

# Dark Matter Theory

## Current status of WIMP DM

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Tohoku University

*Revealing the history of the universe with underground particle and nuclear research 2019*

# Target of the talk

Tons of DM candidates have been proposed so far...

e.g.)

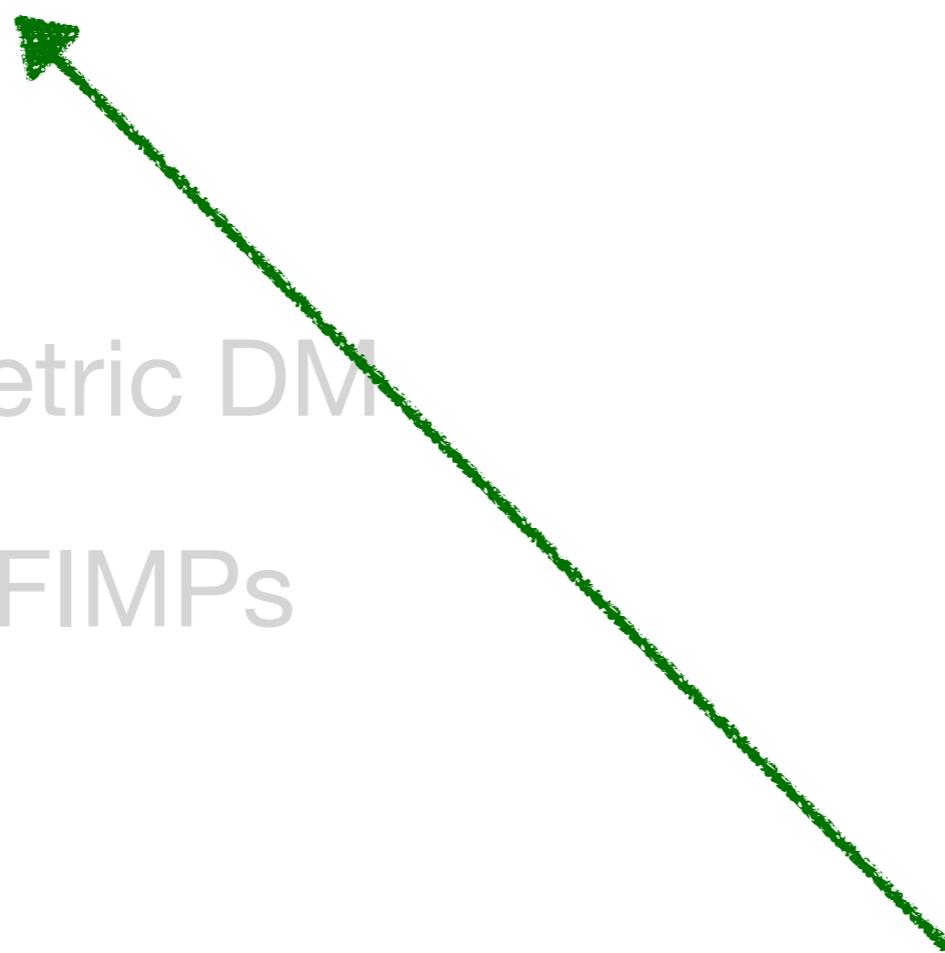
- ▶ WIMPs
  - ▶ Axion
  - ▶ Asymmetric DM
  - ▶ SIMPs, FIMPs
  - ▶ etc...
- 
- Talks by Andreas & Kawasaki-san
- Talk by Ibe-san

# Target of the talk

Tons of DM candidates have been proposed so far...

e.g.)

- ▶ WIMPs
- ▶ Axion
- ▶ Asymmetric DM
- ▶ SIMPs, FIMPs
- ▶ etc...



Let me focus on WIMP DM in this talk.

# WIMP

## Weakly-Interacting Massive Particles (WIMPs)

- ▶ Electrically neutral and colorless particles.
- ▶ Stable.
- ▶ Masses of order Electroweak (EW) scale.
- ▶ Have interactions comparable to EW interactions.



Observed Dark Matter (DM) density can be explained by their **thermal relic**.

# TeV-scale physics and WIMP

## DM thermal relic abundance

$$\Omega_{\text{DM}} h^2 \simeq \frac{3 \times 10^{-27} \text{cm}^3 \text{s}^{-1}}{\langle \sigma_{\text{ann}} v_{\text{rel}} \rangle}$$

$$\Omega_{\text{DM}} h^2 = 0.12 \quad \rightarrow \quad \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \simeq 10^{-9} \text{ GeV}^{-2}$$

e.g.)

$$\langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \simeq \frac{\alpha^2}{m_{\text{DM}}^2} \quad \alpha \simeq 0.01 \quad m_{\text{DM}} \simeq 300 \text{ GeV}$$

WIMP DM predicted new physics at the TeV scale.

WIMPs often appear in models motivated by naturalness.

Expected to be tested in various experiments (such as LHC).

# Goal of the talk

- DM candidates in TeV-scale new physics models have been severely constrained.

Target has been narrowed down.

- On the other hand, the WIMP paradigm itself has not been fully tested yet.

Further exploration is needed.

# Outline

- Viable WIMP DM candidates in SUSY
- Current status of WIMP DM
- Summary

# **DM in SUSY models**

# Supersymmetry (SUSY)

The LHC results, *i.e.*,

- Bound on SUSY particles
- 125 GeV Higgs mass

→ SUSY particles are heavier than expected.

Restrict WIMP DM candidates in (simple) SUSY models.

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Two simple setups

- Constrained MSSM
- High-scale SUSY

# Constrained MSSM (CMSSM)

## Constrained MSSM (CMSSM)

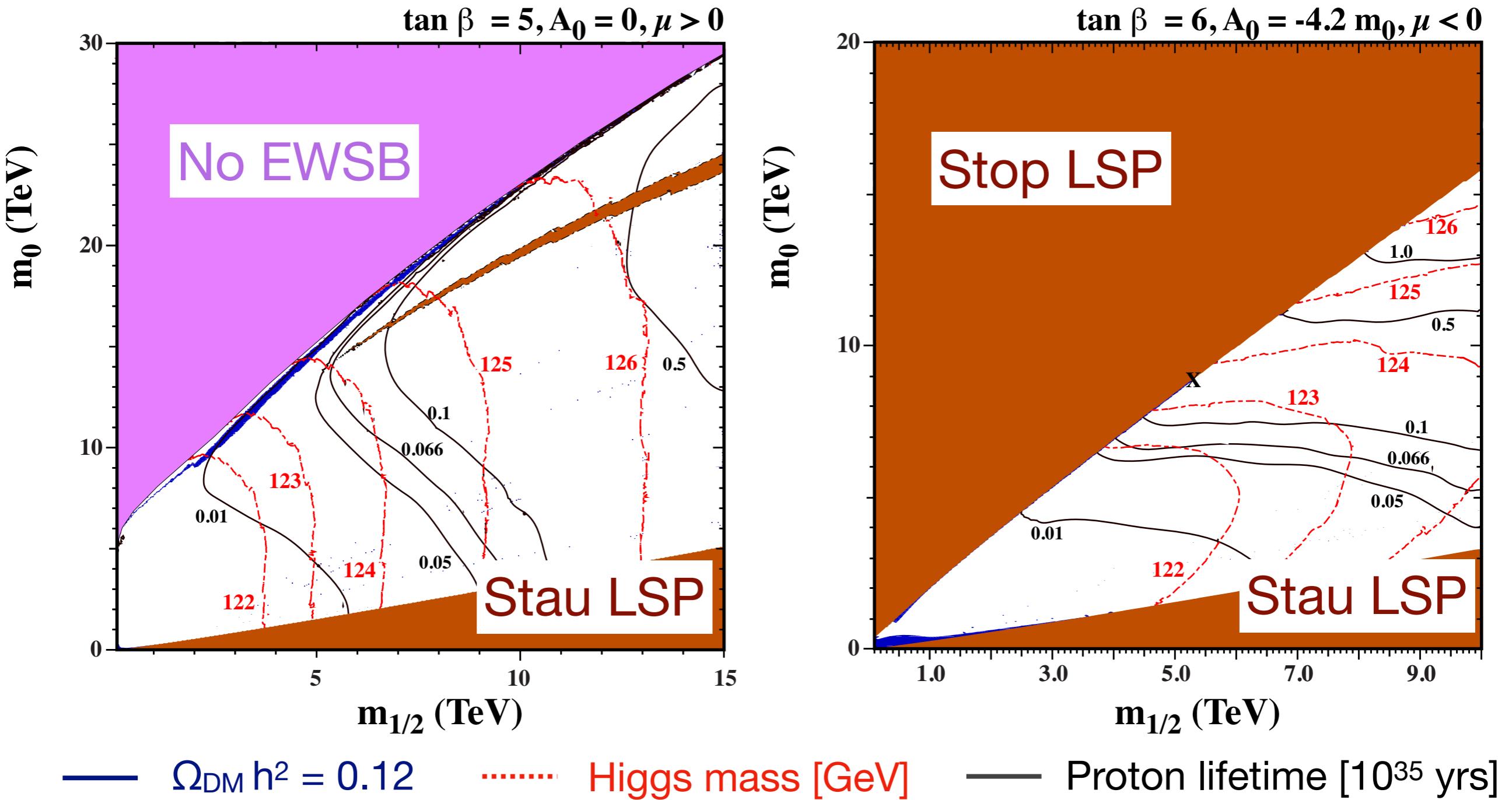
- Traditional benchmark model
- Impose **universality conditions** at the GUT scale.

### Input parameters

$$m_0, \ m_{1/2}, \ A_0, \ \tan\beta, \ \text{sign}(\mu)$$

Soft parameters at low energies are obtained by using renormalization group equations.

# DM in CMSSM



Higgsino-like DM ( $\sim 1$  TeV)

Bino DM  
(stop/stau coannihilation)

# High-scale SUSY

L. J. Hall, Y. Nomura, S. Shirai (2012)

M. Ibe, S. Matsumoto, T. T. Yanagida (2012)

A. Arvanitaki, N. Craig, S. Dimopoulos, G. Villadoro (2012)

N. Arkani-Hamed, A. Gupta, D. E. Kaplan, N. Weiner, and T. Zorawski (2012)

Suppose that the SUSY-breaking field is not a singlet:

Gravitino



Scalar Particles



Higgsinos



Gauginos



Gluino



Bino



Wino

Higgsinos can be light if there is an additional symmetry.

Gaugino masses are induced at loop level.

e.g.) Anomaly mediation

L. Randall and R. Sundrum (1998)

G. F. Giudice, M. A. Luty, H. Murayama, and R. Rattazzi (1998)

# High-scale SUSY

L. J. Hall, Y. Nomura, S. Shirai (2012)

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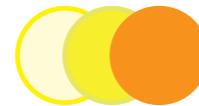
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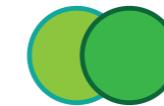
Gravitino



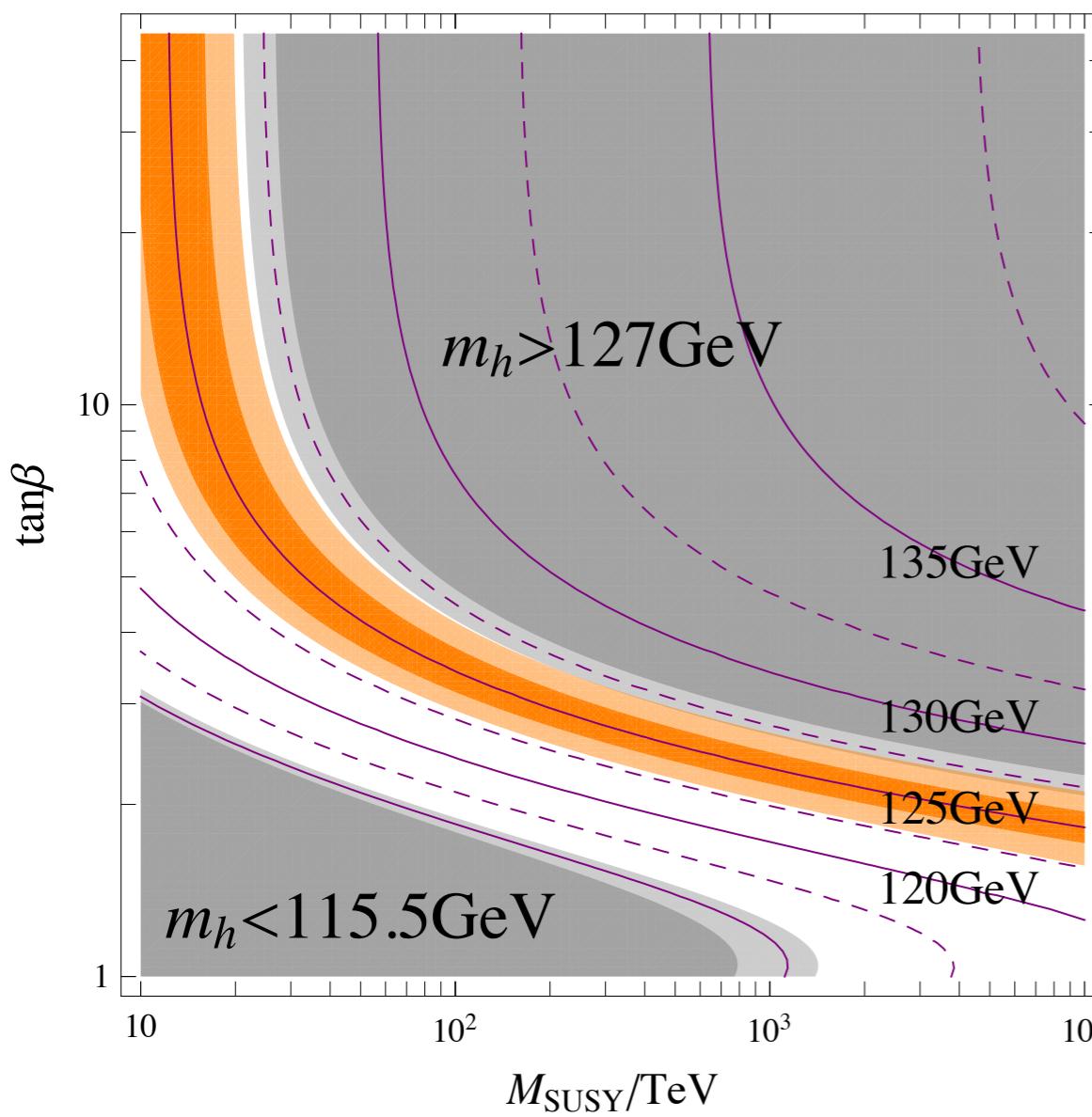
Scalar Particles



Higgsinos



$O(10^{(2-5)})$  TeV



$O(1)$  TeV

$m_h = 125 \text{ GeV}$

High SUSY-breaking scale.

M. Ibe, S. Matsumoto, T. T. Yanagida (2012).

# High-scale SUSY

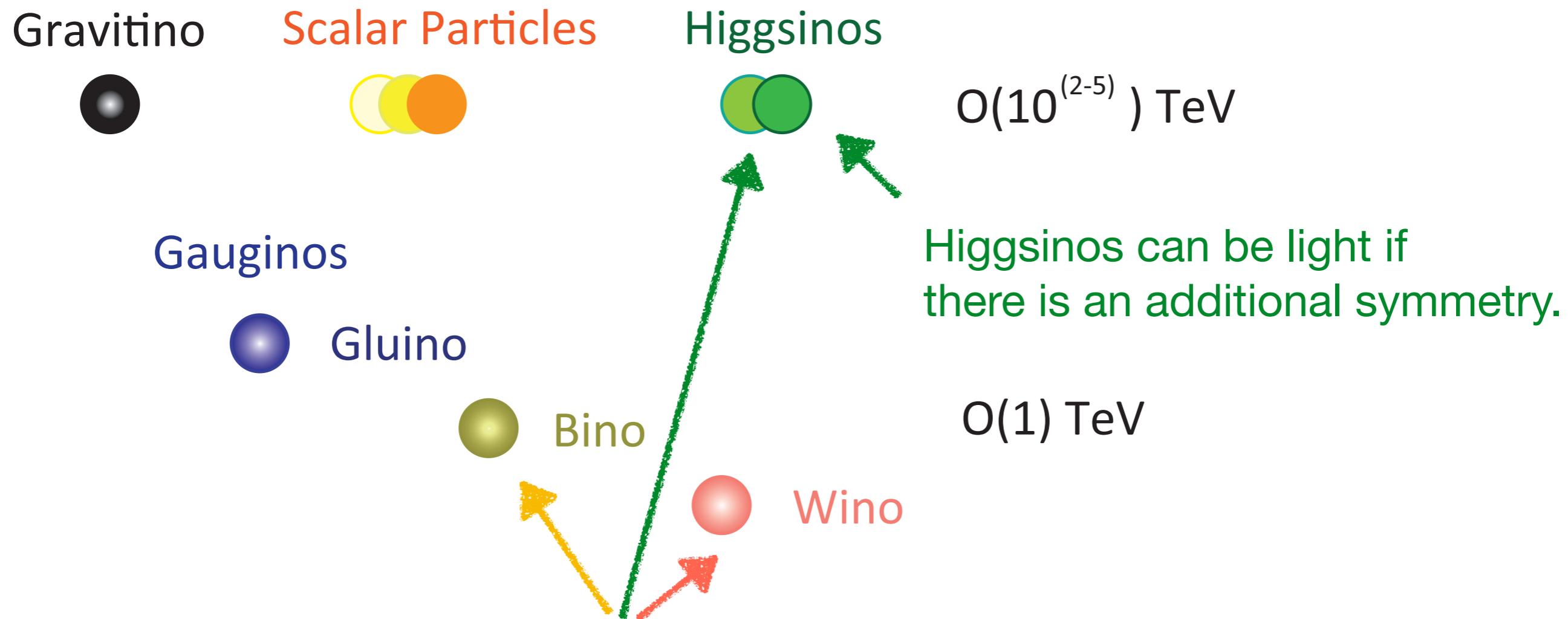
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N. Arkani-Hamed, A. Gupta, D. E. Kaplan, N. Weiner, and T. Zorawski (2012)

Suppose that the SUSY-breaking field is not a singlet:



Dark matter candidates in this setup.

