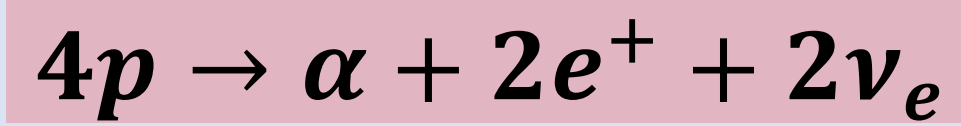


1. Introduction

◆ The Sun

- Energy generation via nuclear fusion reactions [1, 2].

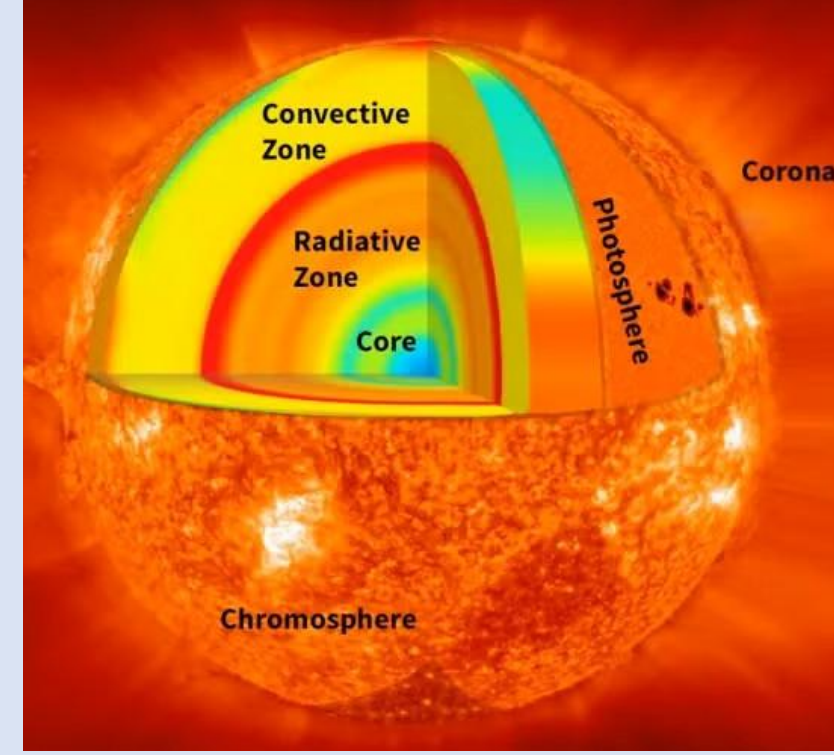


- Electron density, temperature, and metallicity profiles affects the production of solar neutrinos [3].

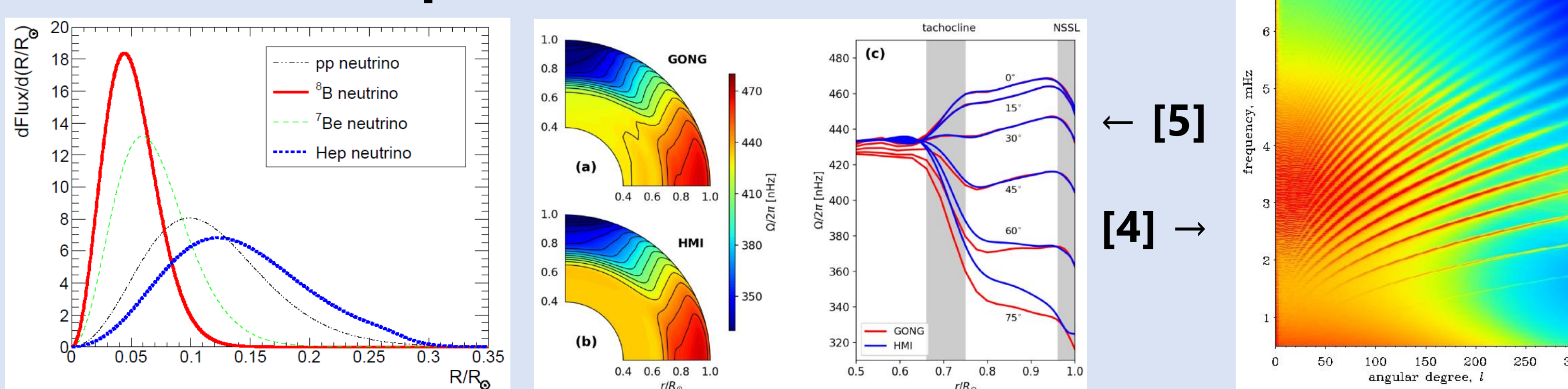
◆ Solar oscillations (p-modes and g-modes)

