

\*Plus, there is a preference for extra cooling of HB stars

$$g_{\phi\gamma\gamma} = (0.29 \pm 0.18) \times 10^{-10} \text{ GeV}^{-1}$$

# Summary

- Inflaton may be searched for at experiments, if the inflaton is an NG boson with sizable couplings to SM.
- The predicted relations between the mass and decay constant are

## Even n

$$f \sim 10^6 m_\phi$$

- SHiP (beam dump exp. at CERN)

$$m_\phi = O(0.1 - 1) \text{ GeV}$$

- The decay of the axion is same as the reheating!

“Big Bang on Earth”

## Odd n

$$f \sim 10^3 \sqrt{m_\phi M_p}$$

- IAXO/TASTE (Solar axion search)

$$m_\phi = O(0.01 - 1) \text{ eV}$$

- The remnant inflaton can be DM. “ALP miracle”
- Dark radiation with  $\Delta N_{\text{eff}} \simeq 0.03$