

Experimental Aspects of Nuclear Matrix Elements for Double Beta Decays and Astro Neutrinos

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Ejiri's log cabin in Tateshina 1450m Thanks organizers

Why Nuclear Matrix element M

1. Get ν -mass $m = [1/M] [T_{1/2} \text{ G}]^{-1/2}$

2. Detector design sensitivity

$$m = k m_0 / M [B/N]^{1/4} \quad m_0 \text{ for } S=1/\text{ty}$$

- $M = \text{NME}$, $B = \text{BG/ty}$ $N = \text{Isotope mass ton}$
- M Factor 3 in M is equivalent to
- Factors 100 in BG/ton year or N tons

3. Theoretical M : factor 10 uncertainty

- Need experimental input to M

1. Neutrino nuclear responses and g_A quenching
2. Experimental studies for ν nuclear responses
3. Low multipole low momentum responses
4. Medium momentum responses for DBD and SN.
5. Neutrino responses for astro neutrinos and DBD

H.Ejiri J.I. Fujita Phys. Rep 38 **1978** 85

H. Ejiri Phys. Rep. 338 **2000** 265

H. Ejiri J. Suhonen K. Zuber Phys. Rep. 797 1 **2019**

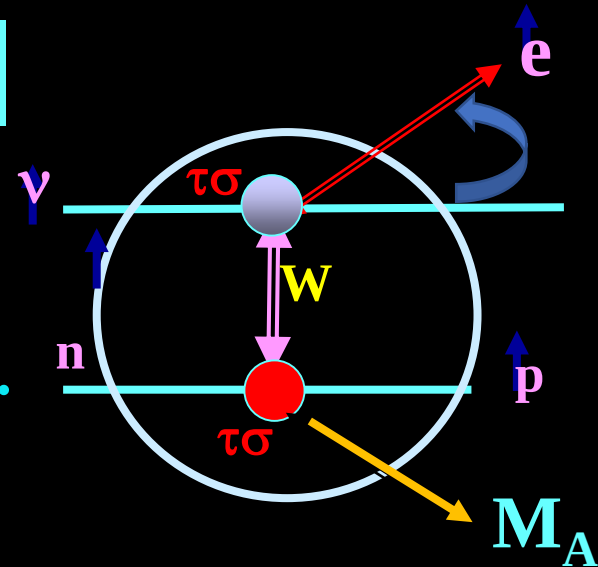
H. Ejiri Frontiers 10.3389/fyhs. **2019**. 00030

H. Ejiri NNR19 May 2019 Neutrino Response Workshop **2019**

Nuclear Response = M : M=NMEs

$$T = G \left[\frac{M}{A_v} \right]^2$$

Nuclear phys **Particle/astro phys.**



A. DBD Neutrino-less $\beta\beta$ M

$M = g_A^2 M_A - g_V^2 M_V + g_A^2 M_T$ with bare $g_{A,V}$ for free N.

$$\mathbf{M}_A = k_A^2 \mathbf{M}_A(\text{model}), \quad \mathbf{M}_V = k_V^2 \mathbf{M}_V(\text{model}),$$

$k_A = g_A^{\text{eff}}/g_A$: Effects which are not in $M_A(\text{model})$

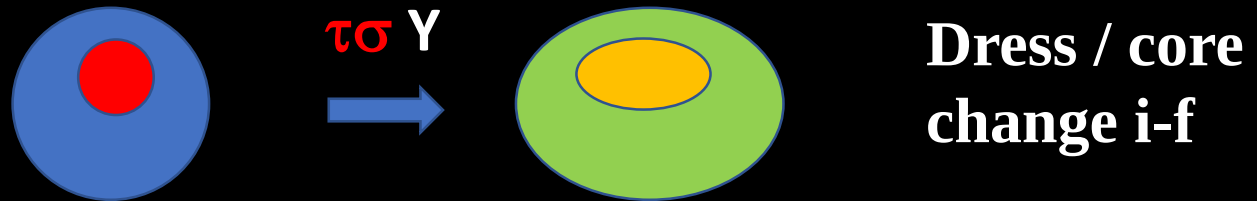
B. Astro ν and anti- ν response

$$\mathbf{M}_A = \mathbf{k}_A \mathbf{M}_A(\text{model}), \quad \mathbf{k}_A = \mathbf{g}_A^{\text{eff}} / \mathbf{g}_A :$$

DBD ν and Astro ν are $q=5-150$ MeV/c, $J^\pm$ with $J=0-5$

Effective couplings $k_A = g^{\text{eff}}/g$

$M_A = k_A M_A(\text{model})$ $k = g^{\text{eff}}/g$ **Deviation of model NME from Exp. = True MNE since Model is NOT perfect**



Since 1960 for μ GT as e^{eff}/e .

A : Theoretical way ab initio NME $k_A = g^{\text{eff}}/g=1$
Cal. for g^{eff}/g for meson isobar, many body, medium

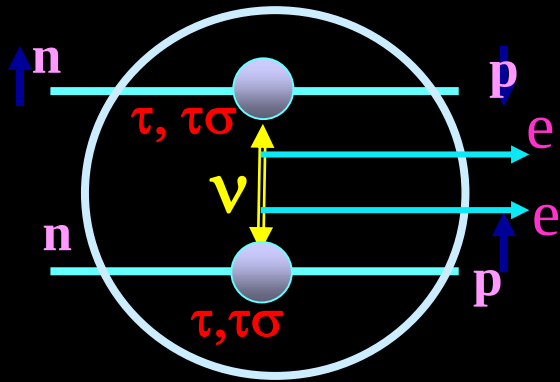
B: Experimental way : present

Exp $g^{\text{eff}}/g = \text{Exp NME}/\text{Model NME}$ for single beta M,
Use Exp. g^{eff}/g and Model QP, QRPA to get NME

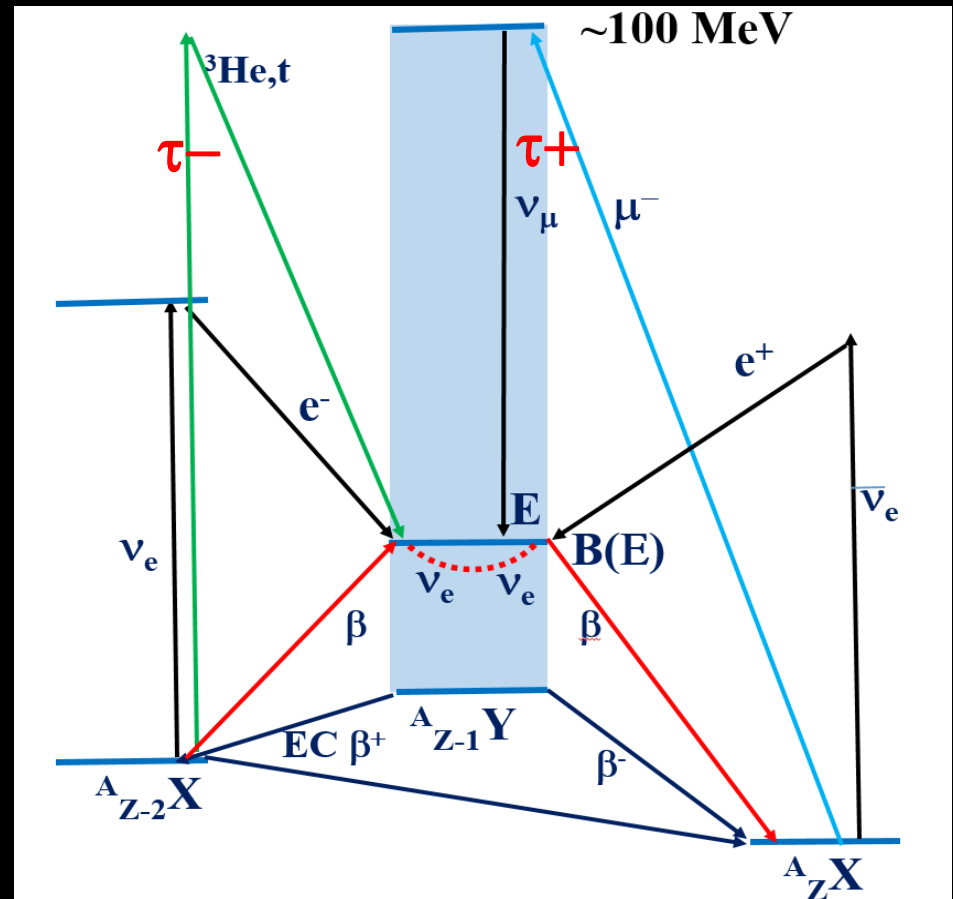
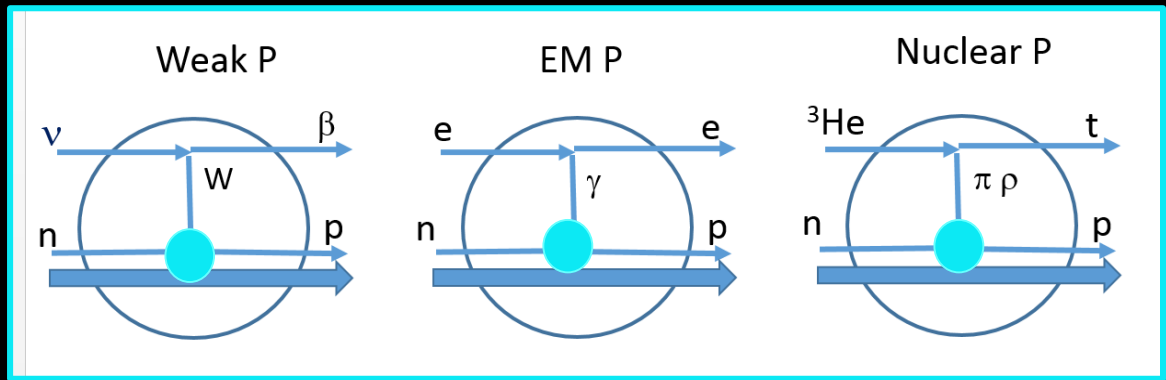
CERs for CC