- **The Sun periodically oscillates** [4] →

Name	Reason	Region	Frequency
p-mode	Pressure	Surface	5 minutes
g-mode	Gravity	Core	1-3 hours



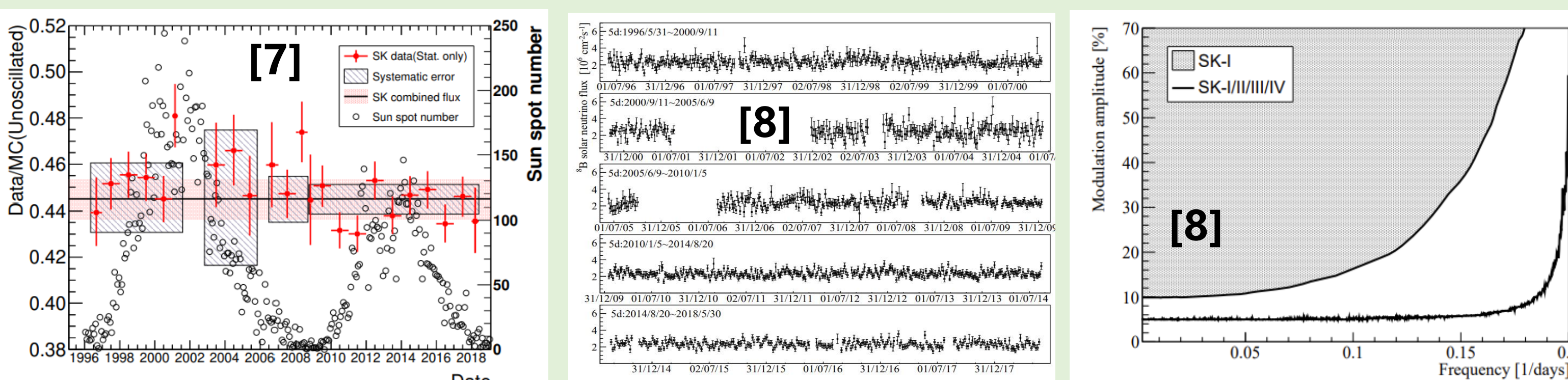
- Frequency measurements of solar p-modes reveal the 1-d sound speed profile and 2-d rotational profile, etc.
- However, **g-modes are not observed** because its amplitude is small at the surface.



2. Periodic change of solar ν

◆ Current situation of solar neutrino measurements

- The Super-Kamiokande detector has measured the solar ⁸B ν for more than 25 years [6, 7].
- **No periodic change is found** except for annual modulation. (< 5 days, amplitude < 5.2% (90% C.L.) [8]).



◆ Periodic amplification of solar ⁸B neutrinos

- G-modes have large amplitude in the core.
- Periodic change of local temperature.

- The energy (production rate of ⁸B ν) **strongly depends on the temperature** [9].