# DM candidates in High-scale SUSY

## WIMP DM candidates

- ▶ **Wino** [3 TeV; anomaly mediation]
- ▶ **Higgsino** [1 TeV]
- ▶ **Bino** [with coannihilation; bino-wino/bino-gluino]

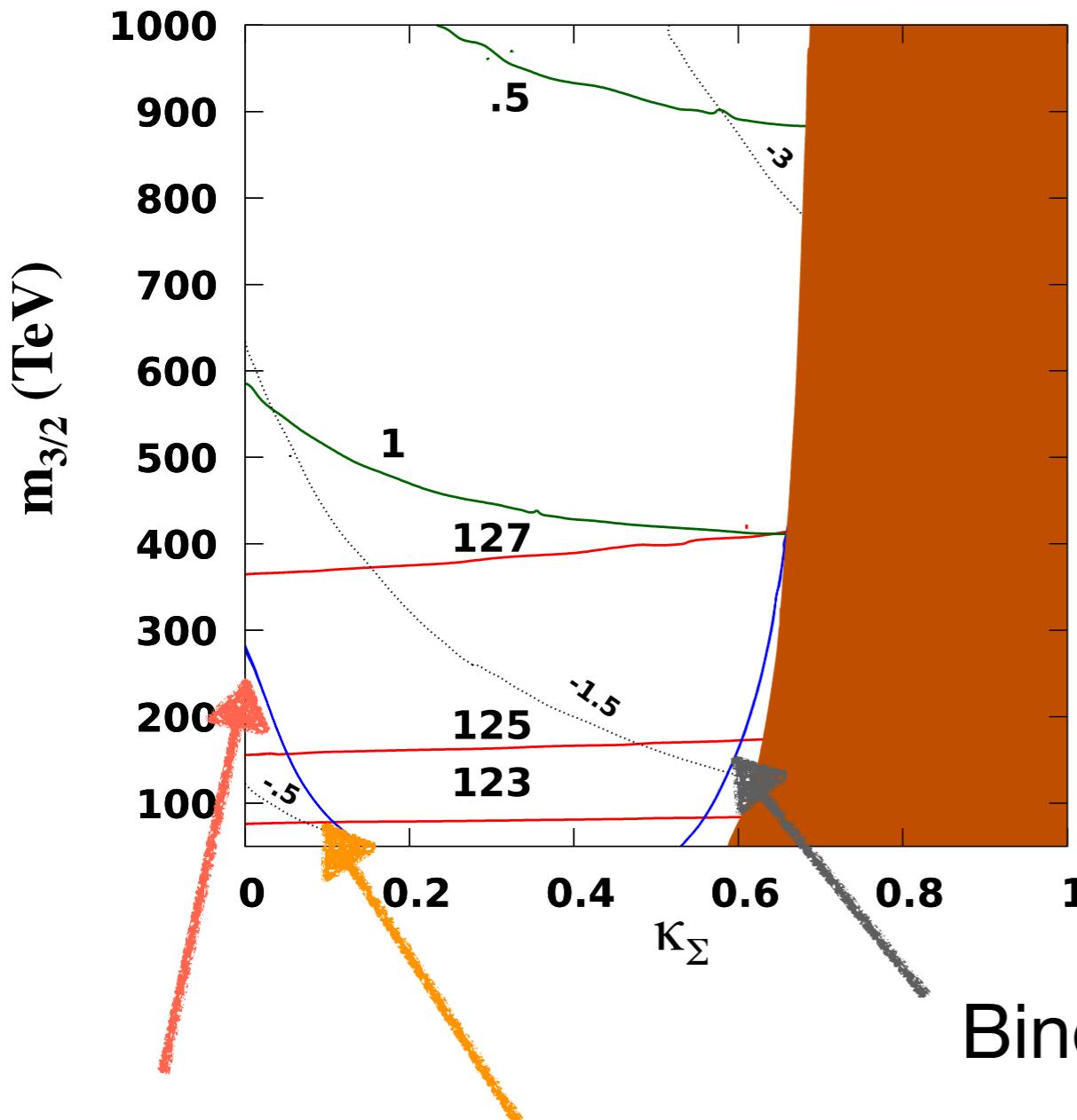
Which of them can actually be realized?

→ Depends on UV physics.

# An example

Parameter space in SU(5) SuperGUT PGM.

$M_{in} = 10^{18}$  GeV,  $\tan \beta = 3.5$ ,  $\lambda = 1$ ,  $\lambda' = 1$ ,  $\mu < 0$



Wino DM

Bino-wino coannihilation

Bino-gluino coannihilation

Gaugino mass contribution

Anomaly mediation  
+ GUT threshold corrections.

with

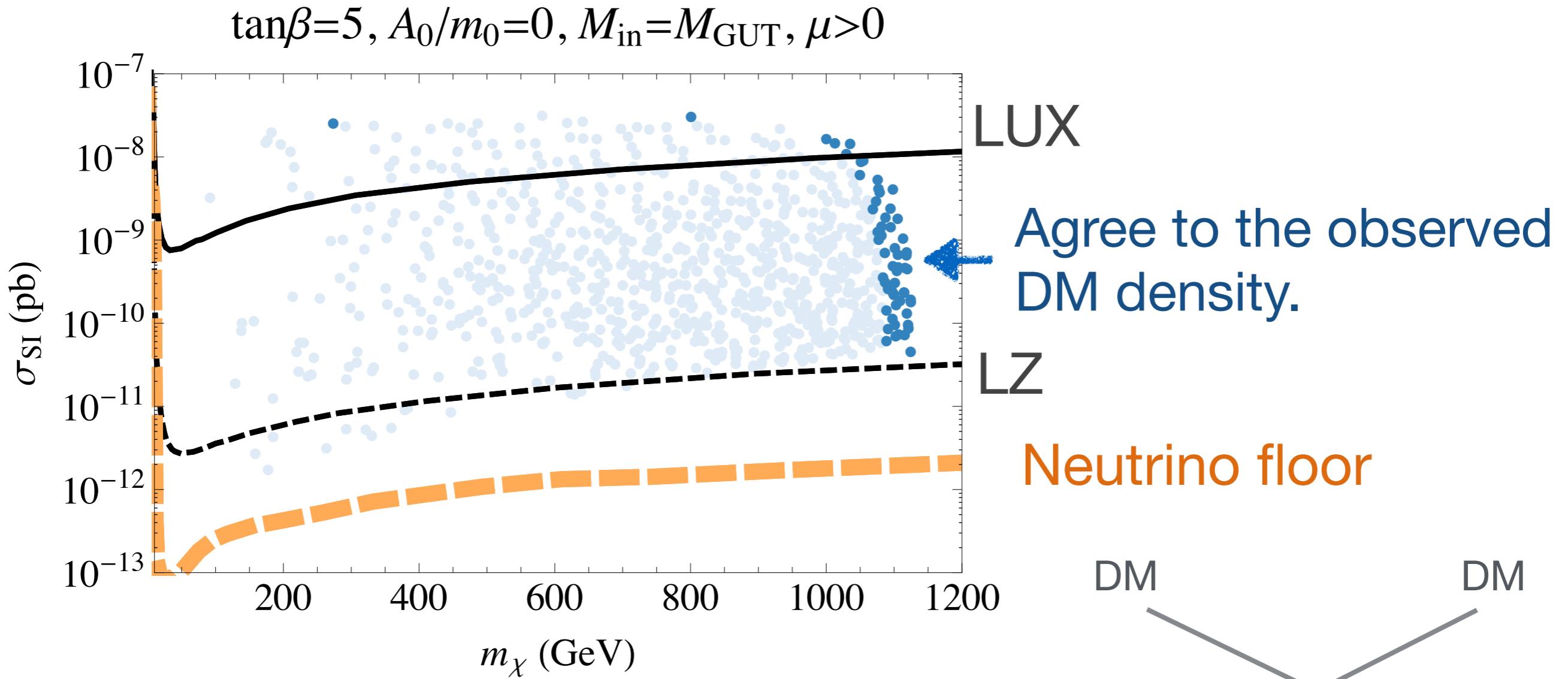
$$\frac{\kappa_\Sigma}{\sqrt{3}M_P}(Z + Z^*)|\Sigma|^2$$

# Summary of DM in SUSY models

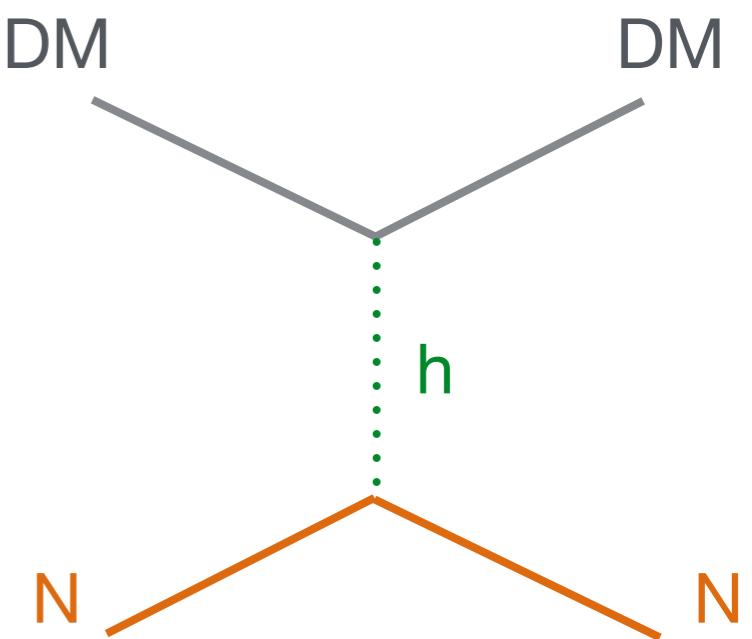
- CMSSM etc.
  - ▶ Higgsino-like DM [ $\sim 1$  TeV]
  - ▶ Bino-stop/stau coannihilation
- High-scale SUSY
  - ▶ Wino [3 TeV]
  - ▶ Higgsino [1 TeV]
  - ▶ Bino-gluino/wino coannihilation

How can we probe these scenarios??

# Higgsino-like LSP in CMSSM



Can be probed in future direct detection experiments

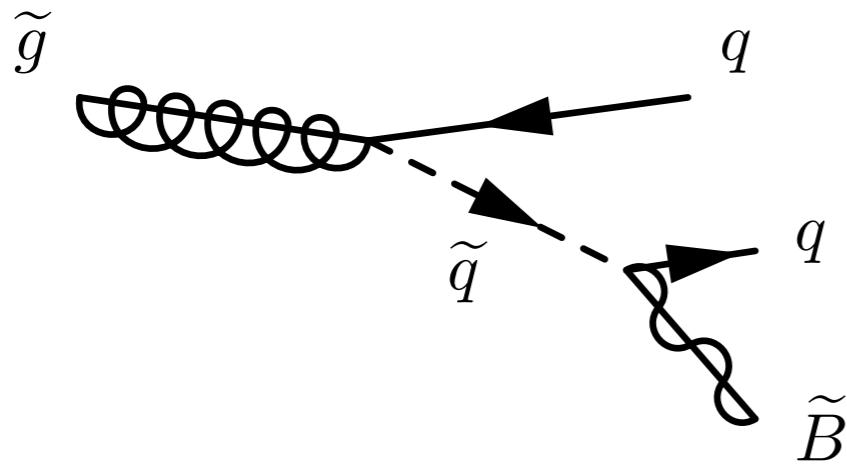


# Bino-gluino/bino-wino coannihilation

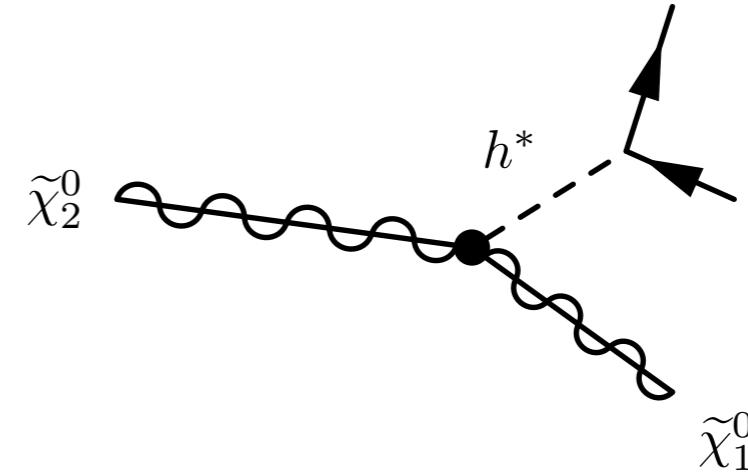
Coannihilation requires NLSP to be degenerate with LSP in mass.

→ Small mass difference makes NLSP long-lived.

## Bino-gluino



## Bino-wino



- $\Delta m = \mathcal{O}(100) \text{ GeV}$
- $c\tau = \mathcal{O}(1) \text{ cm}$

- $\Delta m = \mathcal{O}(10) \text{ GeV}$
- $c\tau = 1 \text{ cm} - 1 \text{ m}$

Can be probed in displaced vertex and/or  $dE/dx$  searches.

# Summary of DM in SUSY models

- CMSSM etc.
  - ▶ Higgsino-like DM [ $\sim 1$  TeV] Direct detection
  - ▶ Bino-stop/stau coannihilation ??
- High-scale SUSY
  - ▶ Wino [3 TeV] To be discussed
  - ▶ Higgsino [1 TeV]
  - ▶ Bino-gluino/wino coannihilation Long-lived particle searches

# **Current status of WIMP DM**

# Quantum numbers of DM

DM should be electrically neutral and colorless.



There still remain many possibilities.

- Spin?

- Real/complex scalar
- Majorana/Dirac fermion
- Vector etc.

- $SU(2)_L \times U(1)_Y$  charge?

$(1, 0), (2, \pm 1/2), (3, 0), (3, \pm 1), (4, \pm 1/2), \dots$

$$Q = T_3 + Y = 0$$

# Quantum numbers of DM

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Singlet scalar DM

# Singlet scalar DM

V. Silveira and A. Zee (1985);  
J. McDonald (1994);  
C. P. Burgess, M. Pospelov, and T. ter Veldhuis (2001).

Just add a neutral scalar field to the Standard Model.

## Lagrangian

$$\mathcal{L}_{\text{int}} = -\frac{1}{2}m^2 S^2 - \frac{1}{2}\lambda_{SH} S^2 |H|^2 - \frac{1}{4!}\lambda_S S^4$$

### ► Stability

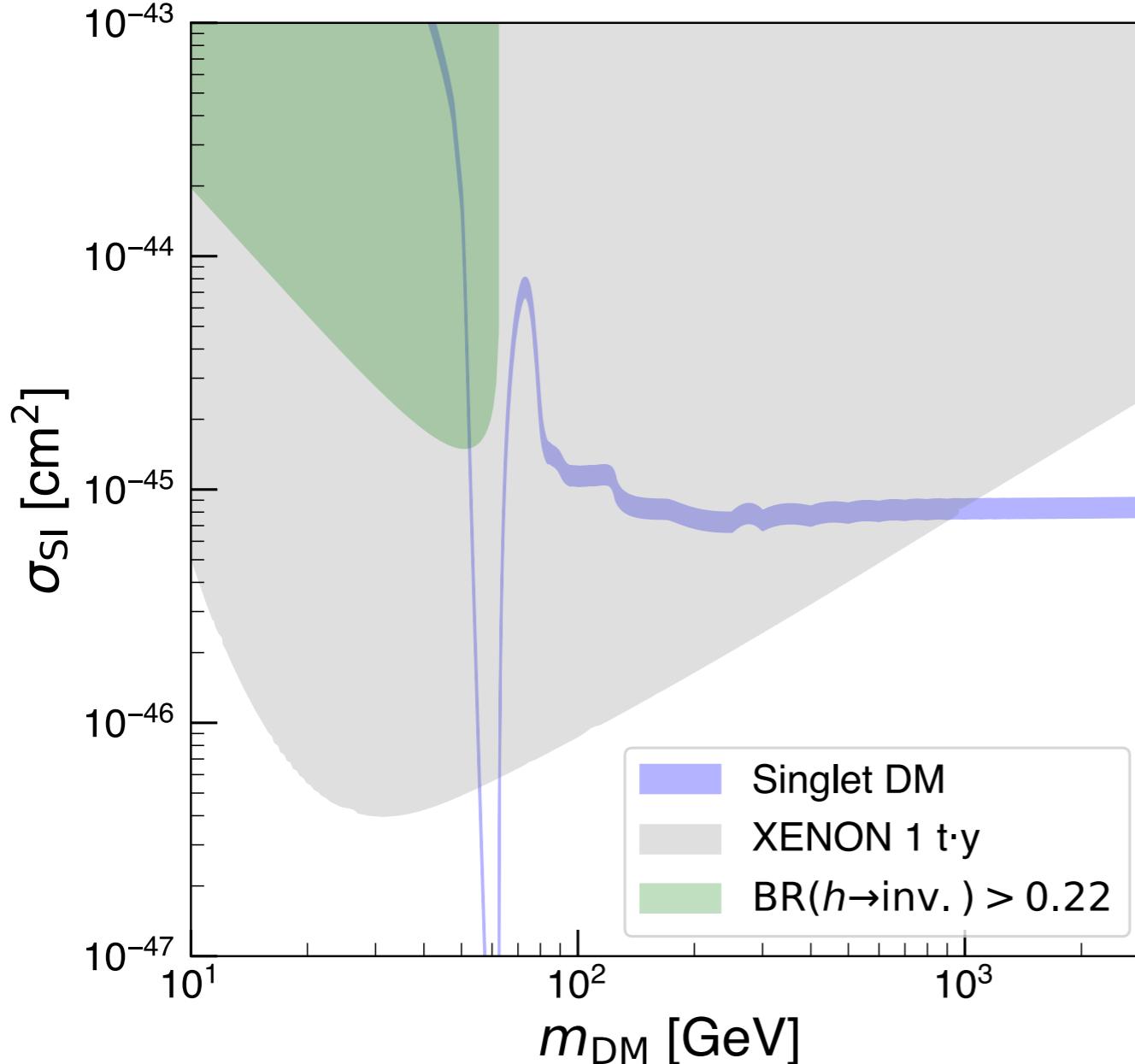
Lagrangian has a  $Z_2$  symmetry:  $S \rightarrow -S$  (odd); SM (even).