$$M = g_A^2 M_{DA} - g_F^2 M_D$$

Sensitive to NN, $N\Delta/\pi$
nuclear medium effects



$M(\text{EXP}) = g_A M, g_F M$ by
lepton and nuclear CERs
to help calculations which are
sensitive to nn & medium.



Response experiments by RCNP/Osaka

RCNP Osaka p, He ,



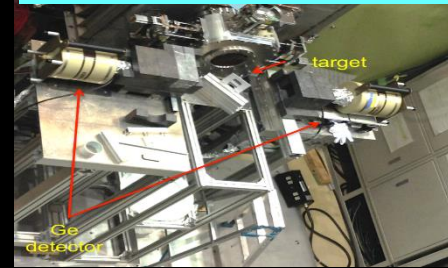
MuSIC μ



J-PARC 3-50 GeV p, ν, μ



MLF MUSE μ

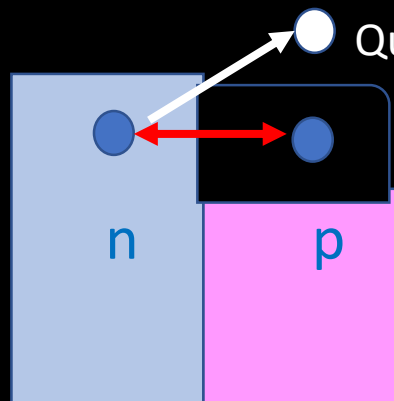
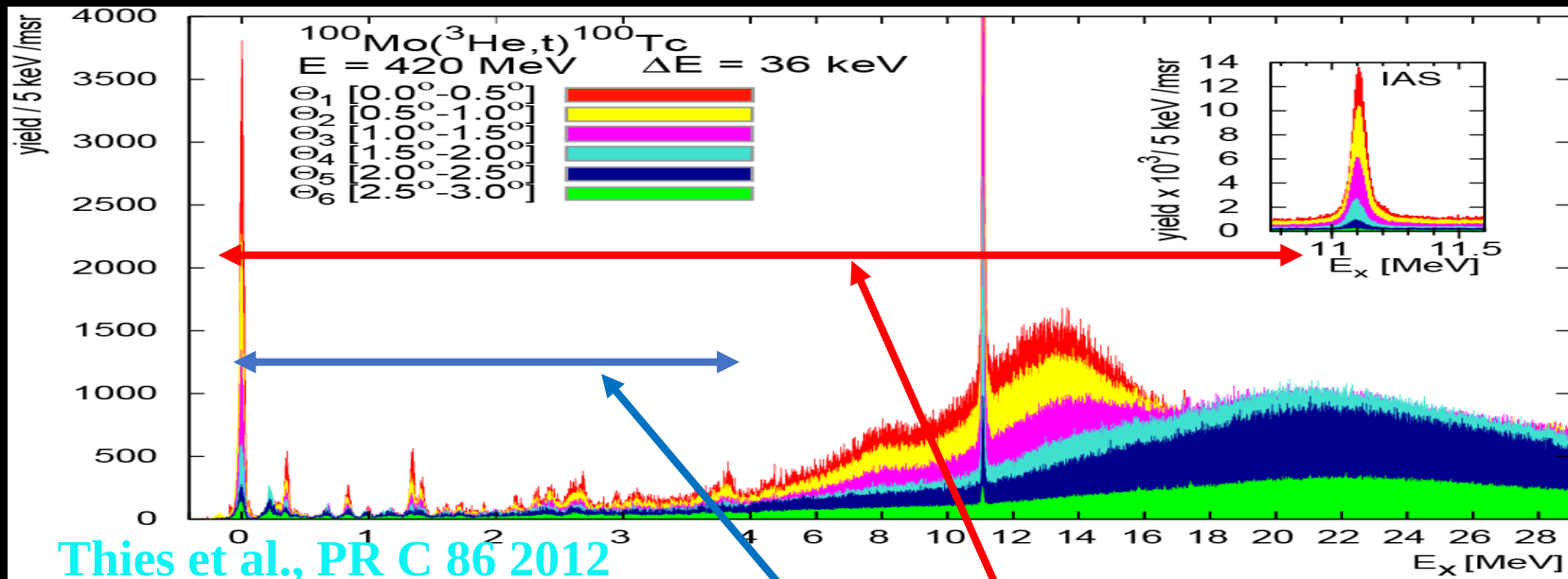