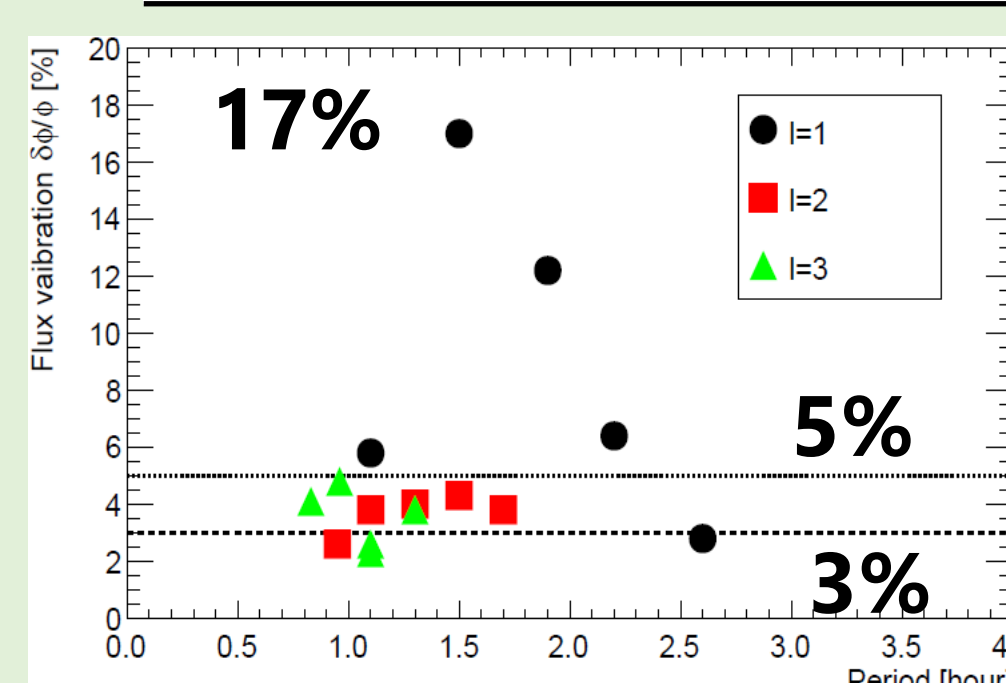
$$\frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \rho}{\rho} + \mu \frac{\delta T}{T}$$

ε : Produced energy
ρ : Density
T : Temperature

- Lopes (2014) [10] suggests that at most **~17% fluctuation of solar ⁸B ν** due to g-modes propagating in the core.

- SNO experiment sets the upper limit of amplitude as 11% for 1-3 hours [11].

Neutrino	Power Index (μ)
pp	[-1.1, -0.9]
pep	-1.4
⁷ Be	11
⁸ B	24~25
¹³ N, ¹⁵ O	20
¹⁷ F	23



3. Motivation and strategy

◆ Goal

- 1) **Search for solar g-mode oscillations using solar neutrinos** by evaluating its amplitude and frequency,
- 2) **Determine the density profile precisely in the core region.**
- 3) Set an upper limit of temperature fluctuation in the core.
- 4) **Improve the solar models by inputting g-mode results.**