### ► Relic abundance

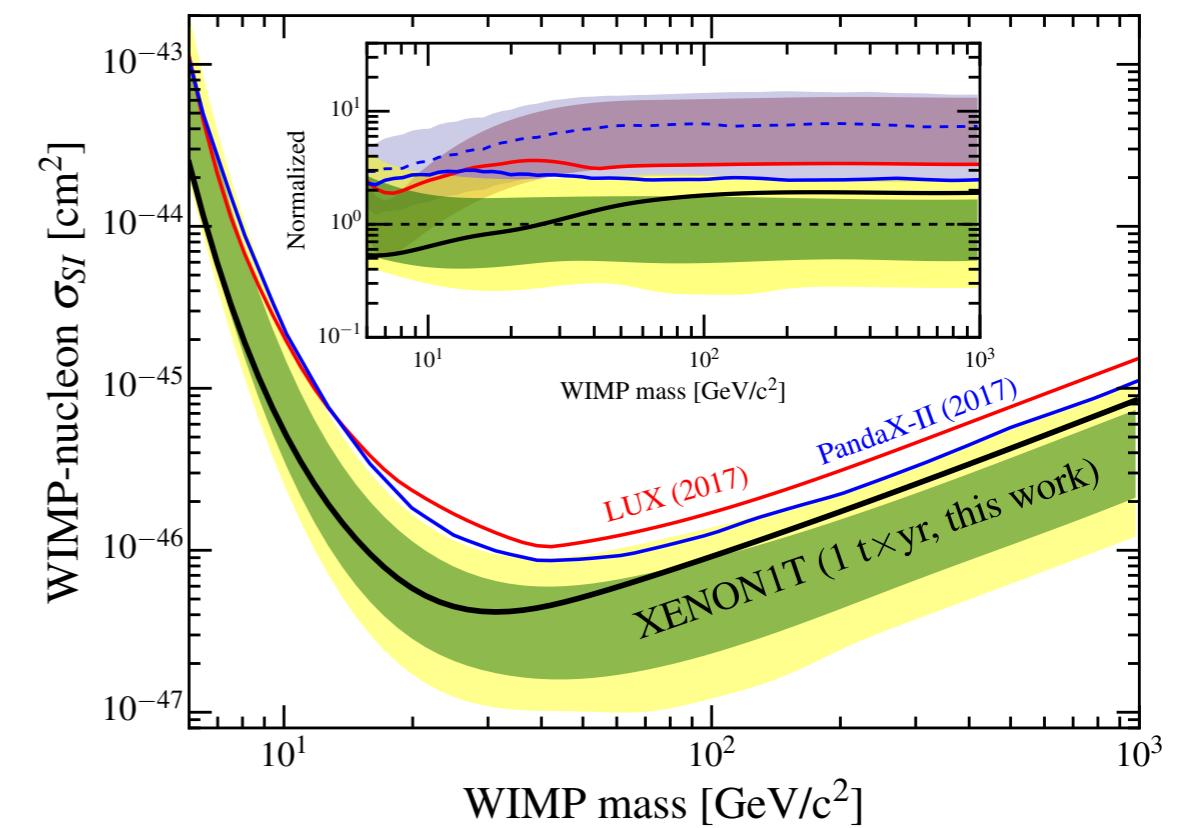
$$\sigma_{\text{ann}} v_{\text{rel}} \simeq \frac{\lambda_{sH}^2}{16\pi m_{\text{DM}}^2} \quad (\text{m}_{\text{DM}} > \text{weak scale})$$

$m_{\text{DM}} \simeq 3.3\lambda_{SH}$  TeV explains the observed DM density.

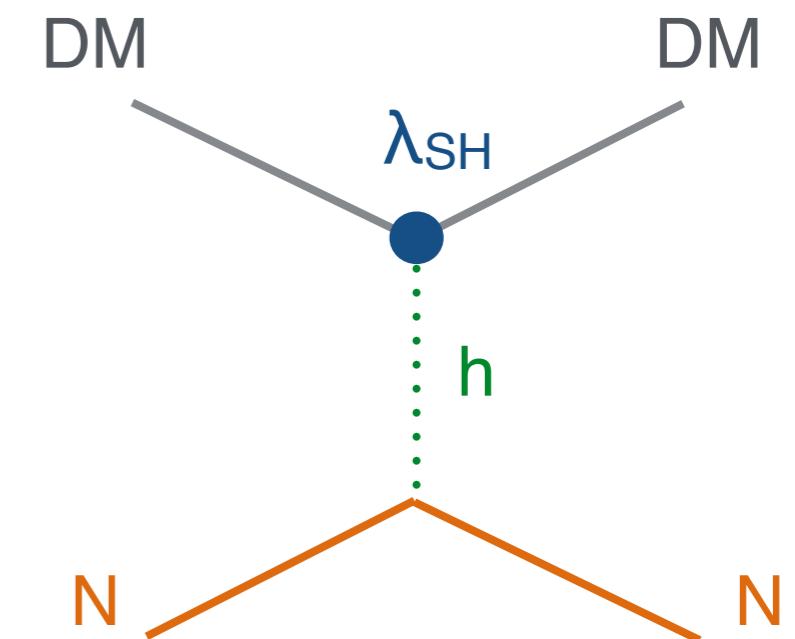
# Singlet scalar DM



Limited up to  $\sim 1$  TeV



XENON Collaboration, arXiv:1805.12562.



# Quantum numbers of DM

DM should be electrically neutral and colorless.



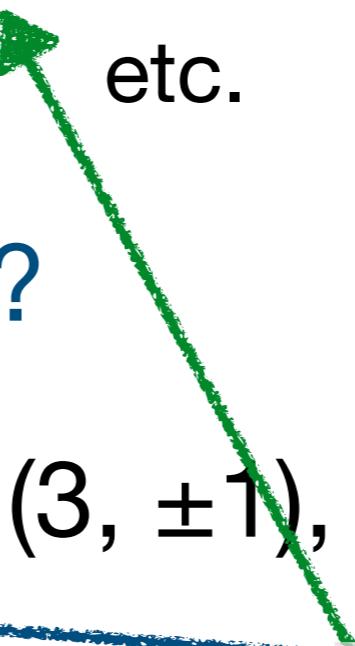
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- $SU(2)_L \times U(1)_Y$  charge?

$(1, 0), (2, \pm 1/2), (3, 0), (3, \pm 1), (4, \pm 1/2), \dots$



Singlet fermion DM

# Singlet fermion DM

## Caveat

Singlet fermion DM **cannot** have direct couplings with the SM particles at the renormalizable level.

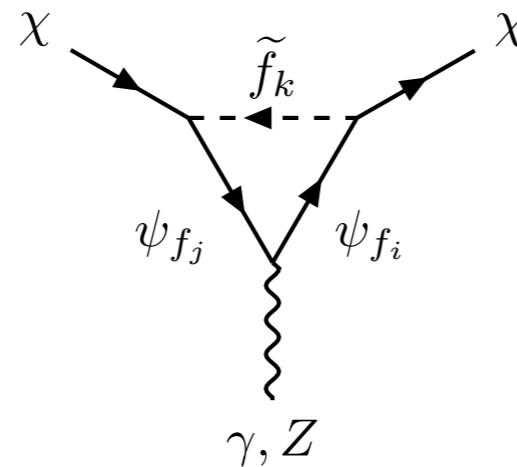
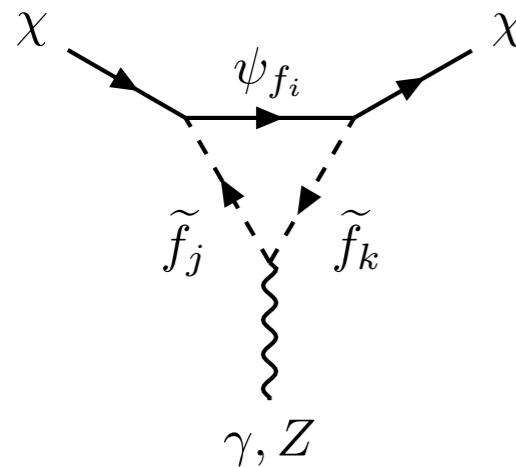


We need to add some extra particles.

Model-by-model analysis required.

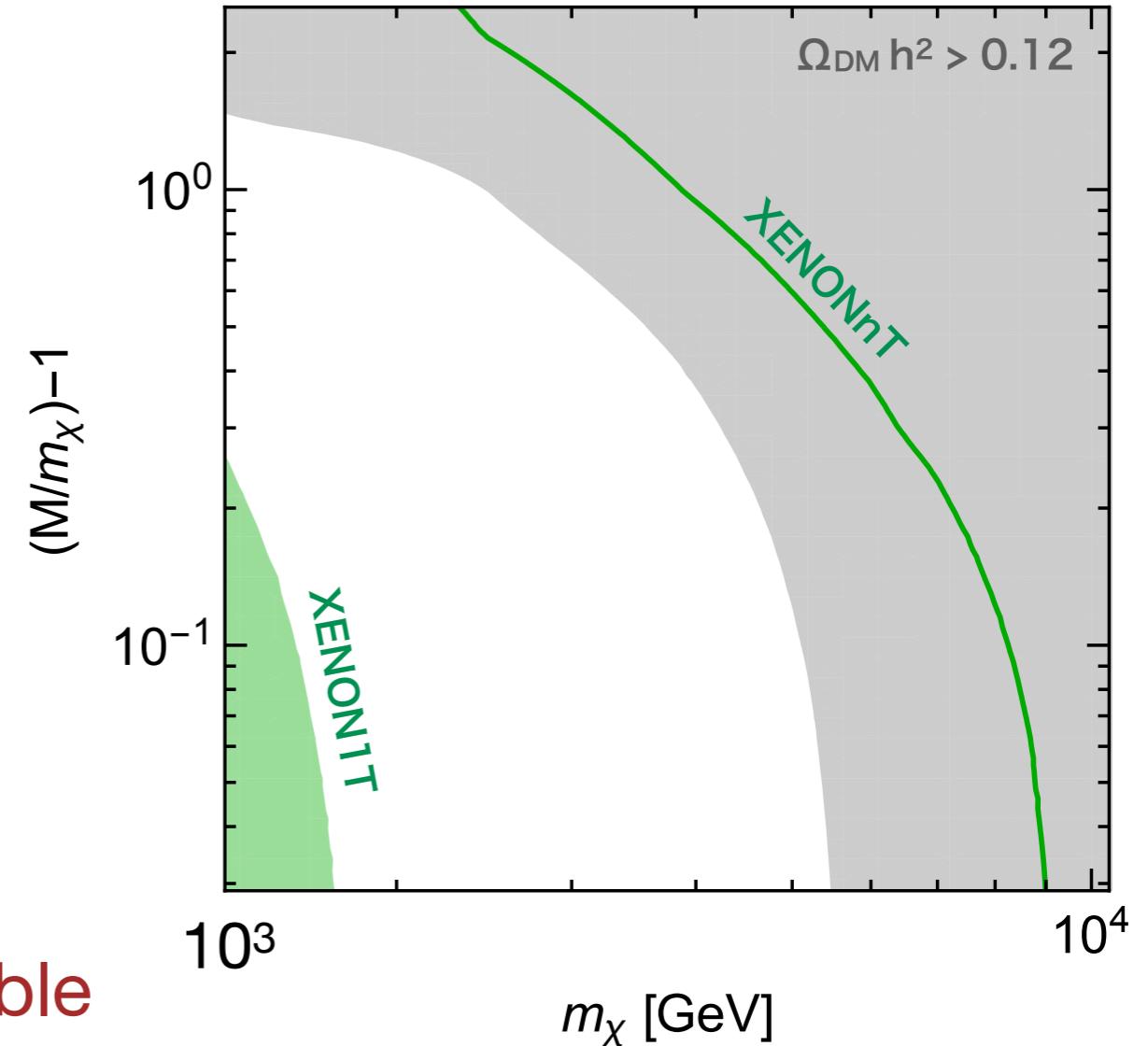
# An example

Consider **singlet Dirac fermion DM** coupling with extra heavy fermion & scalar quarks:



This DM can have MDM/EDM at loop level.

Direct detection possible



- ▶ Can be probed in direct detection experiments.
- ▶ O(1) TeV fermion/scalar quarks can be probed at colliders.

# Quantum numbers of DM

DM should be electrically neutral and colorless.



There still remain many possibilities.

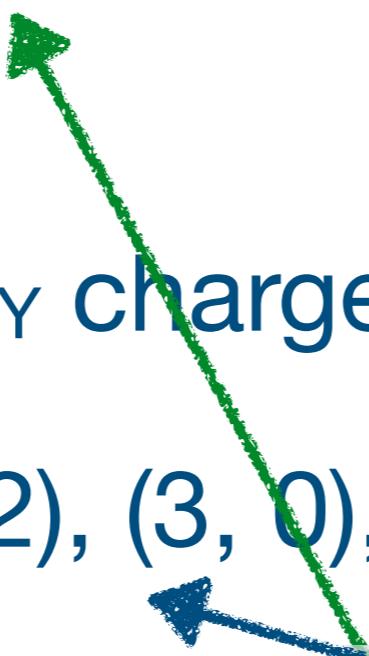
- Spin?

- Real/complex scalar
- Majorana/Dirac fermion
- Vector

etc.

- $SU(2)_L \times U(1)_Y$  charge?

$(1, 0), (2, \pm 1/2), (3, 0), (3, \pm 1), (4, \pm 1/2), \dots$



Electroweak-interacting DM

# Electroweak-Interacting DM

The neutral component of  $SU(2)_L$  n-tuplet, hypercharge  $Y$  is regarded as a DM candidate.

## Examples:

- $n = 2, Y = 1/2$  (higgsino)
- $n = 3, Y = 0$  (wino)
- $n = 5, Y = 0$  (Minimal Dark Matter)

## Interactions

$$\begin{aligned}\mathcal{L}_{\text{int}} = & \frac{g_2}{4} \sqrt{n^2 - (2Y - 1)^2} \overline{\chi^+} W^+ \chi^0 + \frac{g_2}{4} \sqrt{n^2 - (2Y + 1)^2} \overline{\chi^0} W^+ \chi^- + \text{h.c.} \\ & + ig_Z Y \overline{\chi^0} Z \eta^0.\end{aligned}$$

The DM phenomenology is (almost) completely determined by the gauge interactions.

For scalar DM cases, the DM-Higgs couplings also exist.

# Electroweak-Interacting DM

Quantum numbers			DM could decay into	DM mass in TeV	$m_{\text{DM}^\pm} - m_{\text{DM}}$ in MeV	Finite naturalness bound in TeV	$\sigma_{\text{SI}}$ in $10^{-46} \text{ cm}^2$
SU(2) <sub>L</sub>	U(1) <sub>Y</sub>	Spin					
2	1/2	0	<i>EL</i>	0.54	350	$0.4 \times \sqrt{\Delta}$	$(0.4 \pm 0.6) 10^{-3}$
2	1/2	1/2	<i>EH</i>	1.1	341	$1.9 \times \sqrt{\Delta}$	$(0.25 \pm 0.56) 10^{-3}$
3	0	0	<i>HH*</i>	$2.0 \rightarrow 2.5$	166	$0.22 \times \sqrt{\Delta}$	$0.12 \pm 0.03$
3	0	1/2	<i>LH</i>	$2.4 \rightarrow 2.7$	166	$1.0 \times \sqrt{\Delta}$	$0.12 \pm 0.03$
3	1	0	<i>HH, LL</i>	$1.6 \rightarrow ?$	540	$0.22 \times \sqrt{\Delta}$	$(1.3 \pm 1.1) 10^{-2}$
3	1	1/2	<i>LH</i>	$1.9 \rightarrow ?$	526	$1.0 \times \sqrt{\Delta}$	$(1.3 \pm 1.1) 10^{-2}$
4	1/2	0	<i>HHH*</i>	$2.4 \rightarrow ?$	353	$0.14 \times \sqrt{\Delta}$	$0.27 \pm 0.08$
4	1/2	1/2	<i>(LHH*)</i>	$2.4 \rightarrow ?$	347	$0.6 \times \sqrt{\Delta}$	$0.27 \pm 0.08$
4	3/2	0	<i>HHH</i>	$2.9 \rightarrow ?$	729	$0.14 \times \sqrt{\Delta}$	$0.15 \pm 0.07$
4	3/2	1/2	<i>(LHH)</i>	$2.6 \rightarrow ?$	712	$0.6 \times \sqrt{\Delta}$	$0.15 \pm 0.07$
5	0	0	<i>(HHH*H*)</i>	$5.0 \rightarrow 9.4$	166	$0.10 \times \sqrt{\Delta}$	$1.0 \pm 0.2$
5	0	1/2	stable	$4.4 \rightarrow 10$	166	$0.4 \times \sqrt{\Delta}$	$1.0 \pm 0.2$
7	0	0	stable	$8 \rightarrow 25$	166	$0.06 \times \sqrt{\Delta}$	$4 \pm 1$

(→: Sommerfeld enhancement)

## Features

M. Farina, D. Pappadopulo, A. Strumia, JHEP **1308** (2013) 022.

- Relatively **heavy mass** gives correct DM abundance.
- Small mass difference among the multiplet components.