Spring-8 GeV- MeV pol. γ



Oto under gr. $\beta\beta-\nu,$

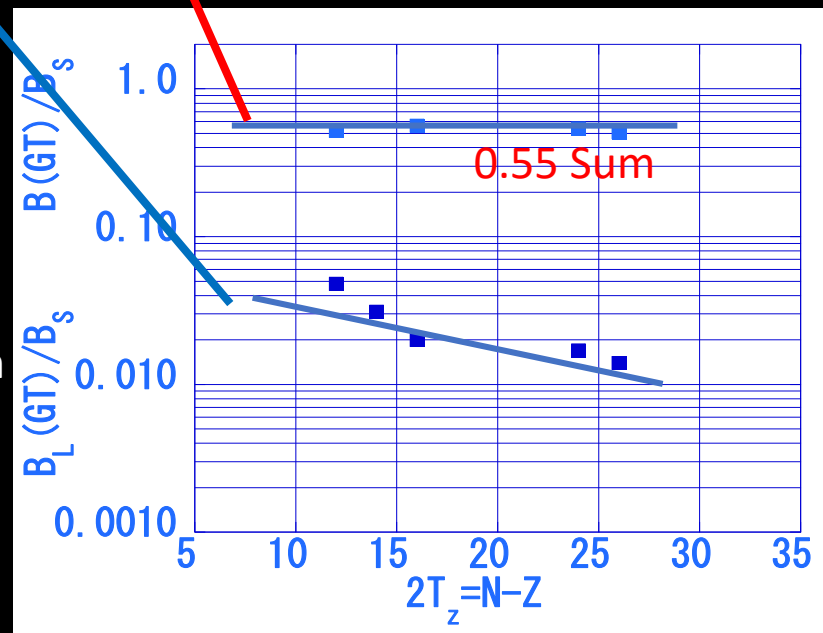
B(GT) sum strength



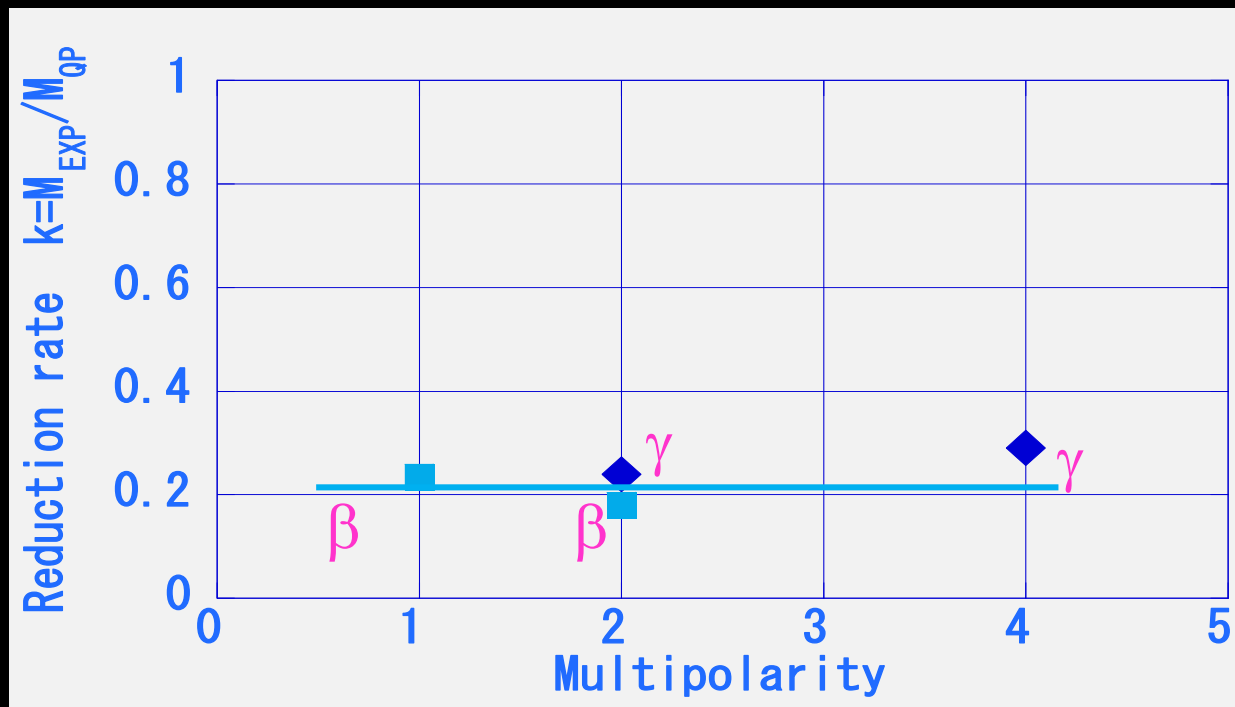
C. Douma 116 122 Sn

$$\Sigma B(\text{GT})/B(\sigma) = 0.55 (N-Z)$$

Note : Nucleon in nucleus
 is 0.55 free nucleon



Universal reductions of axial vector β & γ in low p



Ejiri Fujita
PR 34 85 1978

$k = k(\tau\sigma)$ $k(\text{NM}) \sim 0.25$ with respect to QP

$k = k(\tau\sigma) \sim 0.5$: Nucleonic long range $\tau\sigma$ GR

$k(\text{NM}) \sim g_A^{\text{eff}} / g_A \sim 0.6$: Short range nucl. medium $\Delta \pi$