◆ Strategy

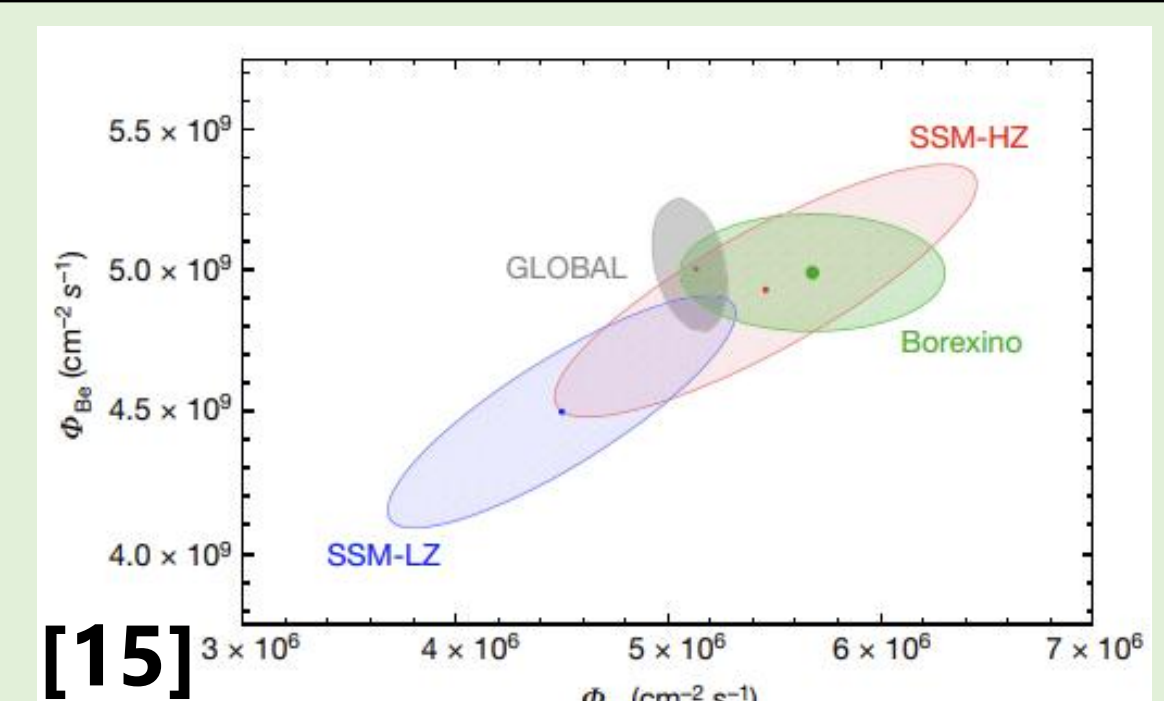
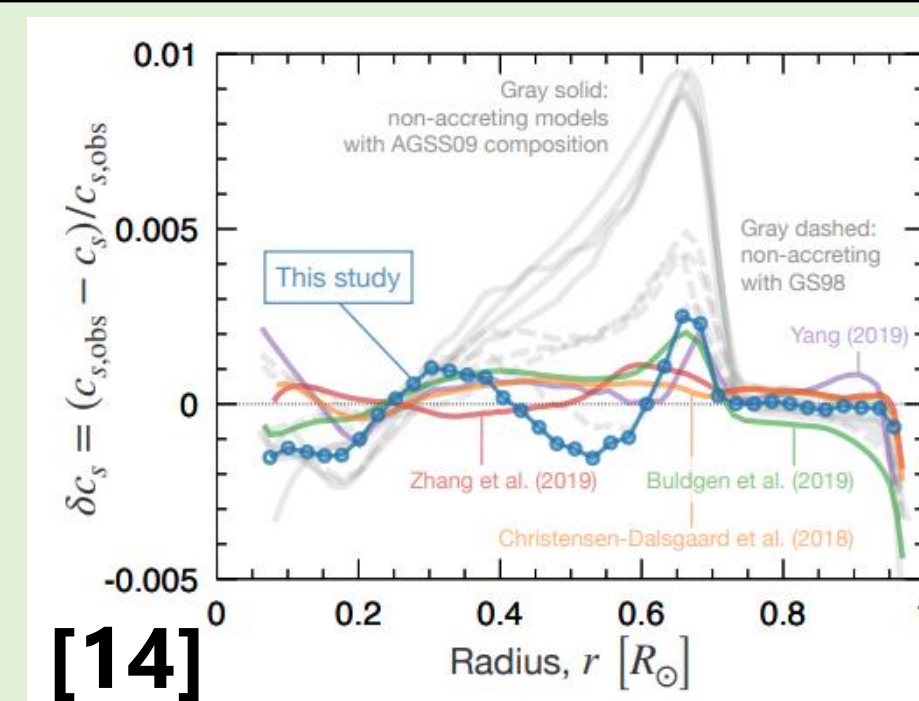
- i) Reproduce Ref. [10] method by using the latest solar models.
- ii) Make a catalog of amplitudes and frequencies of solar ν.
- iii) Search for periodic change of solar ν by neutrino detectors, such as Super-Kamiokande and Hyper-Kamiokande detectors.