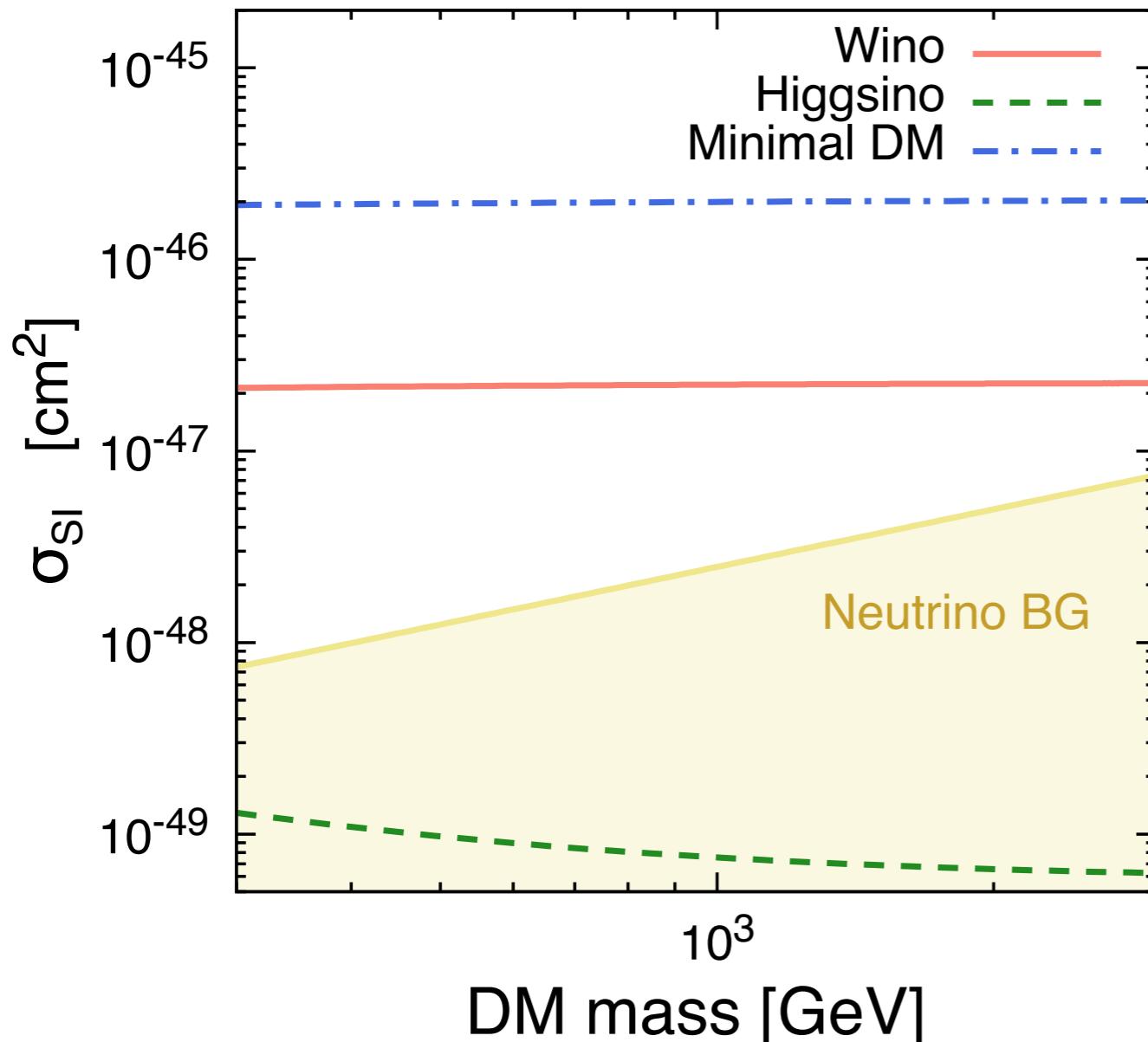
# Electroweak-Interacting DM

These DM candidates are still waiting to be tested.

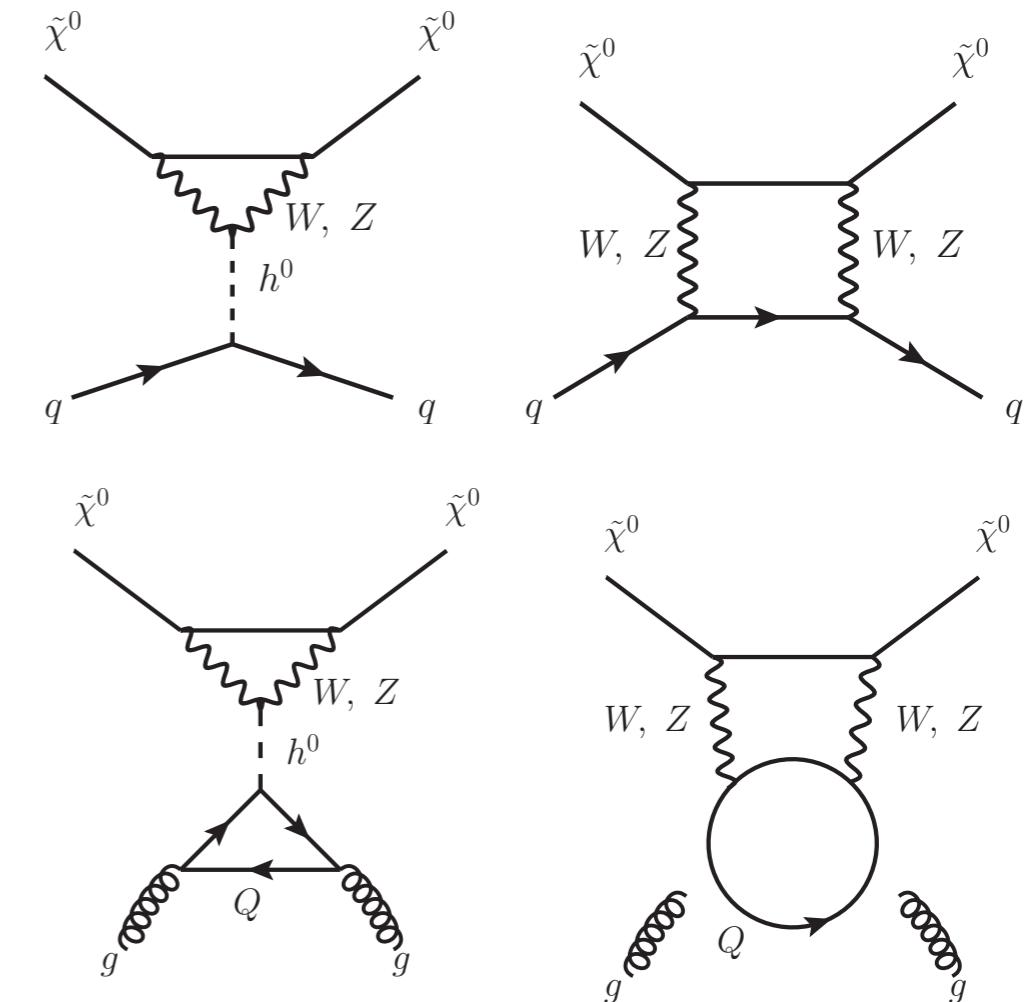
## Search methods

- Indirect searches are promising.  
Large annihilation cross section.
- Collider searches are challenging but doable.
  - ▶ Small production cross section.
  - ▶ Small mass difference.
    - Disappearing track search (+a)
    - Indirect search via quantum corrections.
- Direct searches are also possible.

# Electroweak interacting DM



## Diagrams



- ▶ Triplet (pure wino), Minimal DM can be tested.
- ▶ Doublet (pure higgsino) is hard to probe.

# **Conclusion**

# Message of the talk

- WIMP DM candidates in SUSY models have been narrowed down.
  - ▶ Wino [3 TeV]
  - ▶ Higgsino [1 TeV]
  - ▶ Coannihilation [bino-stop/gluino/wino/stau]
- WIMP paradigm has not been fully tested yet.
- We can explore it in future experiments.

# **Backup**

# Thermal relic scenario (cold DM)

WIMPs were in **thermal equilibrium** with the SM particles in the early Universe.

For  $T \lesssim m_{\text{DM}}$

$$n_{\text{DM}} \simeq \left( \frac{m_{\text{DM}} T}{2\pi} \right)^{\frac{3}{2}} e^{-\frac{m_{\text{DM}}}{T}}$$

DM number rapidly decreases.

→ Annihilation rate also rapidly decreases!

Annihilation process freezes out when

$$n_{\text{DM}}(T_{\text{FO}}) \cdot \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \simeq H(T_{\text{FO}}) \quad \rightarrow$$

$$T_{\text{FO}} \simeq \frac{m_{\text{DM}}}{25}$$



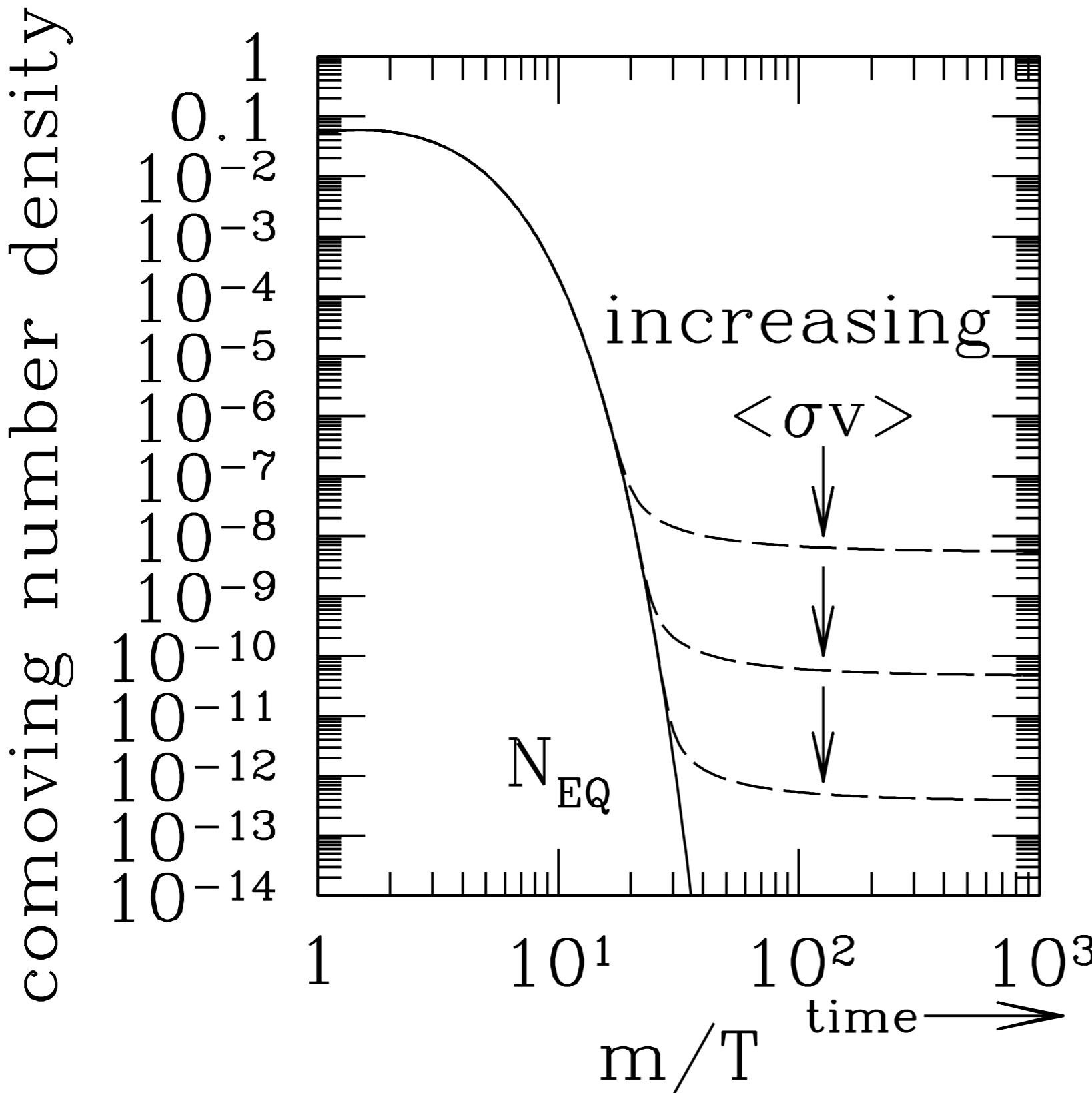
Annihilation rate



Hubble expansion rate

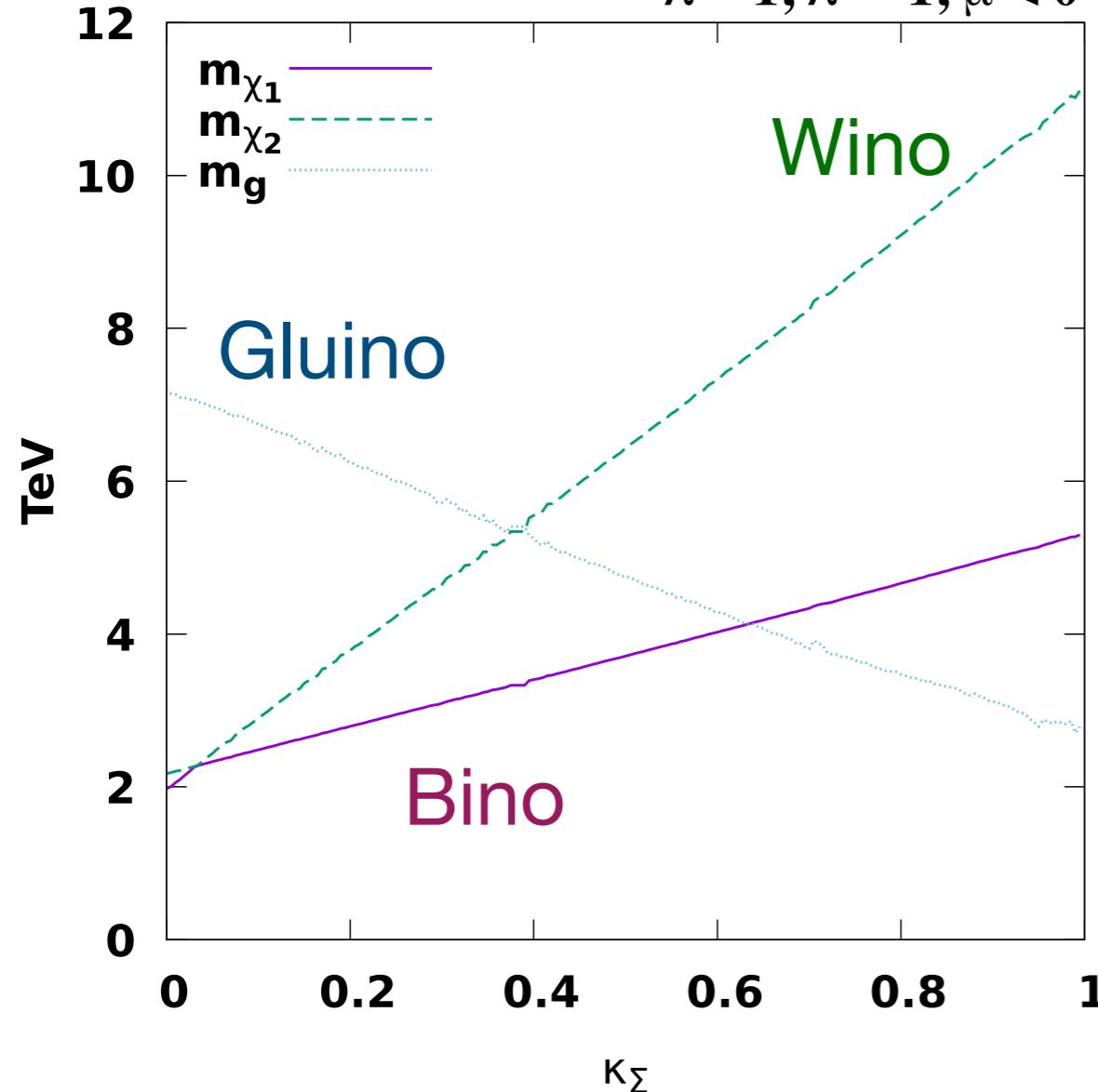
Cold DM

# Thermal relic scenario (cold DM)



# Gaugino masses in SuperGUT PGM

$M_{in} = 10^{18}$  GeV,  $\tan \beta = 3.5$ ,  $m_{3/2} = 200$  TeV,  
 $\lambda = 1, \lambda' = 1, \mu < 0$