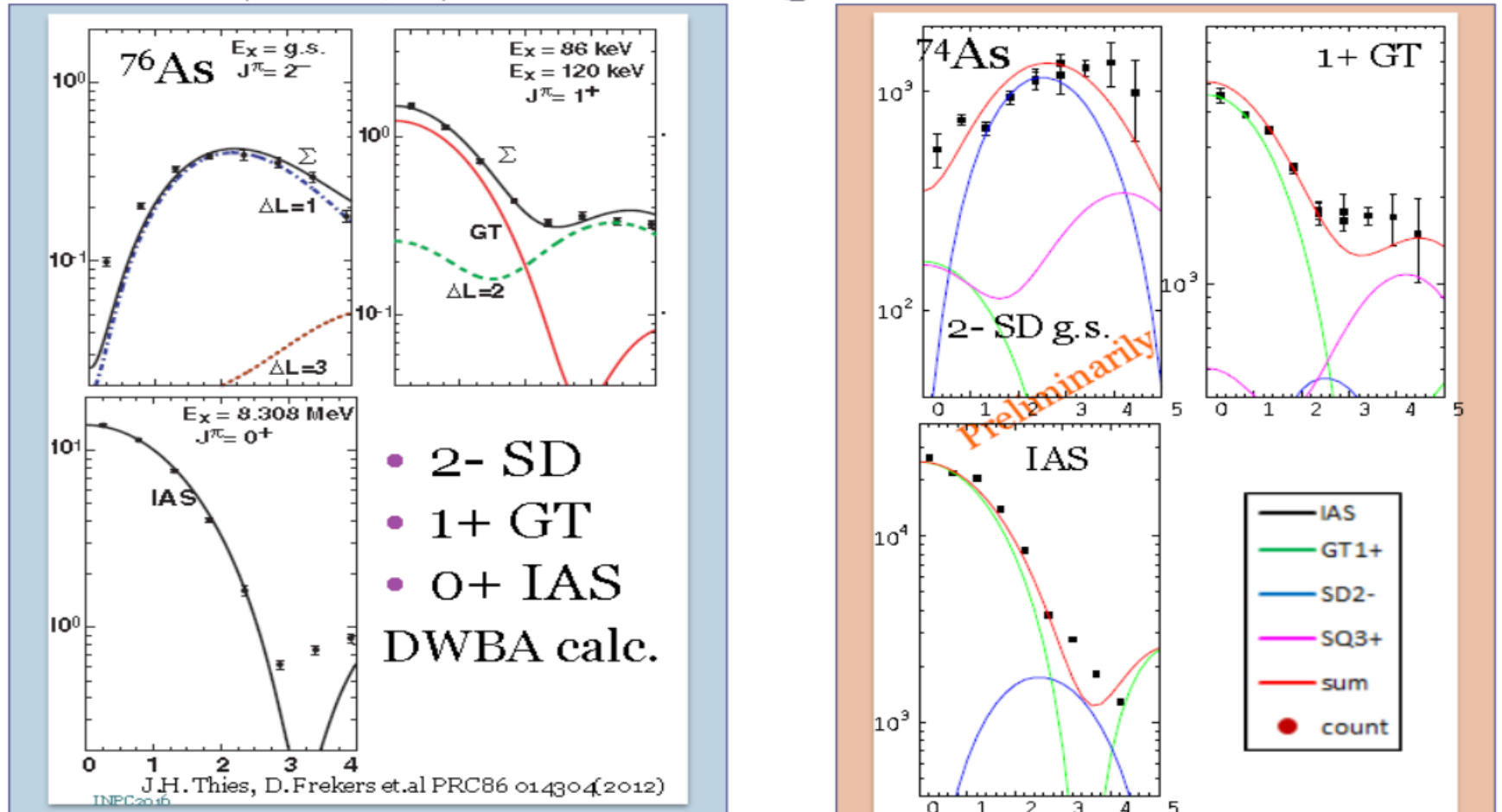
H, Ejiri J. Suhonen J. Phys. G. 42 2015

H. Ejiri N. Soucouthi, J. Suhonen PL B 729 2014 .

L. Jokiniemi J. Suhonen H. Ejiri AHEP2016 ID8417598

SD Spin dipole $\tau[\sigma \mathbf{r} Y_1] 2^-$ Major of DBD

$^{74,76}\text{Ge} (^3\text{He}, t) ^{74,76}\text{As}$ Angular distribution



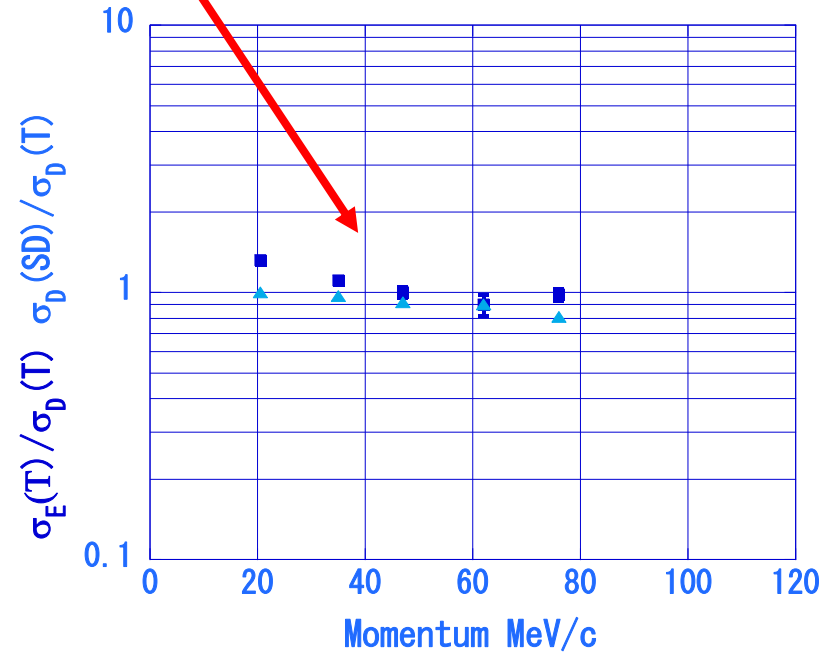
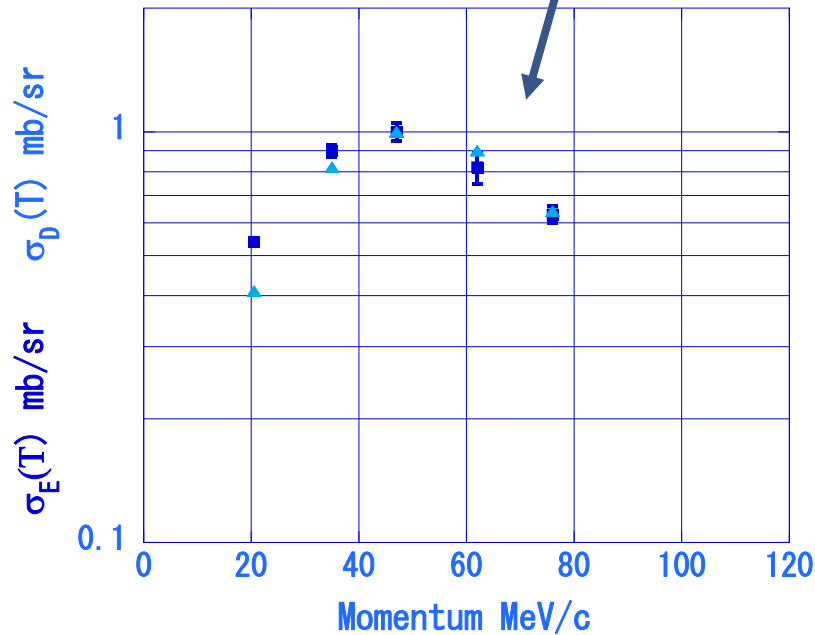
H. Akimune, H. Ejiri, RCNP Catania, KVI, Munster • •

Kinematical q dependence and NME q dependence

$$\frac{d\sigma_i}{d\Omega} = K_i(\alpha) F_i(\alpha, q) J_i(\alpha)^2 \kappa^{eff}(q)^2 B_i(\alpha), \quad (5)$$

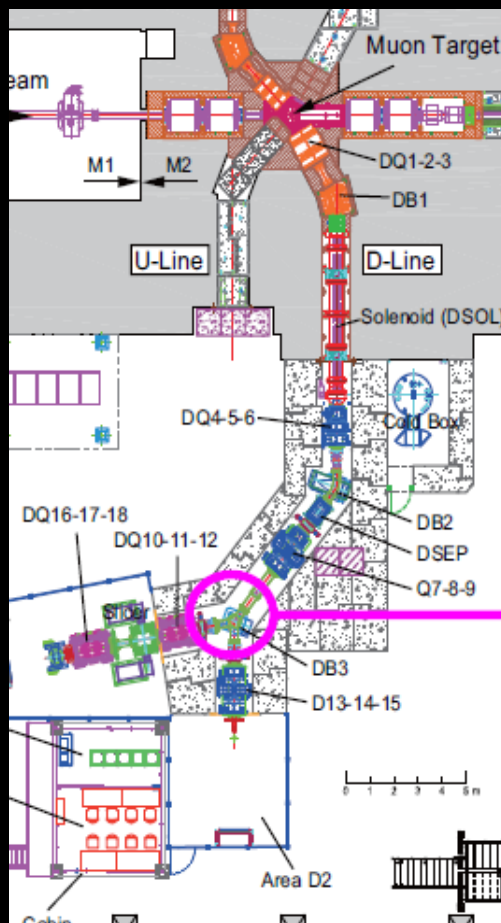
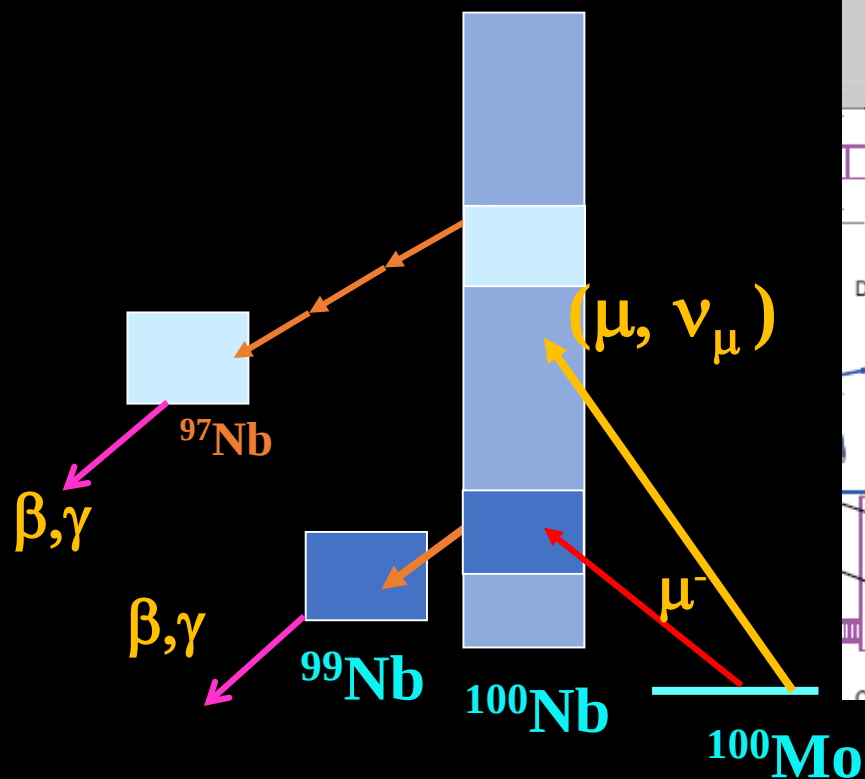
where $K_i(\alpha)$ and $J_i(\alpha)$ with $\alpha=F, GT, \text{ and } SD$ are the kinematic factors and the volume integrals of the interaction, respectively. The kinematic q -dependence is given

^{130}Te SD 2-

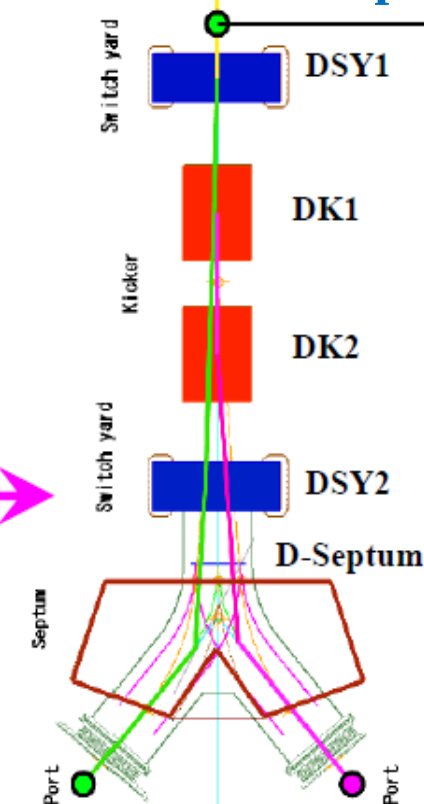


$g_A^{eff} \sim \text{const over } q=0-100 \text{ MeV/c}$

CER ($\mu, \nu_\mu, \text{xn } \gamma$) $\bar{\nu}-\beta^+$ Responses $q \sim 80 \text{ MeV}/c$