4. Solar models

◆ Model construction and assumption

- The Sun is well studied star observationally and theoretically.
- We will test four solar models with different assumptions.

Model	Assumption	Characteristic
SSM-GS98 [12]	Standard solar model High metallicity at the surface (old)	--
SSM-A09 [13]	Standard solar model Low metallicity at the surface (New)	--
K2-A2-12 [14]	Low metallicity abundances opacity increases by ~12% around the base of the convective zone	Sound speed profile inside the Sun is well reproduced.
K2-MZvarA2-12 [14]	Considering the accretion flow to protostars	High metallicity inside the Sun Neutrino fluxes are well re-produced



5. Analysis and results

◆ Analysis scheme

- a) Adding the g-modes effect into the constant solar ν flux under its equilibrium state based on the perturbation theory.

$$\Phi_0 = \int_0^{M_\odot} \varphi_0(m) dm \xrightarrow{\delta T_{nl}(m, t), \delta \varphi_{nl}(m, t)} \Delta \varphi_{nl} = \int_0^{M_\odot} \delta \varphi_{nl}(m, t) dm$$

- b) Relating the neutrino production with temperature change.

$$\frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \rho}{\rho} + \mu \frac{\delta T}{T} \quad \frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \varphi}{\varphi} \quad \frac{\delta T}{T} = (\Gamma_3 - 1) \frac{\delta \rho}{\rho} \quad \frac{\delta \varphi}{\varphi} = \left(\frac{1}{\Gamma_3 - 1} + \mu \right) \frac{\delta T}{T}$$

Adiabatic oscillation, ideal gas $\Gamma_3 = 5/3$ at the core.

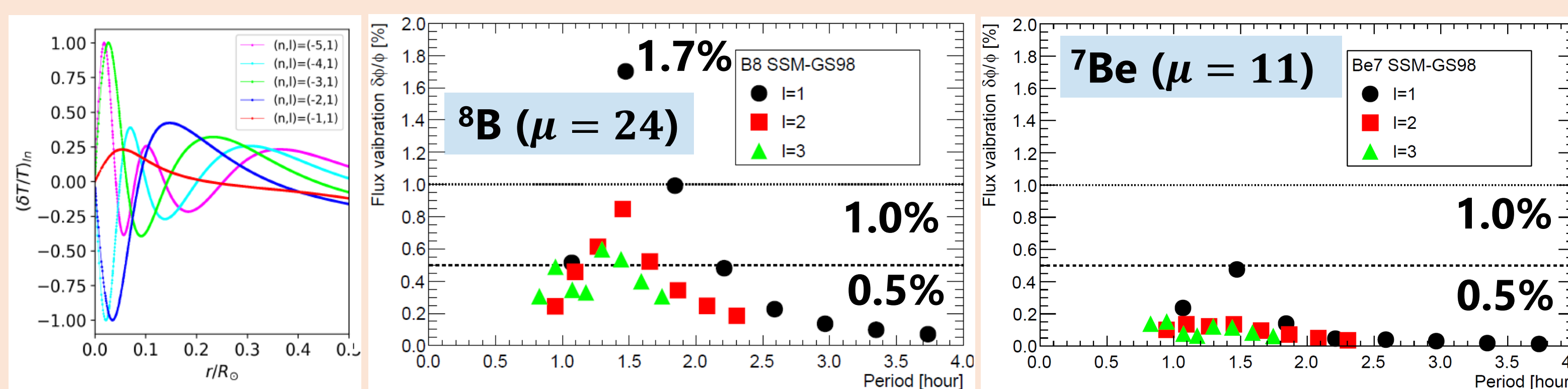
- c) Compute the neutrino flux fluctuations with δT_{nl} that are obtained by solving the eigenvalue problem.