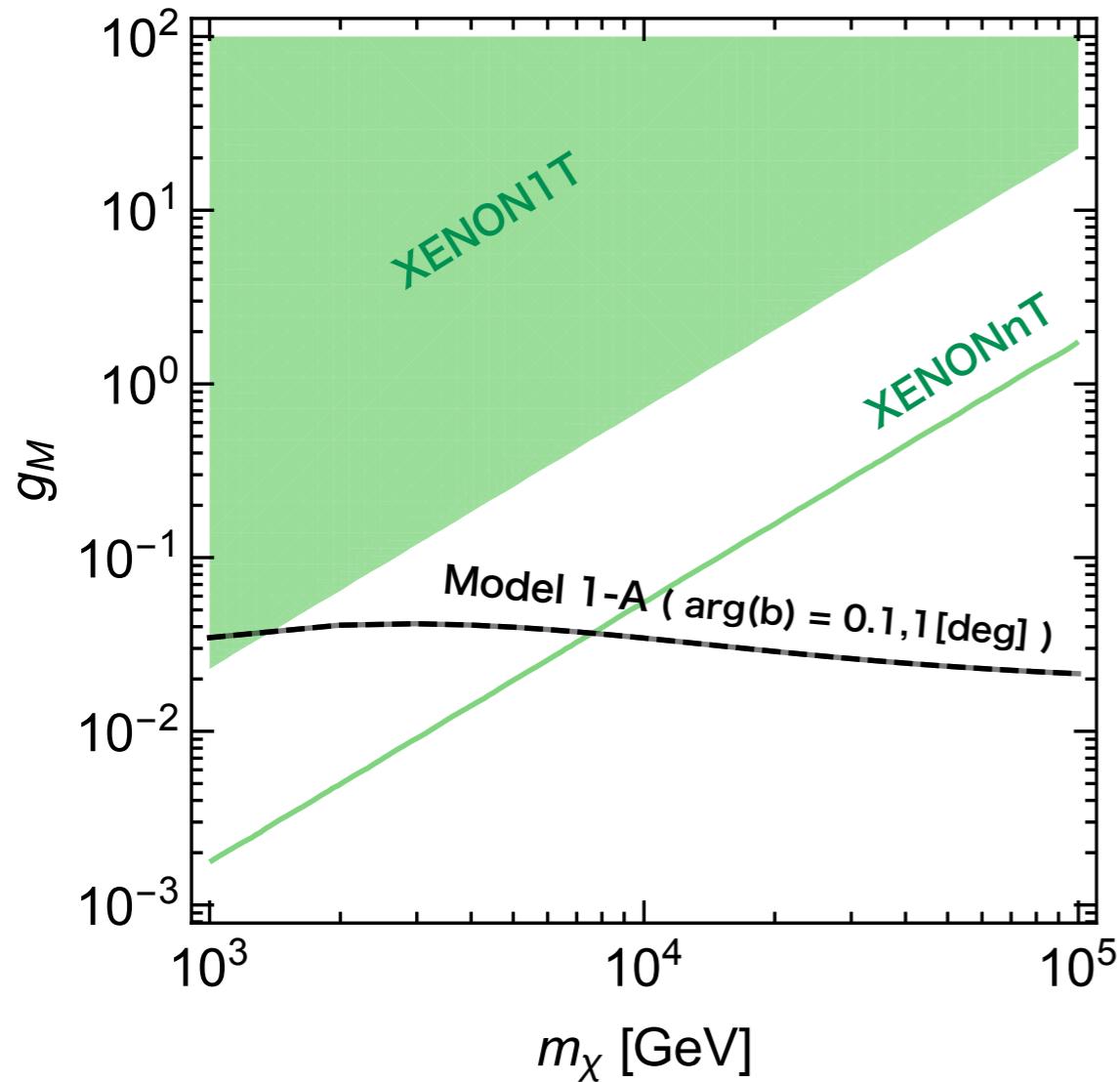


$$\frac{\kappa_\Sigma}{\sqrt{3}M_P}(Z + Z^*)|\Sigma|^2$$

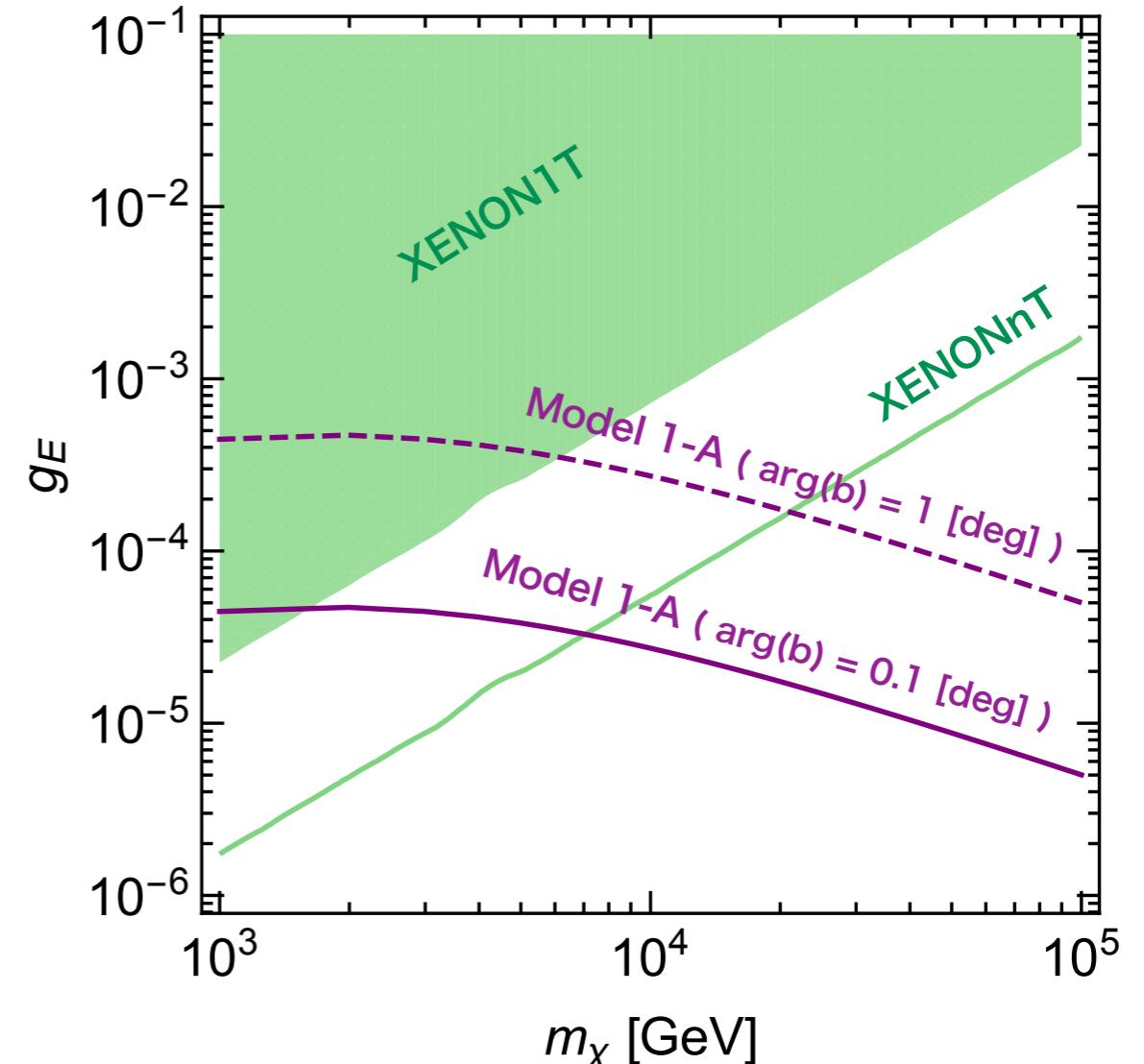
→  $\Delta A_{\lambda'} = 3\kappa_\Sigma m_{3/2},$   
 $\Delta B_\Sigma = 2\kappa_\Sigma m_{3/2}$

# Singlet Dirac Fermion DM

## Magnetic dipole moment



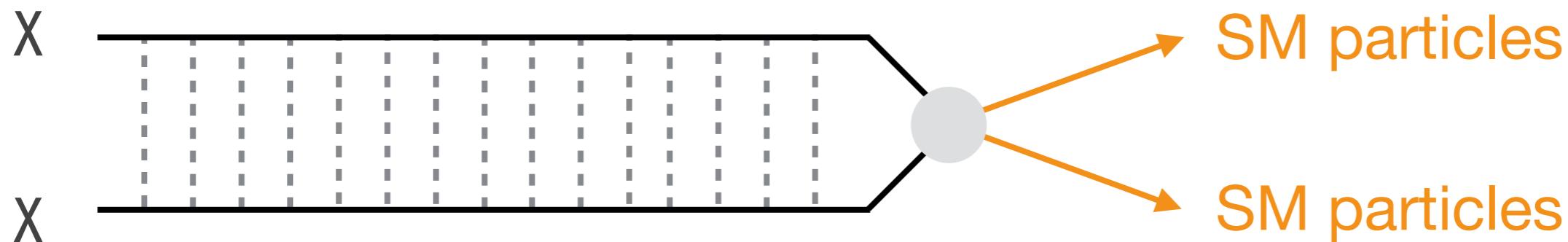
## Electric dipole moment



# Sommerfeld effects

J. Hisano, S. Matsumoto, and M. M. Nojiri, Phys. Rev. Lett. **92**, 031303 (2004).

Electroweak-interacting DM has **self-interactions** via EW interactions.



Incoming wave-functions deviate from plane waves due to **long-distance self-interactions**.



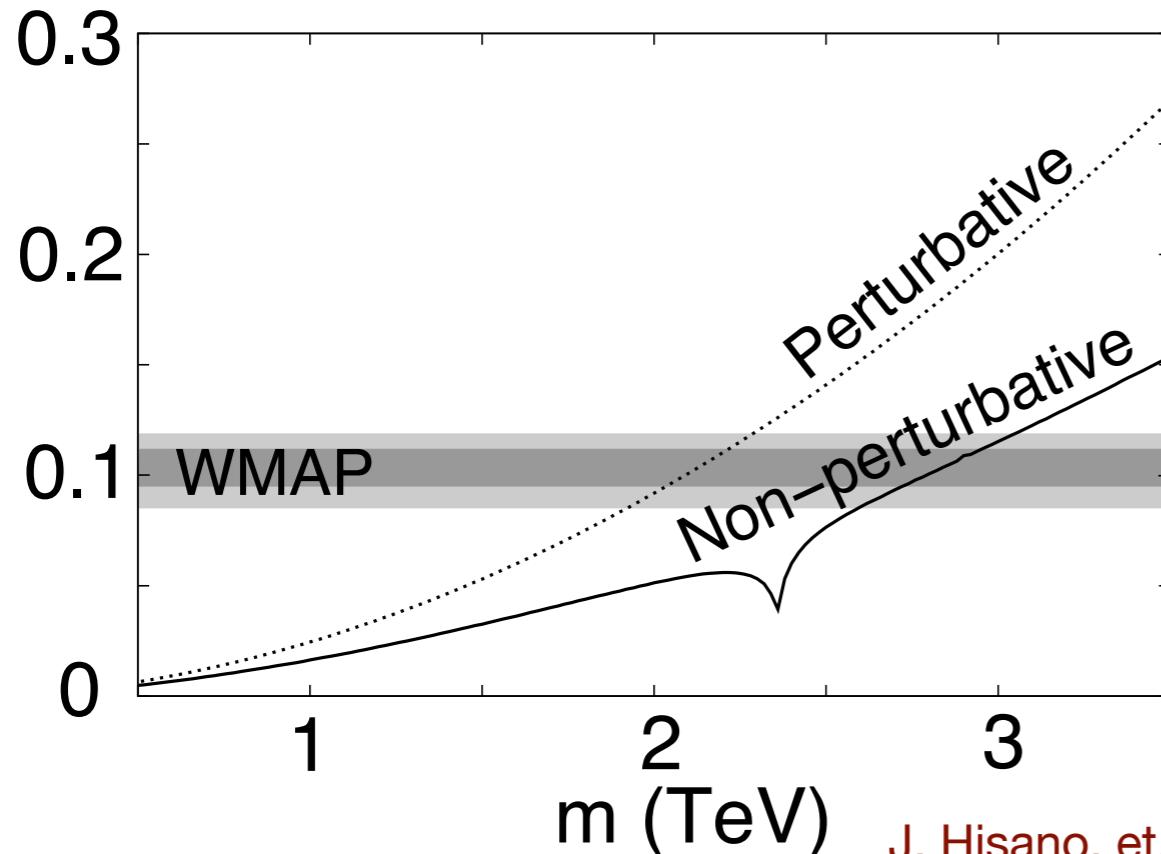
**Sommerfeld effect**

This effect becomes important when the interaction range becomes longer than the Bohr radius of the two-body system.

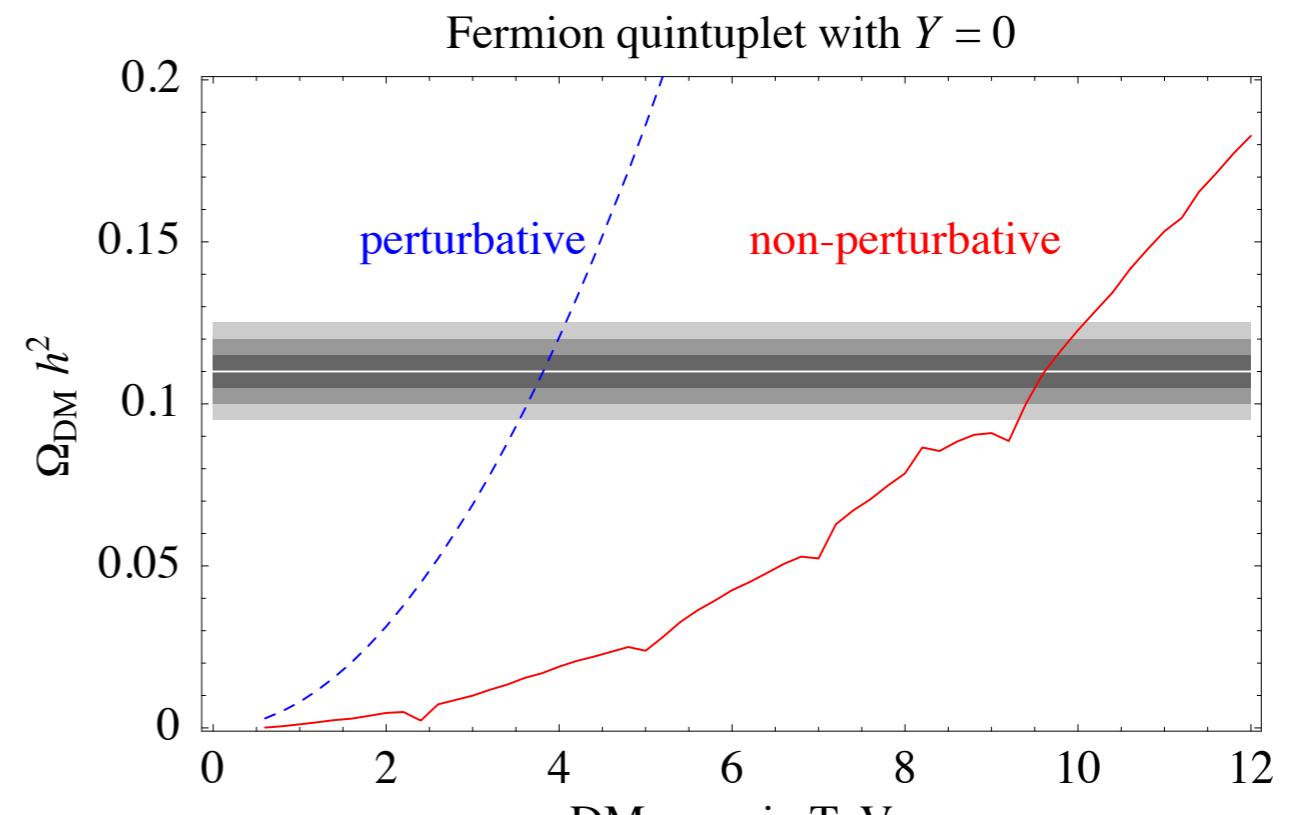
$$\frac{1}{m_W} \gtrsim \frac{1}{\alpha_2 m_{\text{DM}}}$$

# Sommerfeld effects

## Triplet



## Quintuplet



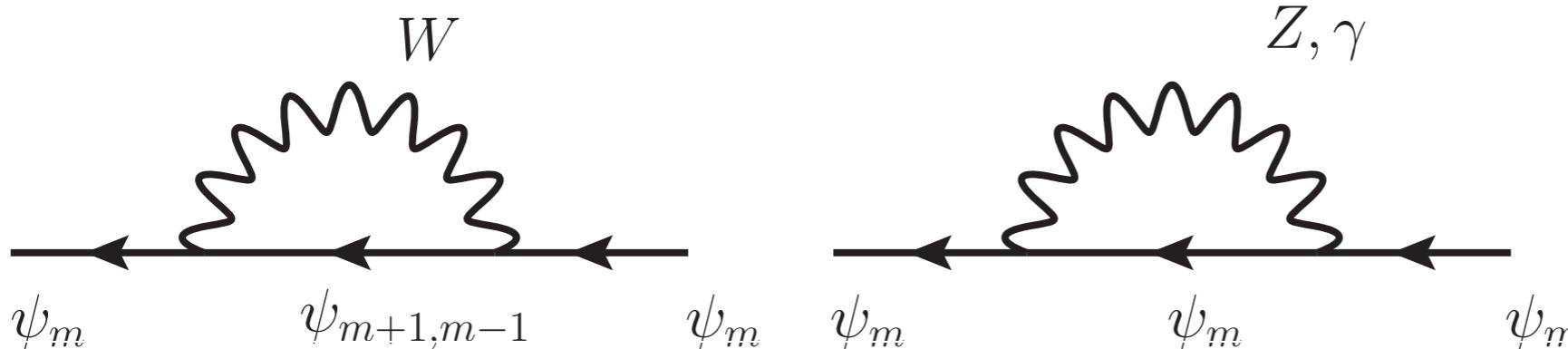
Sommerfeld effect significantly enhances annihilation cross sections.

→ A heavier mass is favored in terms of thermal relic.

In order to make a precise prediction for the DM mass, we need to take this effect into account.

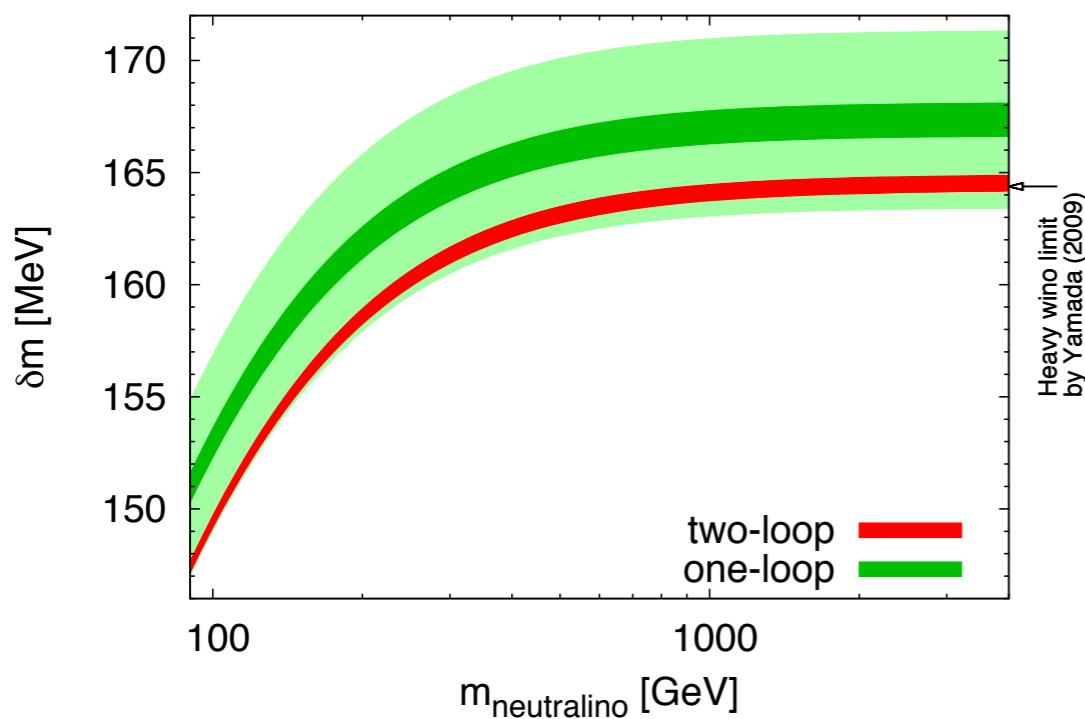
# Mass splitting

Charged-neutral mass splitting of a wino or Higgsino is generated via IR radiative corrections by EW gauge boson loops.



$$\Delta M \simeq \alpha_2 m_W \sin^2 \frac{\theta_W}{2} + \alpha_2 Y m_W \left( \frac{1}{\cos \theta_W} - 1 \right)$$

O(100) MeV.