J-PARC 3 GeV p

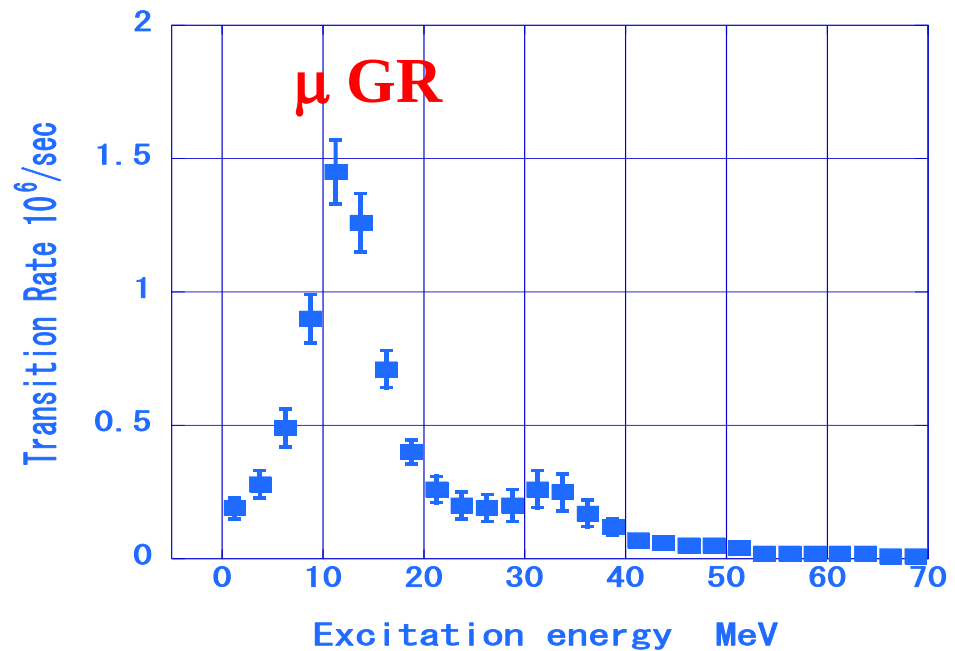
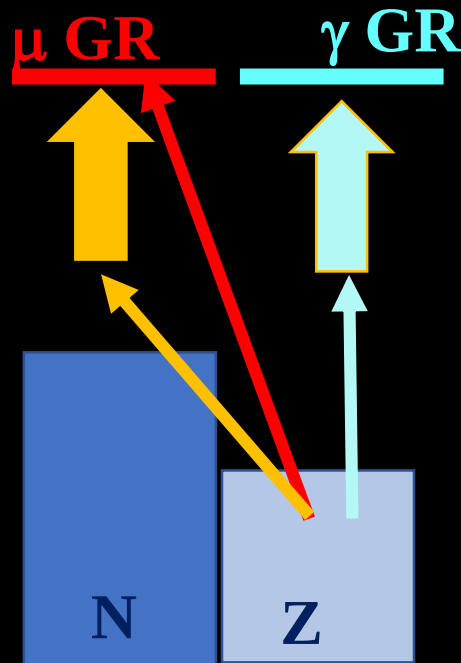
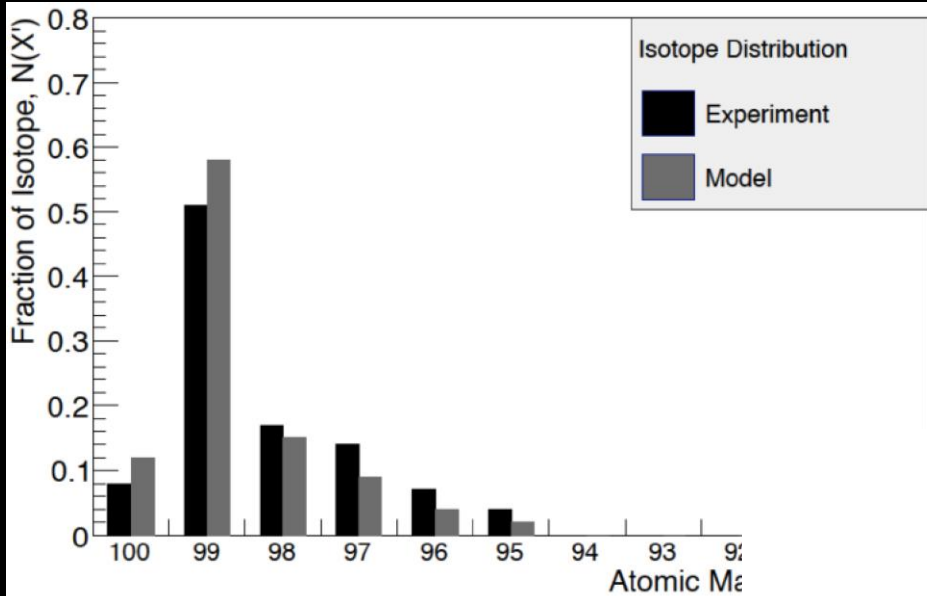


γ_i from $^{100-i}\text{Nb}$: relative strength Life time : the absolute strength

H. Ejiri Proc. e- γ conference Sendai 1972, H. Ejiri et al., JPSJ 2014
NNR19:I. Hashim , Hashim H. Ejiri et al., PRC 97 (2018) 014617

Jokiniemi L, Suhonen H, Ejiri H, and Hashim I.H. 2019 P L B 794 143.

$k \sim 0.4$ for pnQRPA



I. Hashim H. Ejiri, MXG16, PR C 97 2018

$$M^{0\nu} = \left[\frac{g_A^{eff}}{g_A}\right]^2 [M_M^{0\nu}(GT) + M_M^{0\nu}(T)] + \left[\frac{g_V}{g_A}\right]^2 M_M^{0\nu}(F),$$