$$\Delta \varphi_{nl}(t) = \Phi_0 \times \boxed{A_{nl}} \times \int_0^{R_\odot} \Phi_0^{-1}(\mu) \left[\frac{\delta T}{T}(r) \right]_{\text{Norm}} \varphi_0(r) \times 4\pi r^2 \rho dr \times e^{-i\omega_{nl}t}$$

We assumed the constant amplitude of A_{nl} because g-modes are not observed. (one "free" parameter in this analysis)

◆ Results and discussion

- We reproduced the solar ⁸B ν fluctuations while **its amplitude is 1/10** compared with the original method.
- Less than 2% of accuracy is required to search for this effect.
- **Hyper-Kamiokande can possibly detect?? (5-10 events/hour).**



- **Amplitude of solar ⁷Be neutrino is quite small.**
- May be difficult by Borexino, KamLAND, and JUNO detectors.

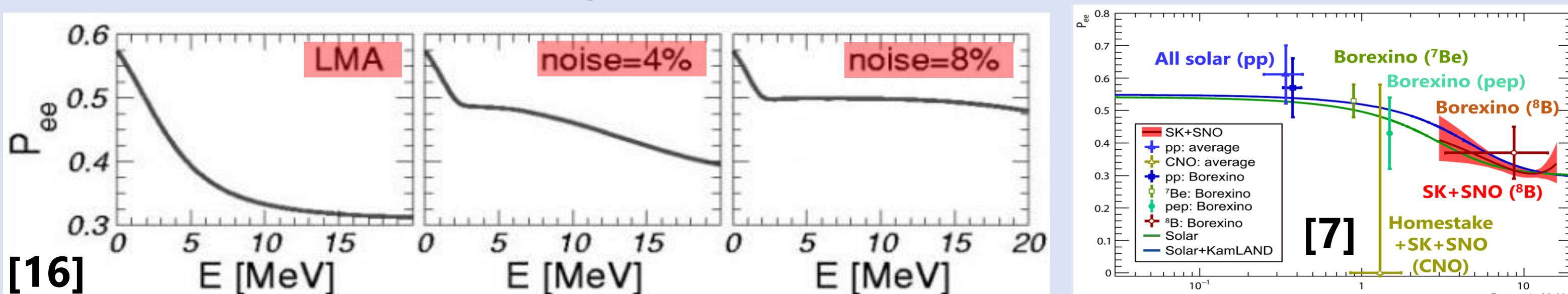
6. Summary and future prospect

◆ Summary

- Solar g-modes propagating inside the Sun is not observed.
- Search for this oscillation by solar neutrinos.
- Periodic amplification of solar neutrinos due to g-modes.
- **1.7% of solar ⁸B neutrinos** (detectable in Hyper-K detector).

◆ Prospects

- G-mode may affect the survival probability by MSW effect [16].
- We are also discussing the second-order effect.



Reference: [1] Phys. Rev. 54, 248 (1938) [2] Phys. Rev. 55, 434 (1939) [3] Mod. Phys. 54, 767 (1982) [4] SOHO (gallery) [5] Spa. Sci. Rev. 21, 77 (2023) [6] Phys. Rev. D 94, 052010 (2016) [7] Phys. Rev. D 109, 092001 (2024) [8] Phys. Rev. Lett. 132, 241803 (2024) [9] Phys. Rev. D 53, 4202 (1996) [10] Astrophys. J. Lett. 792, L35 (2014) [11] Astrophys. J. 710, 540 (2010) [12] Spa. Sci. Rev. 85, 161 (1998) [13] Annu. Rev. Astron. Astrophys. 47, 481 (2009) [14] A&A 655, A51 (2021) [15] Nature 562, 505 (2018) [16] Astrophys. J. 588, L65 (2003)