Non-decoupling effect  
Two-loop calculation (wino,  $Y = 0$ )

$$\Delta M \simeq 165 \text{ MeV}$$

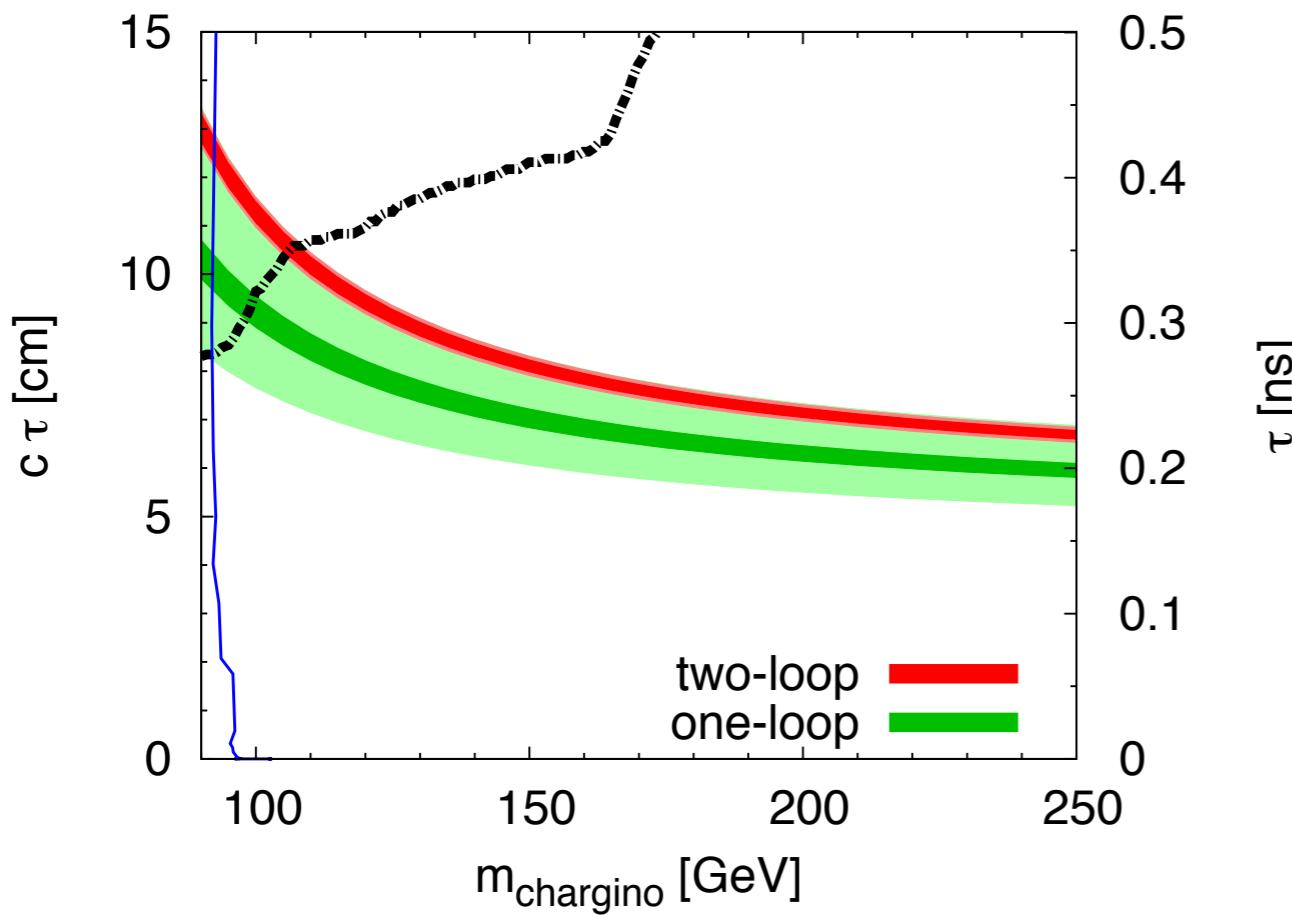
# Wino lifetime

Due to the small mass splitting, wino becomes rather **long-lived**.

Main decay channel:  $\chi^\pm \rightarrow \chi^0 + \pi^\pm$

Branching fraction for the leptonic decay modes (three-body decay) is a few %.

$$\Gamma(\chi^\pm \rightarrow \chi^0 + \pi^\pm) = \frac{4G_F^2 V_{ud}^2 f_\pi^2}{\pi} \Delta M^3 \left(1 - \frac{m_\pi^2}{\Delta M^2}\right)^{\frac{1}{2}}$$

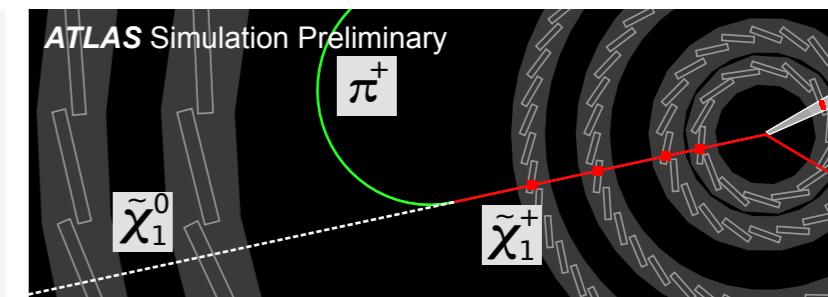
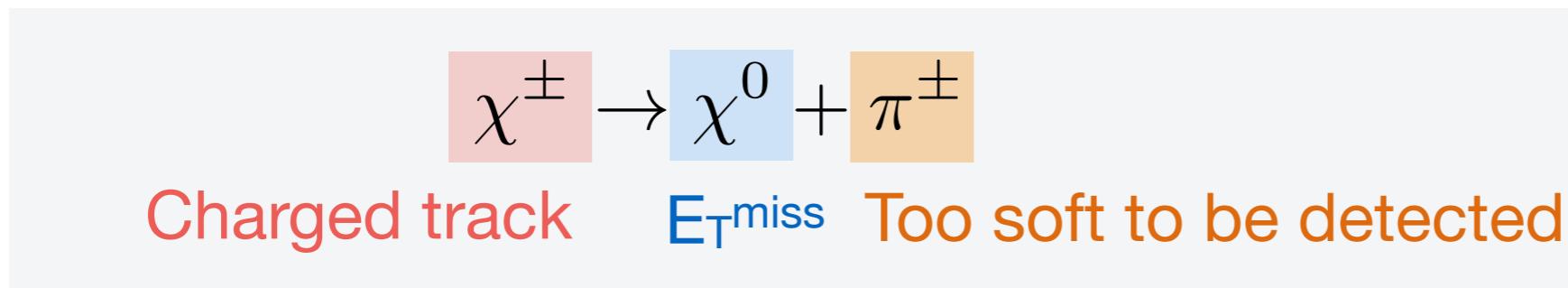


$$\begin{aligned}\tau &\simeq 0.2 \text{ ns} \\ c\tau &\simeq 6 \text{ cm}\end{aligned}$$

# Disappearing track searches

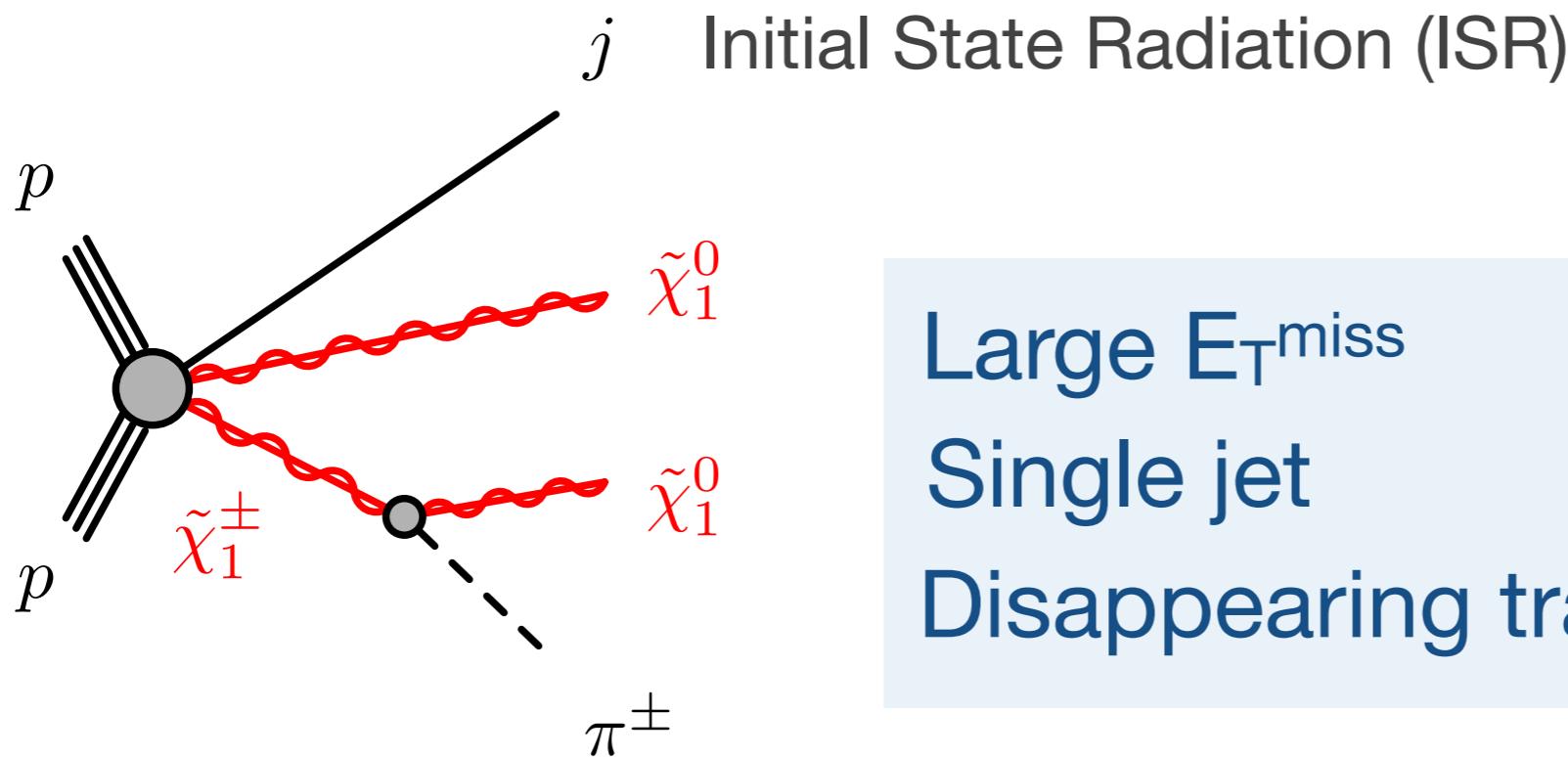
A charged wino with a decay length of  $O(1)$  cm leaves a **disappearing track** in detectors.

J. L. Feng, T. Moroi, L. Randall, M. Strassler, S. F. Su (1999);  
M. Ibe, T. Moroi, T. T. Yanagida (2006), etc...



Requiring this signature, we can reduce SM BG significantly.

## Signal topology

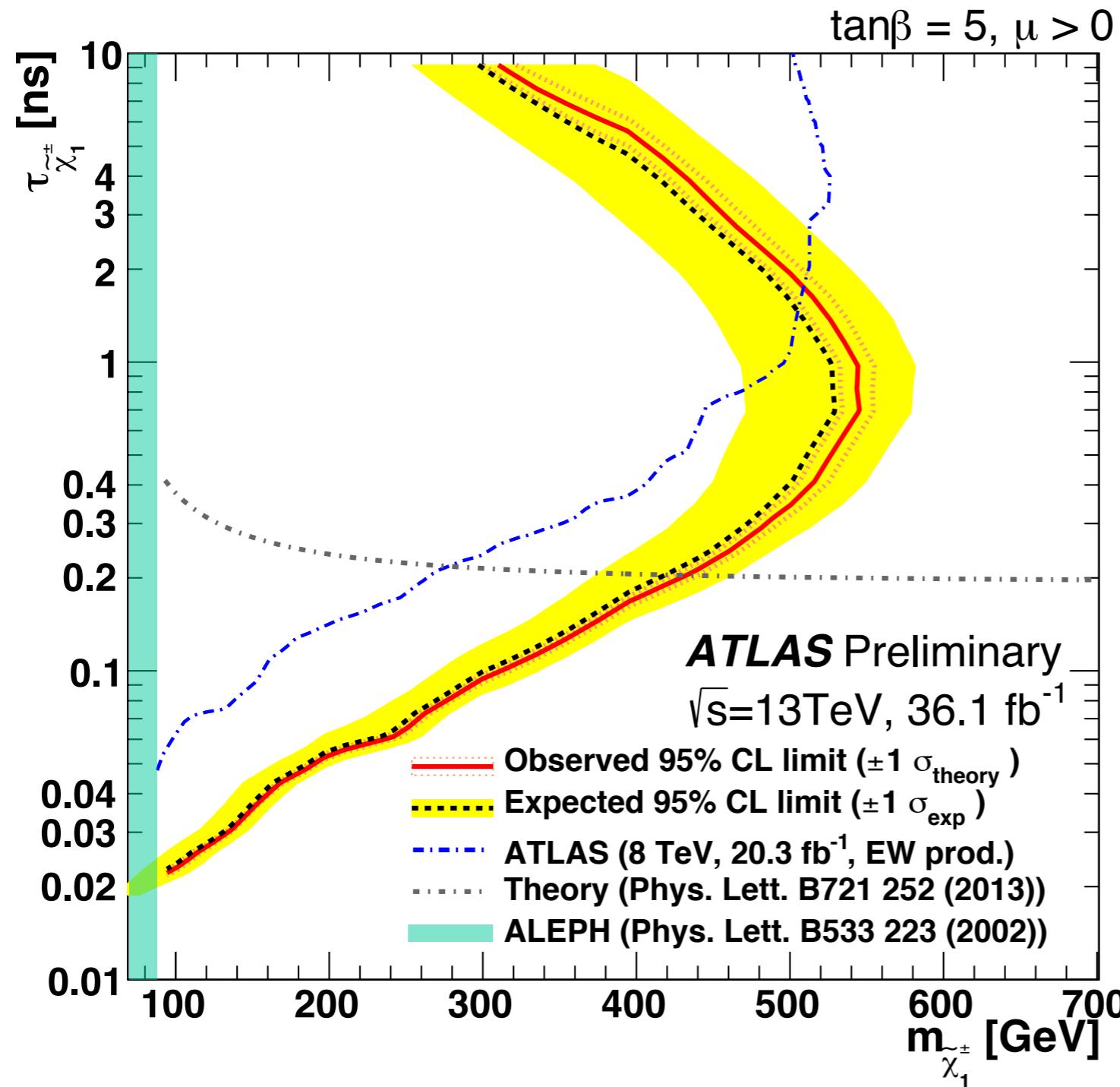


Large  $E_T^{\text{miss}}$   
Single jet  
Disappearing track

## Ryu Sawada's talk

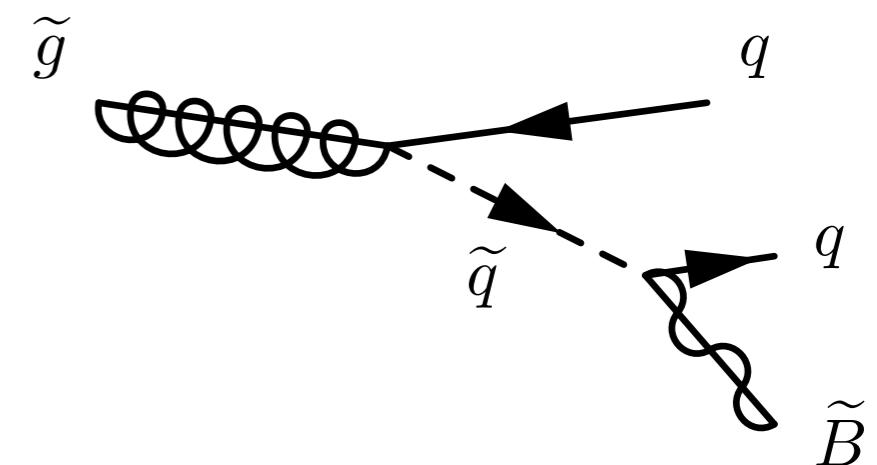
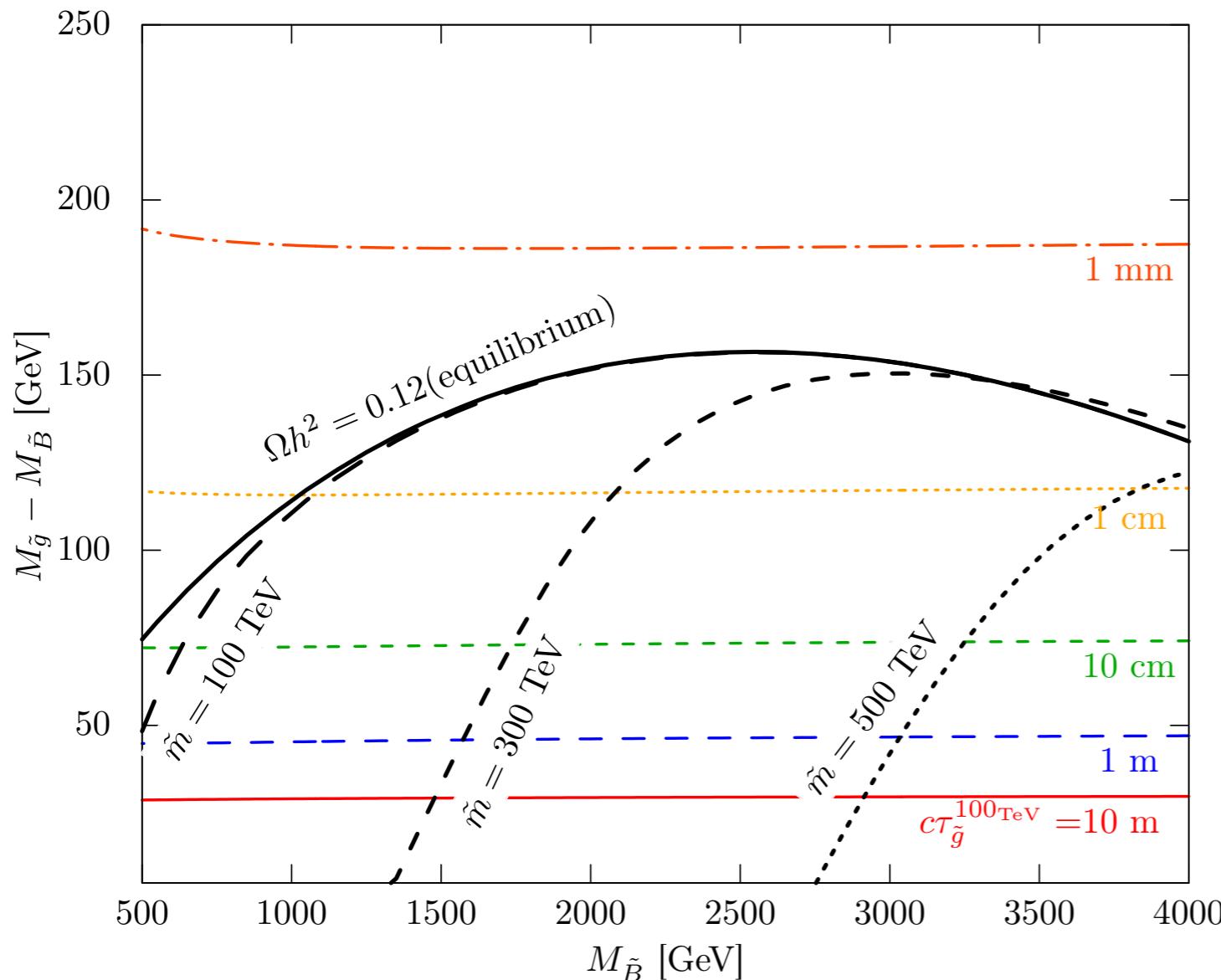
- ### Role of ISR
- Trigger
  - Boost the system