M(α) Model

pnQRPA

^{76}Ge

M(GT)=5.4,

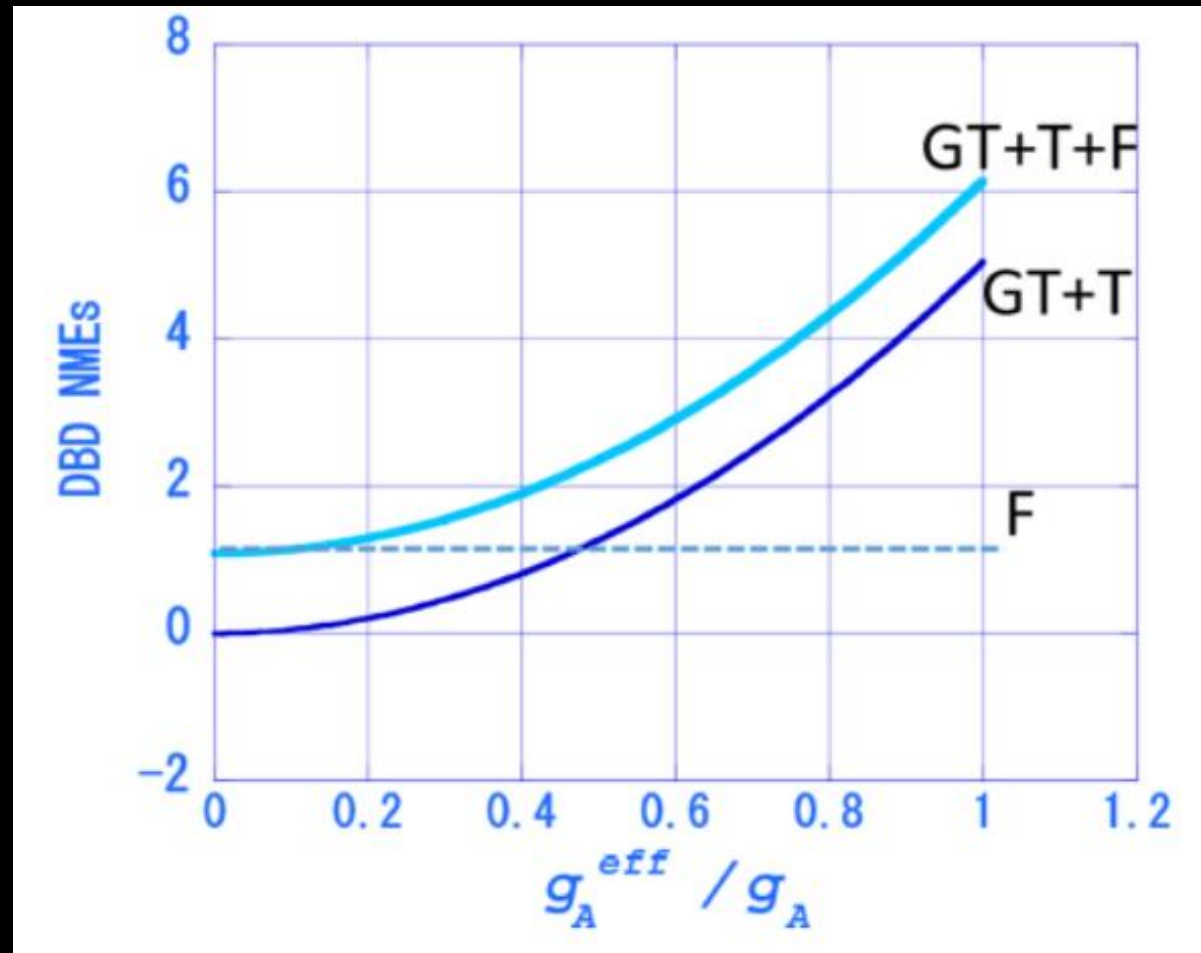
M(T)=-0.36

M(F)=1.76

Jokiniemi,

Ejir, Suhonen

PR C 98 2018

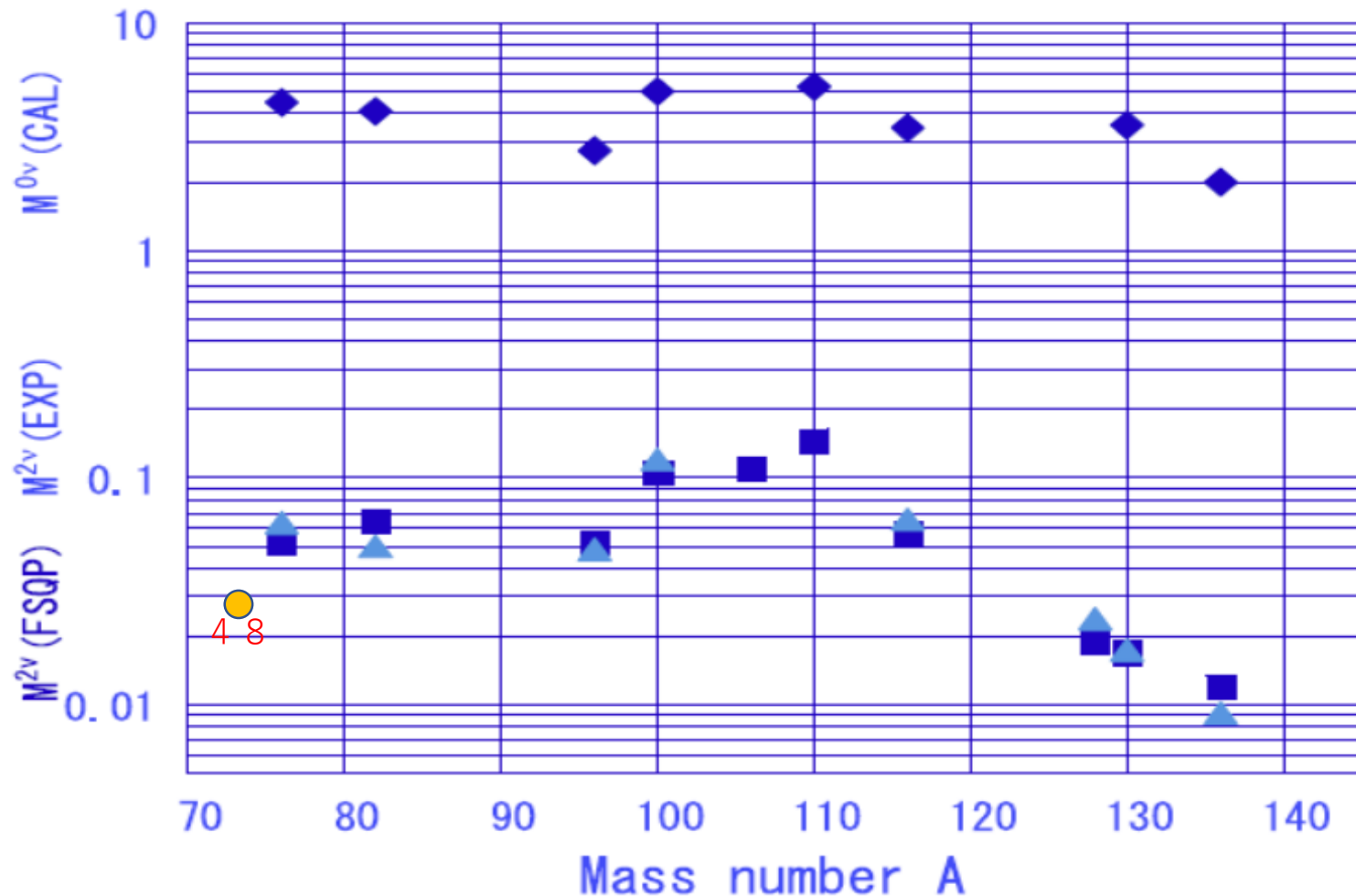


$g_A^{eff} / g_A = 0.5$ leads to reductions 0.2 for M(GT),

0.4 for $M^{0\nu}$, 0.16 for DBD rate, ~ 40 for DBD detector

Nuclear structures on 2ν and $0\nu\beta\beta$ NMEs

H. Ejiri, J. Suhonen and K. Zuber / *Physics Reports* 797 (2019) 1–102



$2\nu\beta\beta$ NMEs square exp, triangle FSQP(Ejiri) J. Phys. 2017

DBD strategy Goal IH mass 20-15 meV

Yes Majorana and IH and mass , No Dirac or NH

- $m = k m_0 / M [B/N]^{1/4} m_0$ for $S=1/\text{ty}$
- $M = NME$, $B = BG/\text{ty}$ $N = \text{Isotope mass ton}$

ν -mass from 200 meV to 20 meV :

- BG by a factor 100 and N by 100.

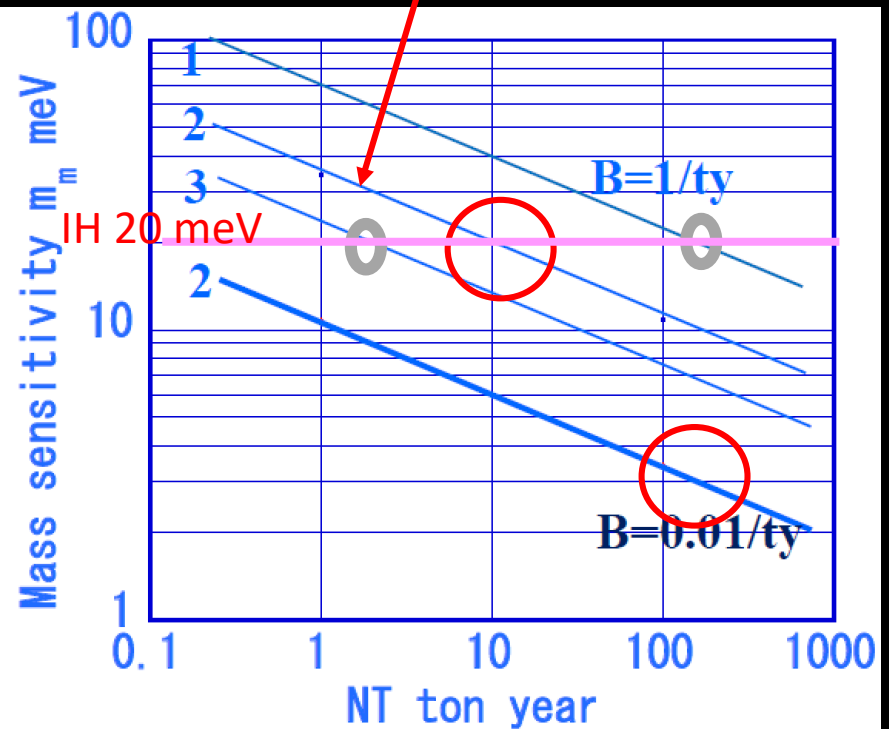
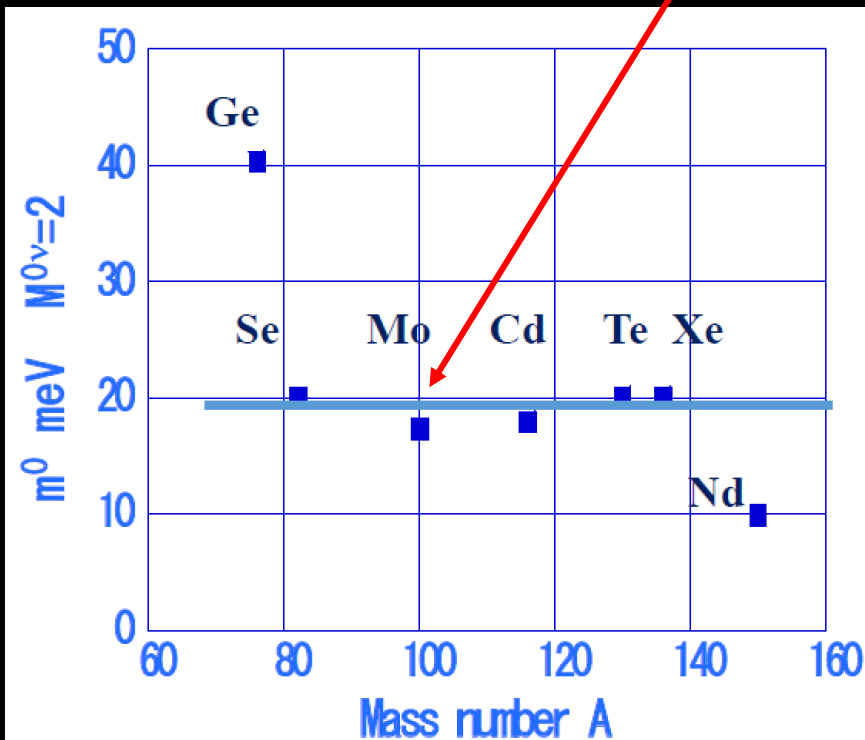
Exp. with Large M, large N, small BG

DBD $0\nu\beta\beta$ NMEs and DBD mass sensitivity

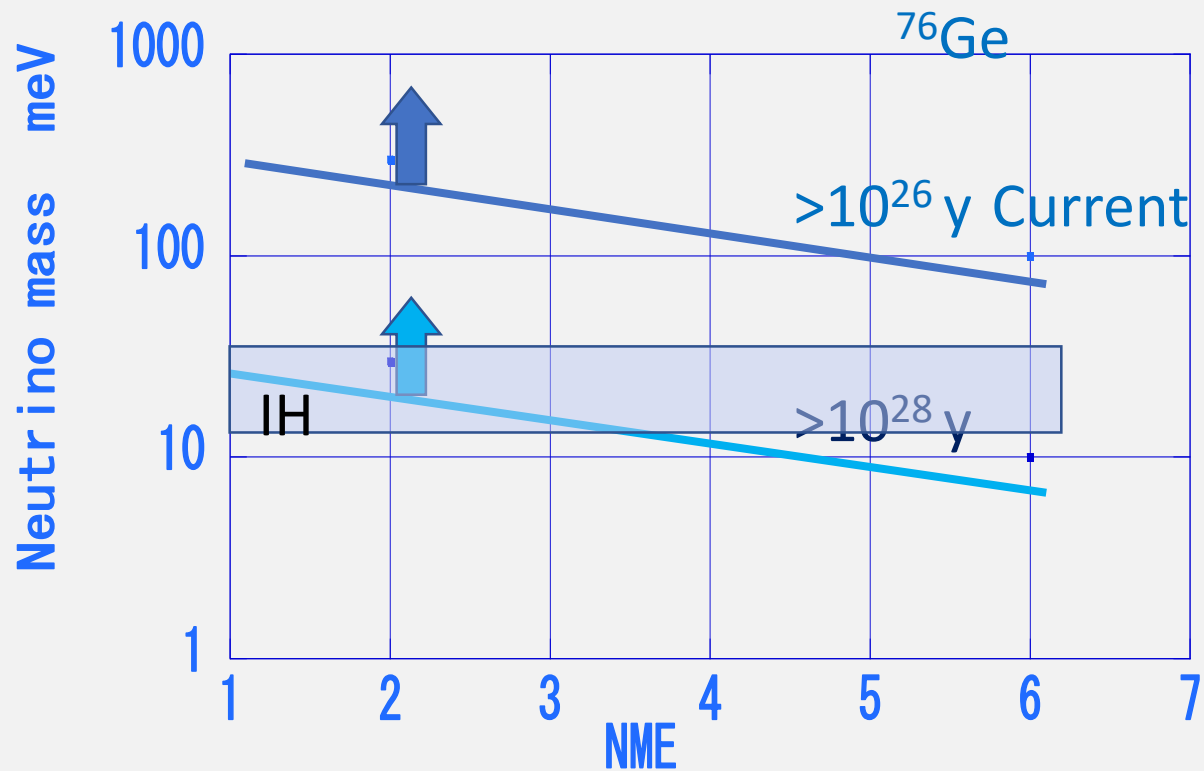
Nuclear sensitivity $m^0 =$ mass for 1/t y

Ge requires a factor 20 less BG

Mass sensitivity mass to be detected $m_m = m^0 D$



$$M^{0\nu} = k^2 M(\text{QRPA}) \sim 2, \quad k = (g^{\text{eff}}/g) \sim 0.6 - 0.7$$



Neutrino mass regions depend on NME

Possible DBD detector with IH mass 20 meV

Yes Majorana and IH and mass No Dirac or NH

- $m = k m_0 / M [B/N]^{1/4}$ m_0 for $S=1/ty$
 - $M = NME = g_A^2 M(QRPA)$
 - $B = BG/ty$ $N = \text{Isotope mass ton}$

m_0	In case M	BG/t y	N ton /5y	Isotope A
40	2	0.1	3	Ge 76
20	1.5	1	6	Se 82
20	2	1	2	Mo 100
20	1-2	1	30-2	Xe 136



Thanks for your attention Greenary Nymph 翠の精

Remarks

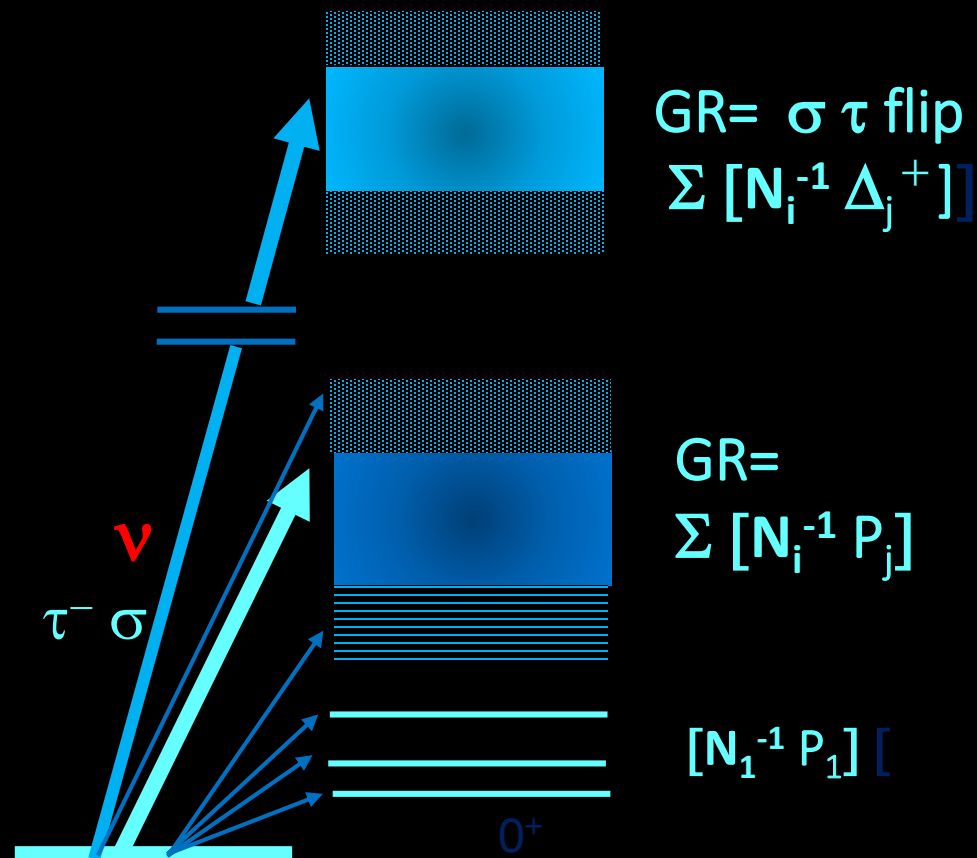
1. CER: (${}^3\text{He}, t$) provides NMEs $J=0-2$, $p=5-100$ MeV/c used for evaluating β^- , ν astro ν and DBD responses.
2. CER: (μ, ν_μ) shows MGR (giant resonance) at 12 MeV provides NMEs $J=0-3$, $p=50-100$ MeV/c used for evaluating β^+ , ν astro $\bar{\nu}$ and DBD responses.
3. $M_{\text{EXP}}(\text{GT}, \text{SD})$ are reduced from M_{QP} by $k^{\text{eff}} \sim 0.2-0.25$, $k_{\text{ts}} \sim 0.4-0.5$ by nucl. $\tau\sigma$, $k_{\text{m}} \sim 0.4-0.6 = (g_{\text{A}}^{\text{eff}}/g_{\text{A}})$.
4. DBD NMEs ~ 0.5 NMEs(QRPA), and 16 times less BG or more DBD isotopes than QRPA.