# ATLAS limit



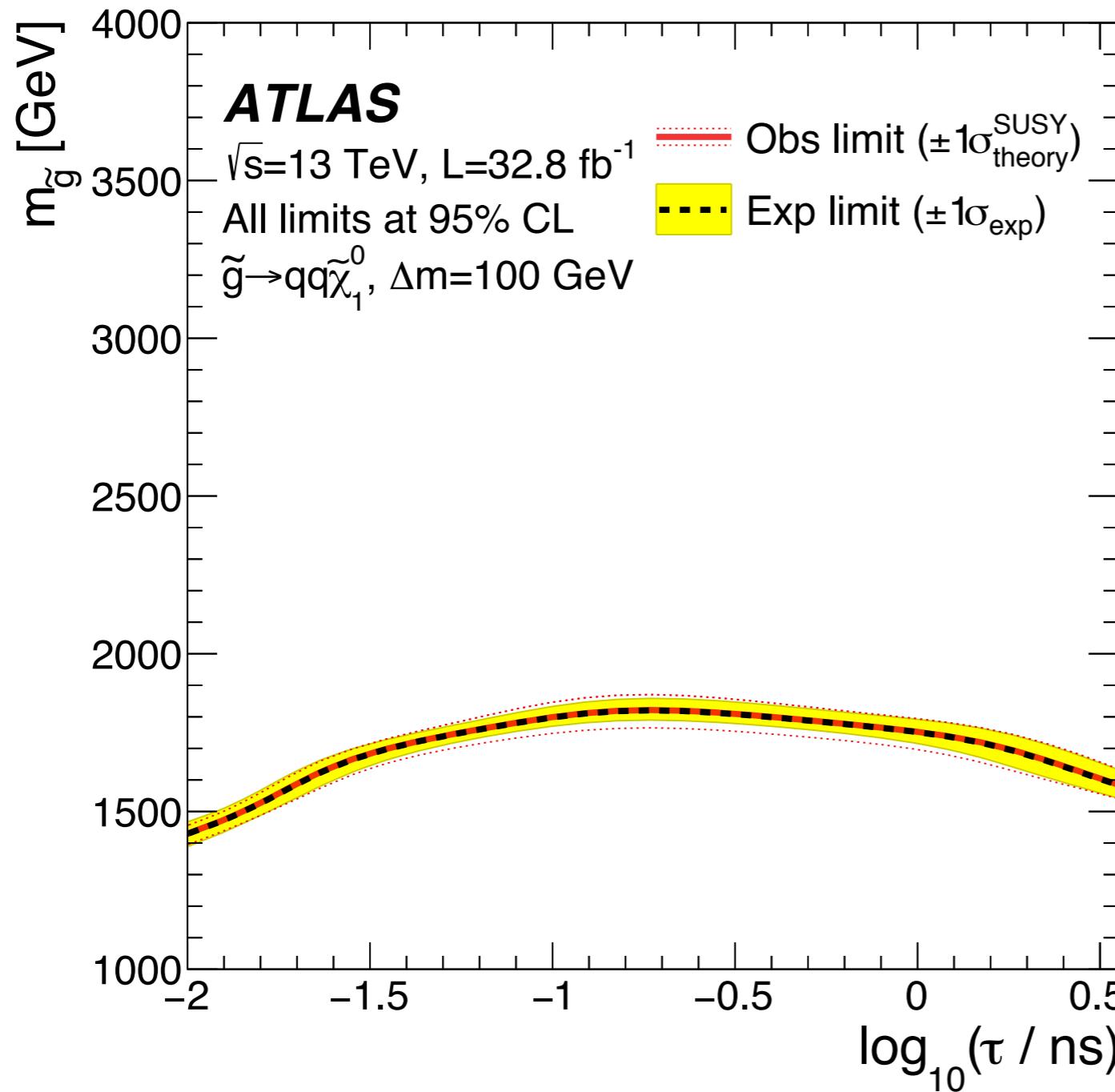
Wino with a mass up to 430 GeV has been excluded!

# Gluino decay length

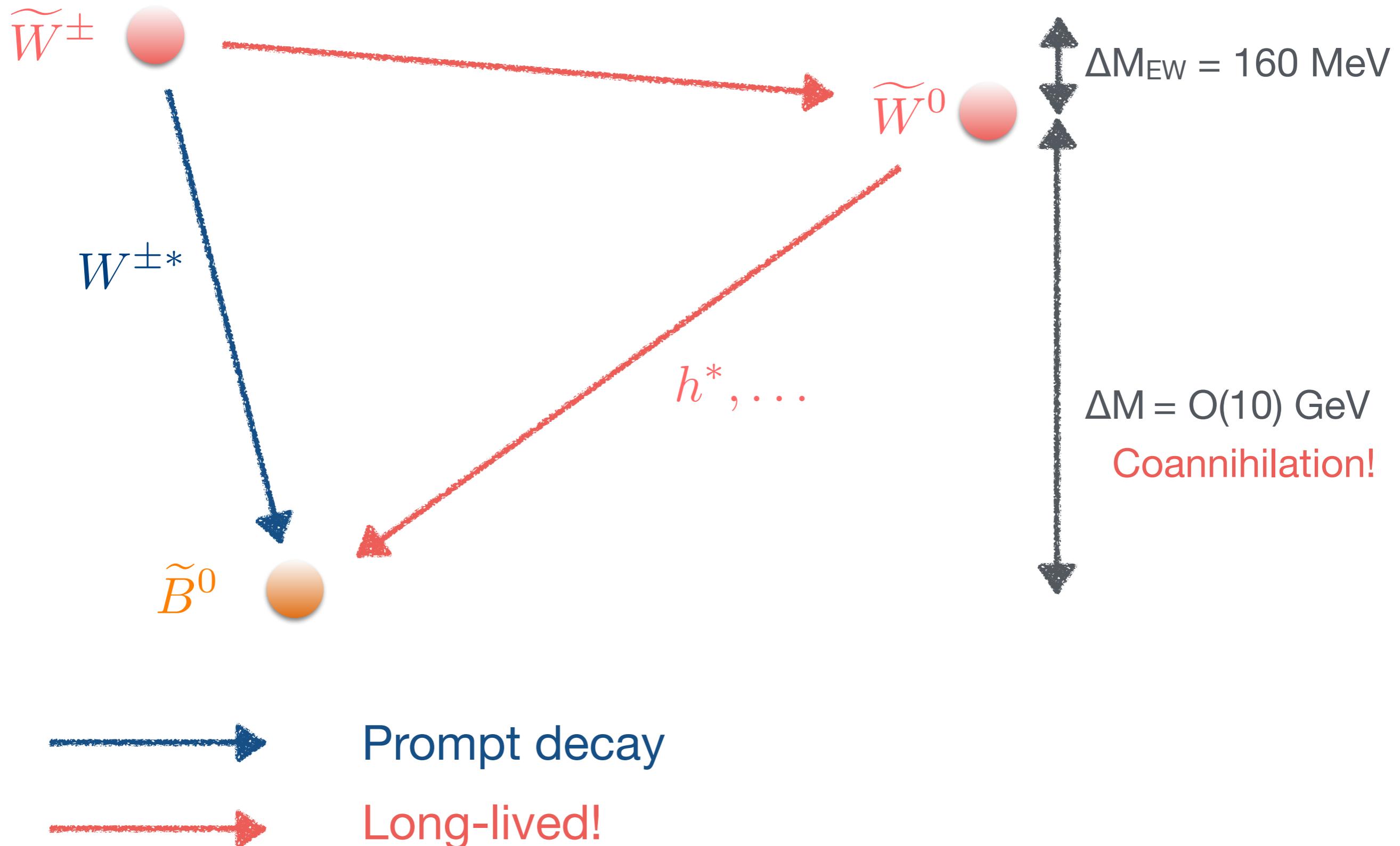


$$c\tau_{\tilde{g}} \sim \left( \frac{\Delta M}{100 \text{ GeV}} \right)^{-5} \left( \frac{\tilde{m}}{100 \text{ TeV}} \right)^4 \text{ cm}$$

# ATLAS limit



# Mass spectrum and decay chains

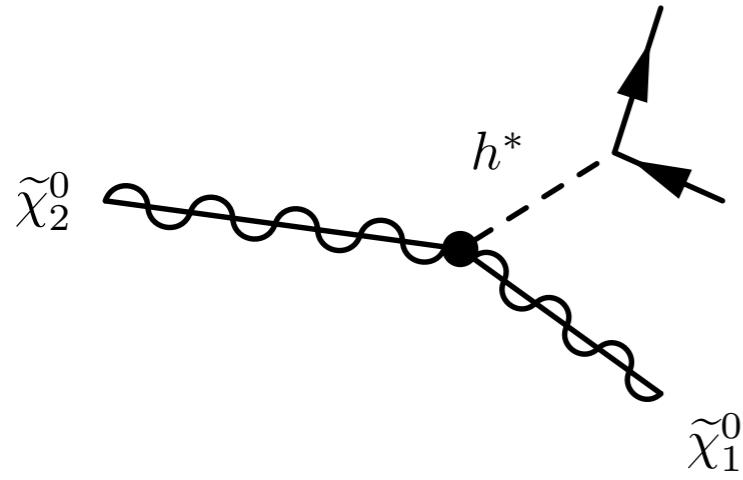


# Neutral wino decay

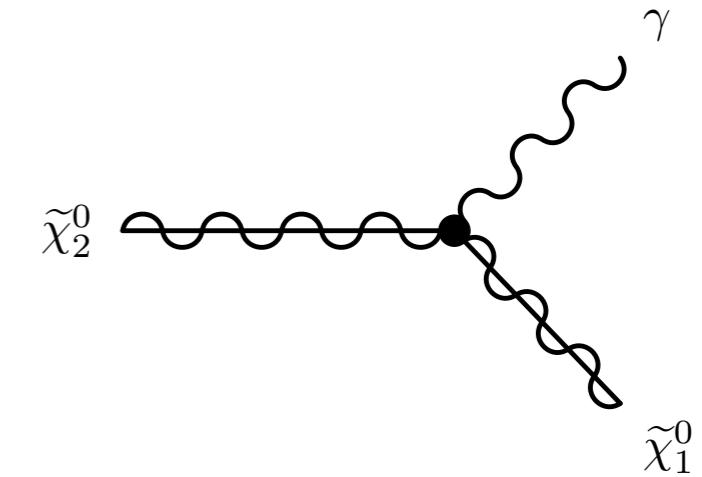
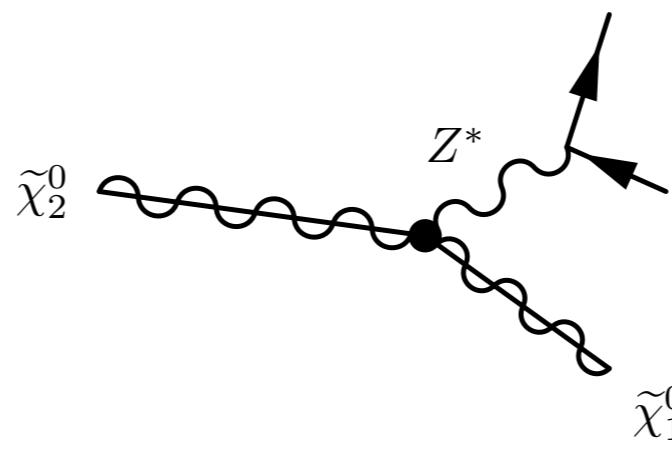
A neutral wino can decay into the bino LSP via Higgsino mixing.

→ The decay rate is suppressed for a large Higgsino mass.

Dominant diagram



Sub-dominant diagrams



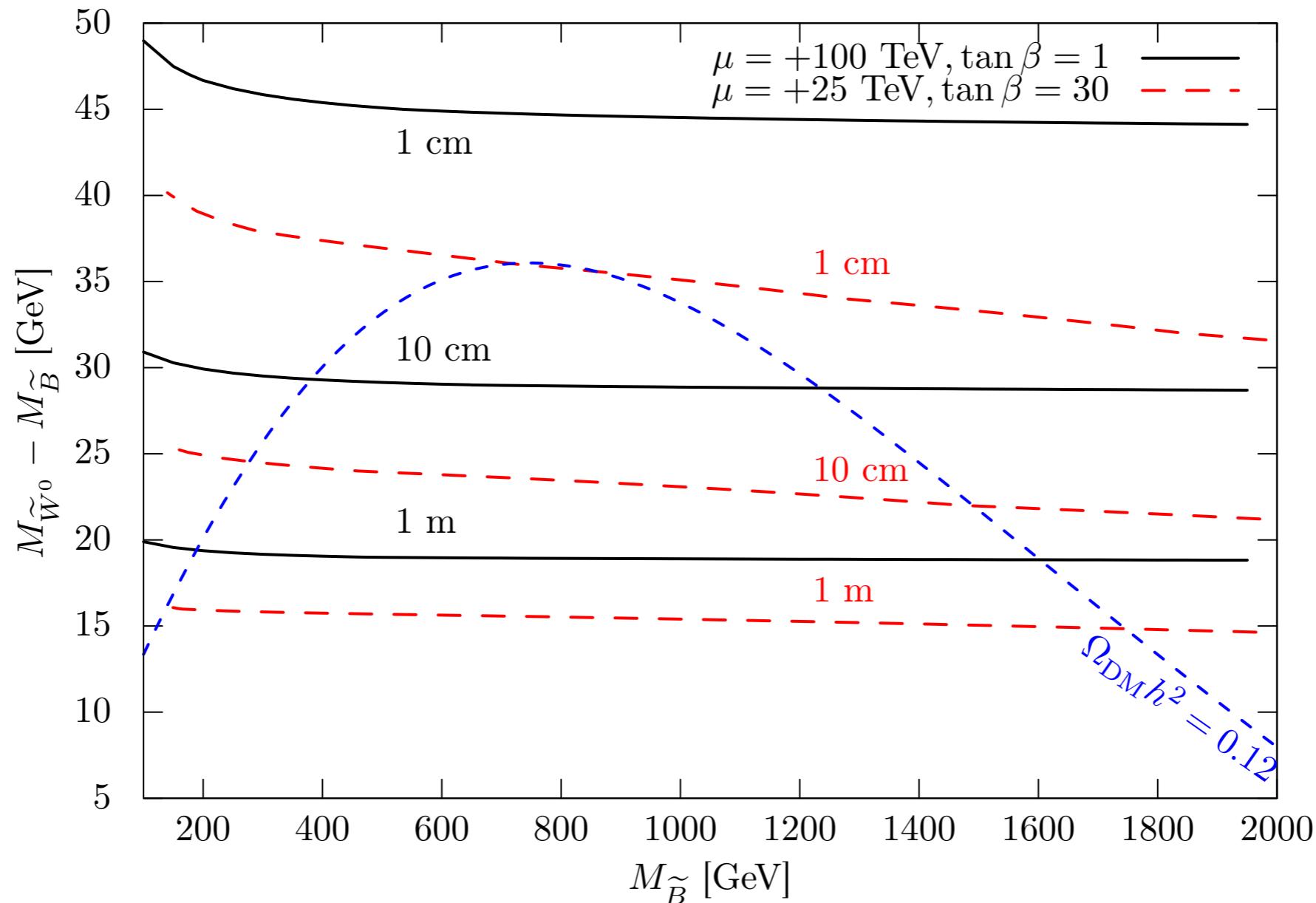
$$\propto y_f \sin(2\beta) \frac{m_W}{\mu}$$