Estimation of $M(SD)$ for $\beta\beta$ nuclei

$$R = \frac{B(SD)}{B(F)} \bigg/ \frac{\sigma_{SD}}{\sigma_{IAS}} = \frac{B'(SD)}{B'(F)} \bigg/ \frac{\sigma'_{SD}}{\sigma'_{IAS}} \quad B(SD) = \frac{|M(SD)|^2}{2J_i + 1}$$

Benchmark Nuclei		M(SD)	$\sigma(SD)/\sigma(IAS)$	R
$^{74}\text{Ge} \leftrightarrow ^{74}\text{As}$	2- g.s.	1.68	$3.80 \pm 0.20 \text{ E-02}$	2.38 ± 0.25
$^{122}\text{Sn} \leftrightarrow ^{122}\text{Sb}$	2- g.s.	3.75	$1.71 \pm 0.23 \text{ E-01}$	6.60 ± 0.89
$^{124}\text{Te} \leftrightarrow ^{124}\text{Te}$	2- g.s.	2.74	$8.00 \pm 1.50 \text{ E-02}$	5.30 ± 0.74
$\beta\beta$ decay Nuclei		M(SD)		
$^{76}\text{Ge} \leftrightarrow ^{76}\text{As}$	2- g.s.	1.57 ± 0.24	$2.71 \pm 0.13 \text{ E-02}$	2.38 ± 0.66
$^{128}\text{Te} \leftrightarrow ^{128}\text{I}$	2- 134 keV	2.82 ± 0.48	$7.75 \pm 0.50 \text{ E-02}$	5.95 ± 0.60
$^{130}\text{Te} \leftrightarrow ^{130}\text{I}$	2- 354 keV	3.33 ± 0.59	$9.90 \pm 1.47 \text{ E-02}$	5.95 ± 0.60

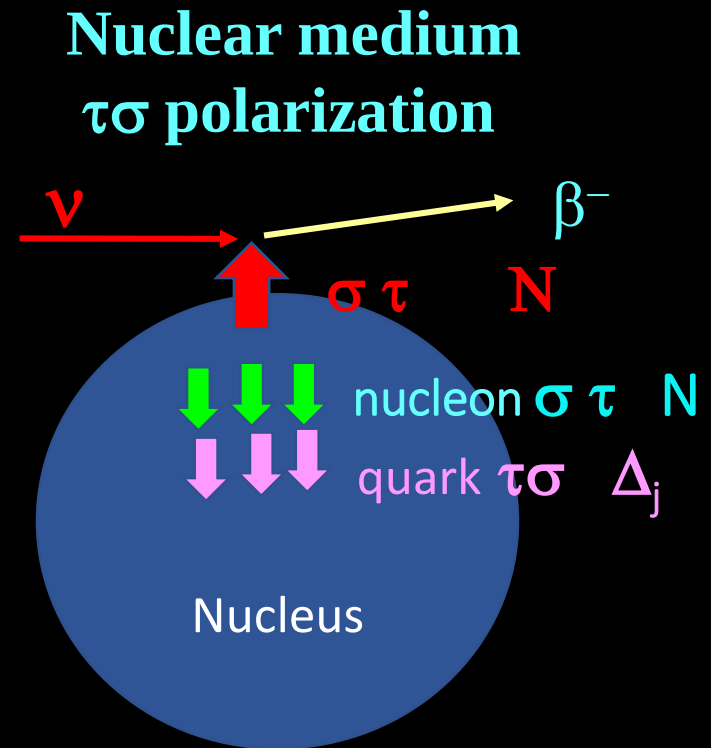
Weak int.: spin isospin $\tau\sigma$ $N^{-1}N$ GR and $N^{-1}\Delta$ GR



$$|I\rangle = |NP\rangle - \varepsilon |GRn\rangle - \delta |GR\Delta\rangle$$

$$M^{\beta \sim k^{\text{eff}}} M_0 \quad k^{\text{eff}} \quad (\tau\sigma) \sim 1/(1 + \chi_{\tau\sigma}) = 0.4$$

$k^{\text{eff}}(\Delta) \sim 0.6$ χ_{TS} : susceptibility

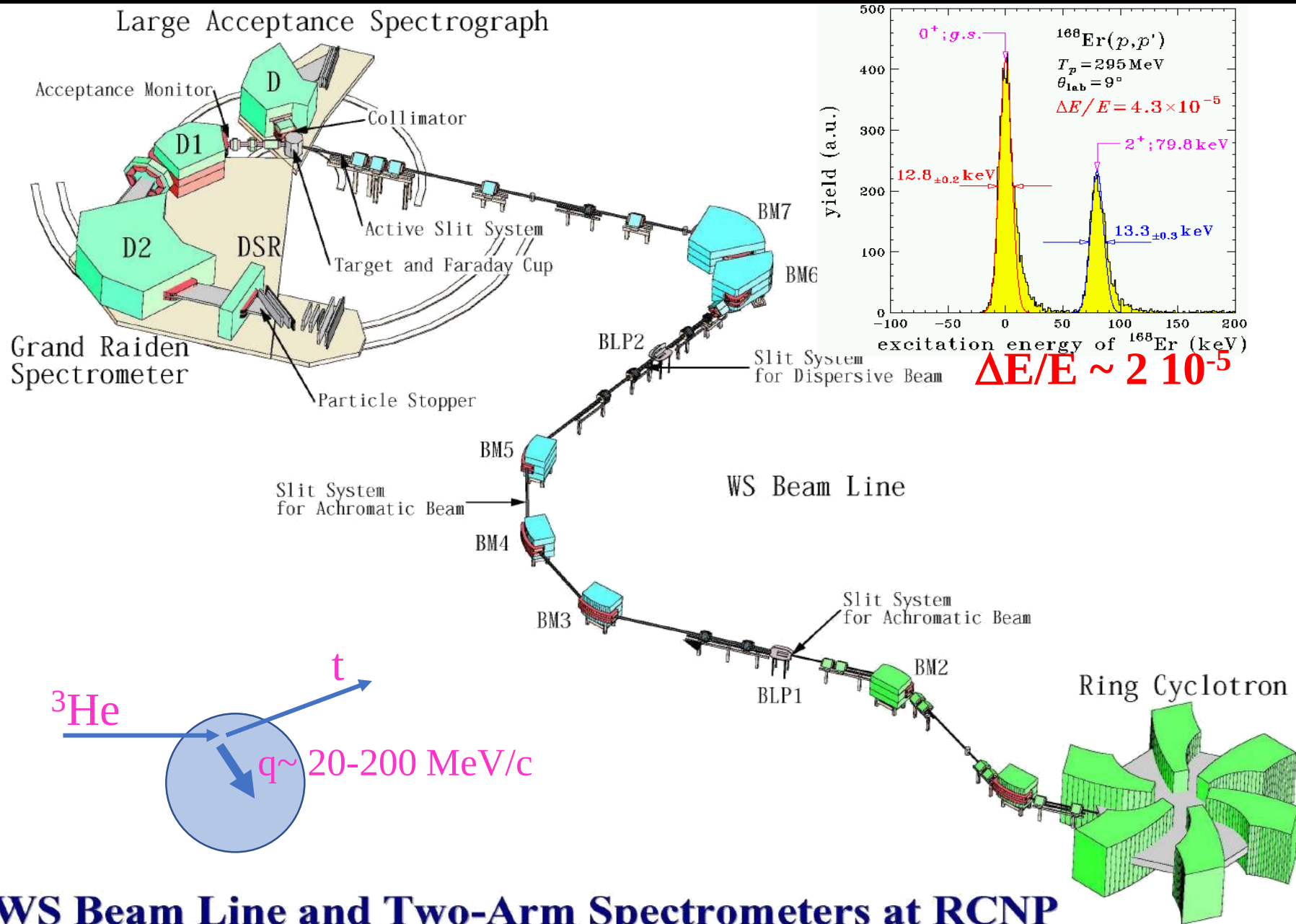


H. Ejiri PRC 26 '82 2628

Nuclear core change , Bohr¹⁺ Mottelson²⁻

PL B 10 '81 10 Isobar

High E resolution ($^3\text{He}, t$) CERs at RCNP Osaka



$$M(\text{SD } 2^-)_{\text{EXP}} = k M(\text{SD QP})$$

$$B(\text{SD}) = [\sigma(\text{SD})/\sigma(\text{IAS})]B(\text{IAS}) \quad \mathbf{K}, \quad B(\text{SD}) = M(\text{SD})^2$$

$\sigma(\text{SD})/\sigma(\text{IAS})$ for ^{76}Ge , $B(\text{IAS}) = N - Z$, and $\mathbf{K}$ is from the measured cross section ratio for ^{74}Ge with $B(\text{SD})$ from ft

	M(CER)	M (FSQP)
^{76}Ge (SD)	1.57 ± 0.24	2.1
^{128}Te (SD)	2.82 ± 0.48	3.4
^{130}Te (SD)	3.33 ± 0.59	3.7

$M(\text{ESQP})$ with $k \sim 0.25$ from ft data in neighboring nuclei.

H. Ejiri D. Frekers J. Physics G. Letters Sept.

$k \sim 0.25$, with 0.5 from $\tau\sigma$ and medium(g_A) effect 0.5

SD RCNP H. Akimune, H. Ejiri, RCNP Catania, Munster, KVI , • •