$$\propto \cos(2\beta) \frac{m_Z^2}{|\mu|^2}$$

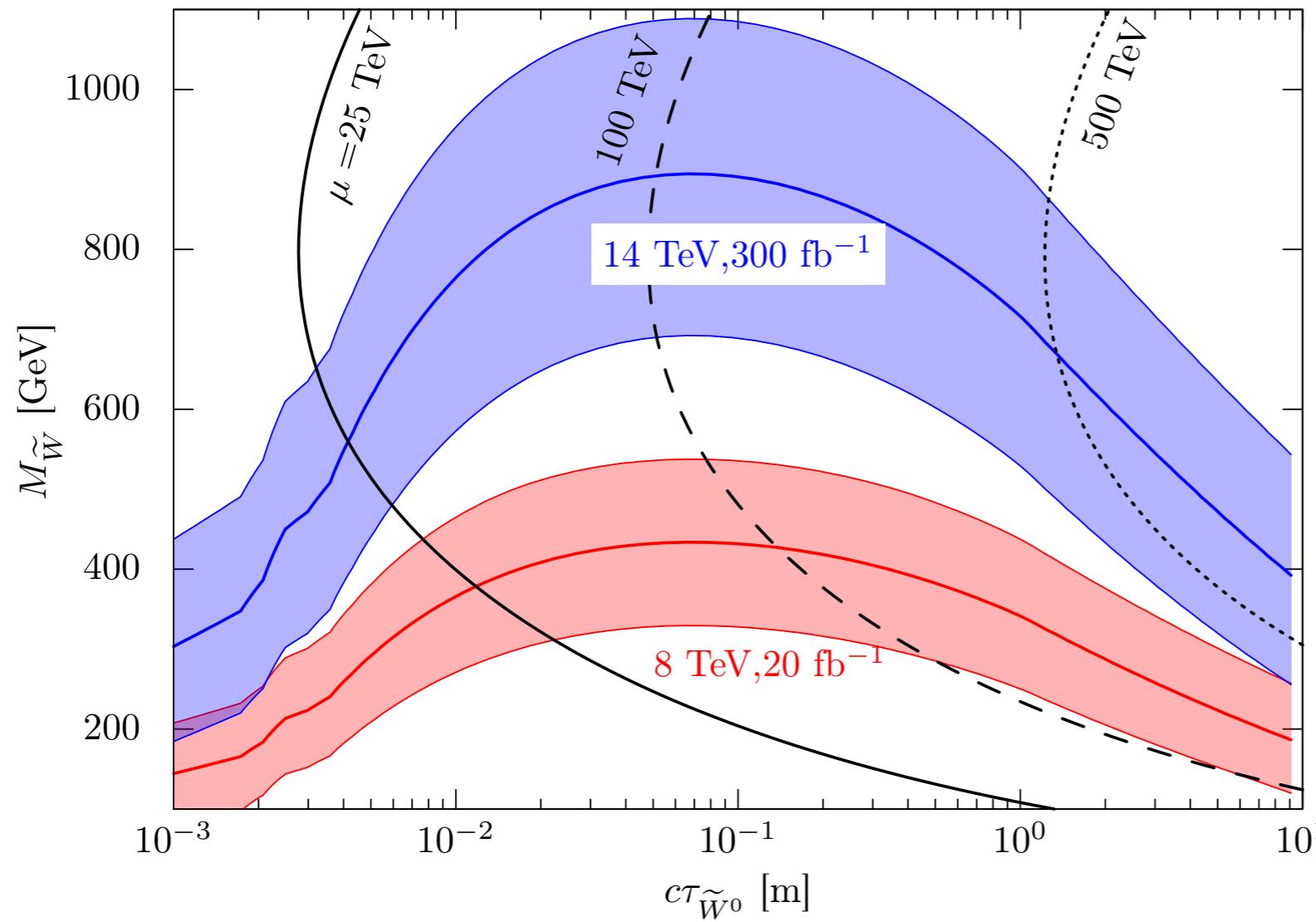
$$\propto \cos(2\beta) \frac{M_{\tilde{\chi}^0}}{16\pi^2 |\mu|^2}$$

When Higgsino mass is quite large, the **neutral wino**  $\widetilde{W}^0$  becomes long-lived.

# Decay length of neutral wino



# Prospects for the long-lived wino search



$\Delta M = 30 \text{ GeV}$   
 $\tan\beta = 2$

Acceptance rate is varied by a factor of three.

400 GeV (800 GeV) wino can be probed at 8 (14) TeV LHC.

# Indirect search

Indirect searches, especially those search for  $\gamma$  rays, are quite promising since electroweak-charged DM has a large annihilation cross sections.

## Galactic Center

Large uncertainty from DM profile.

## Dwarf spheroidal galaxies (dSphs)

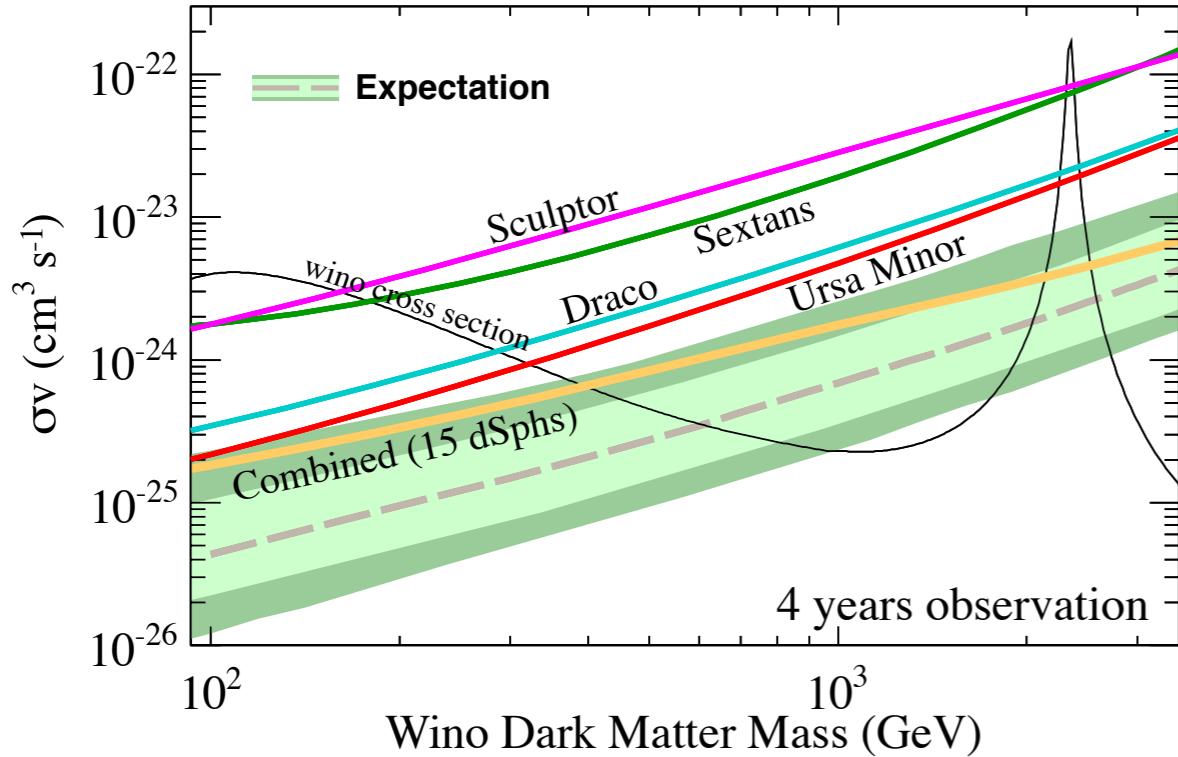
Uncertainty from DM distribution is relatively small.



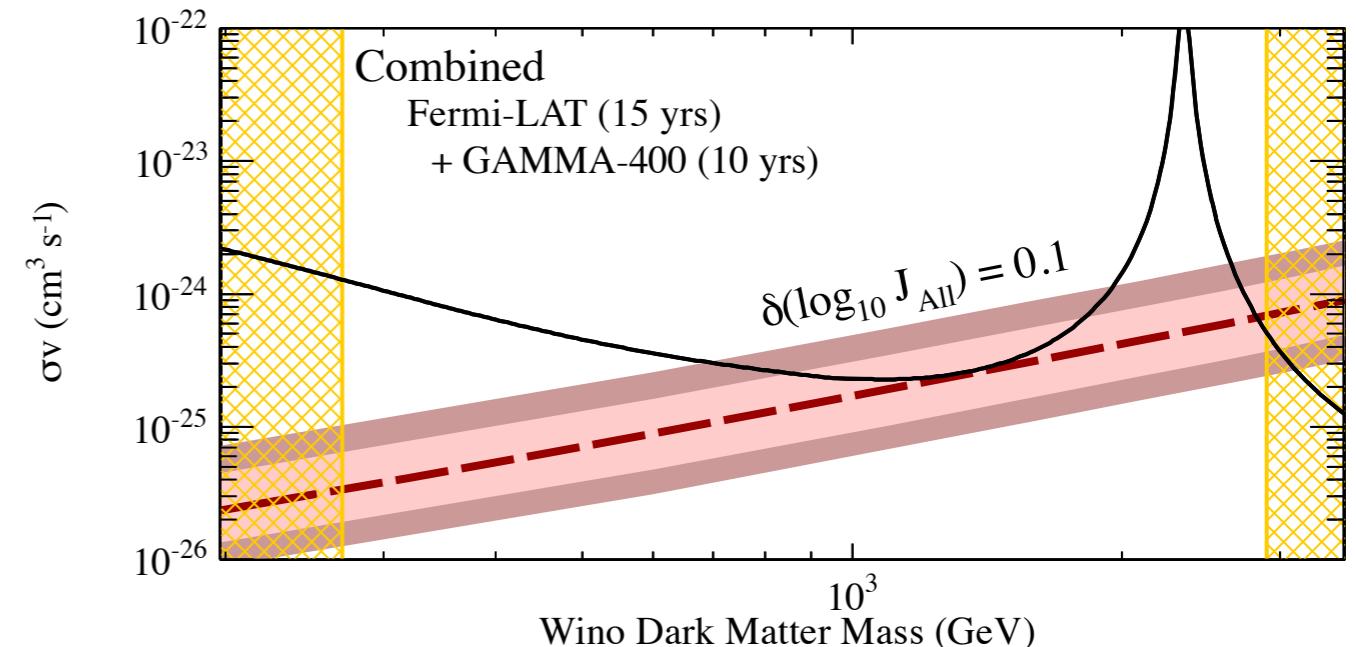
Gives a robust bound.

# Indirect search (triplet)

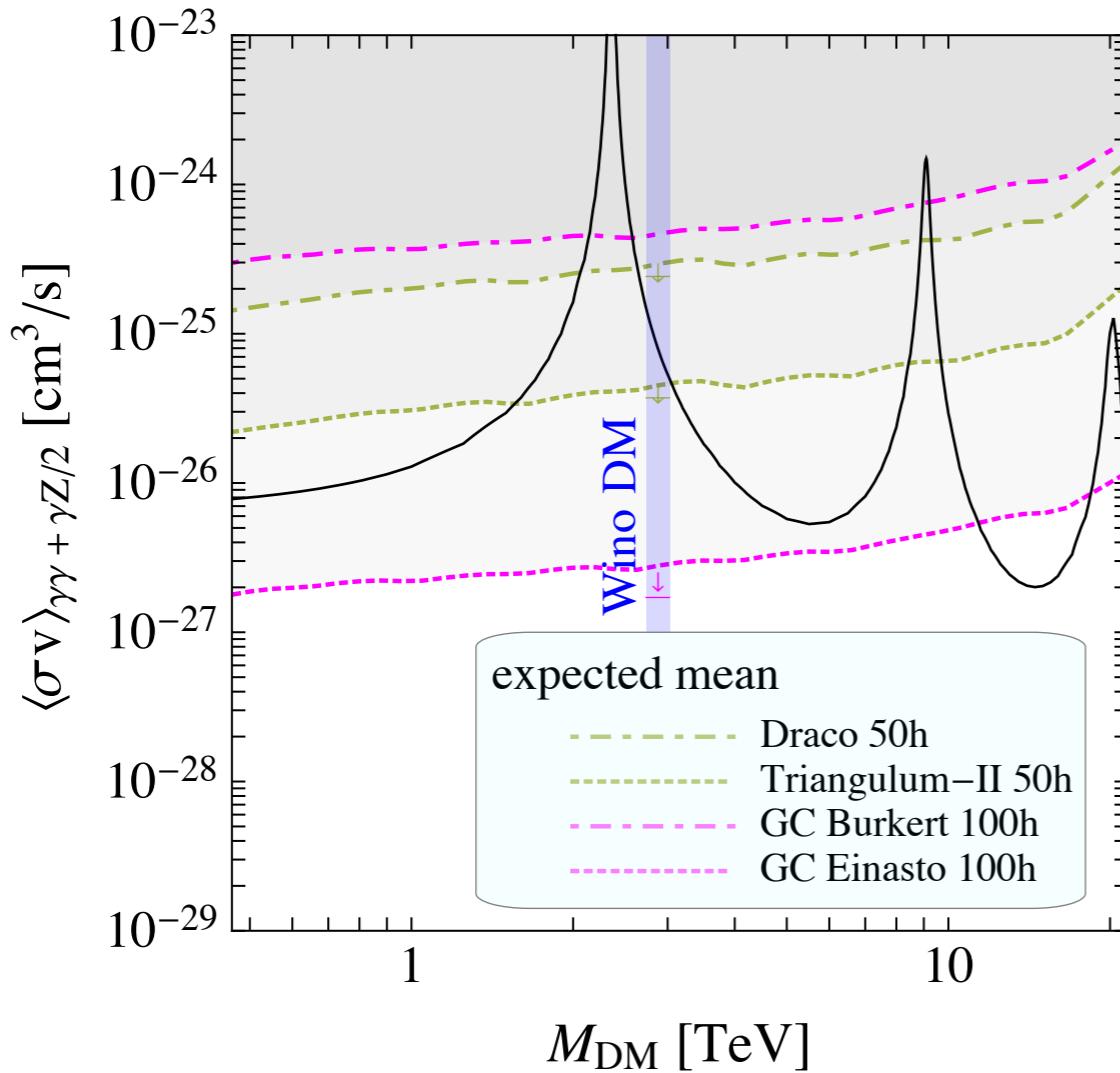
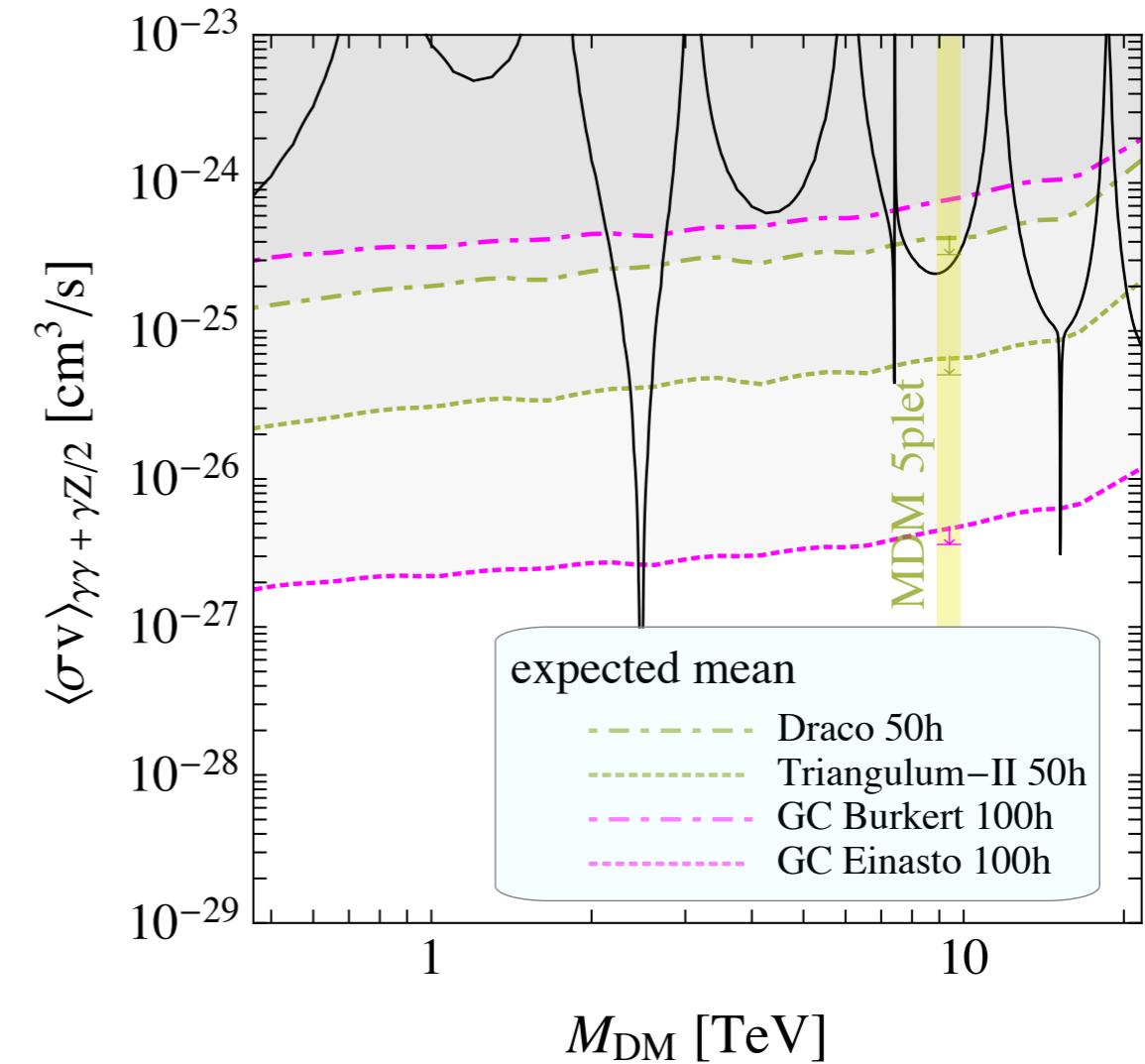
## Current constraint



## Future prospects



Triplet case can be tested in future experiments.

Triplet caseQuintuplet case

Galactic Center  $\gamma$ -ray searches suffer from large uncertainty from DM density profile.