

Y. Nakano⁽¹⁾, Y. Hatta⁽²⁾, S. Sugama⁽³⁾, M. Kunitomo⁽⁴⁾, H. Ito⁽⁵⁾,
⁽¹⁾Univ. of Toyama (ynakano@sci.u-toyama.ac.jp),
⁽²⁾ISEE Nagoya Univ., ⁽³⁾Yokohama Natl. Univ., ⁽⁴⁾Kurume Univ., ⁽⁵⁾Kobe Univ.,



科研費
KAKENHI

基礎研究 (B) 24K00654
太陽内部構造と日食観測に基づく
太陽ニュートリノを用いた太陽g-mode振動探査

March 6th-7th 2026, 第11回「極低放射能技術」研究会 @ 神戸大学

1. Introduction

◆ The Sun

- Energy generation via nuclear fusion reactions [1, 2].

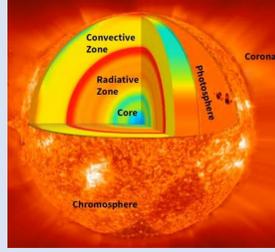


- Electron density, temperature, and metallicity profiles affects the production of solar neutrinos [3].

◆ Solar oscillations (p-modes and g-modes)

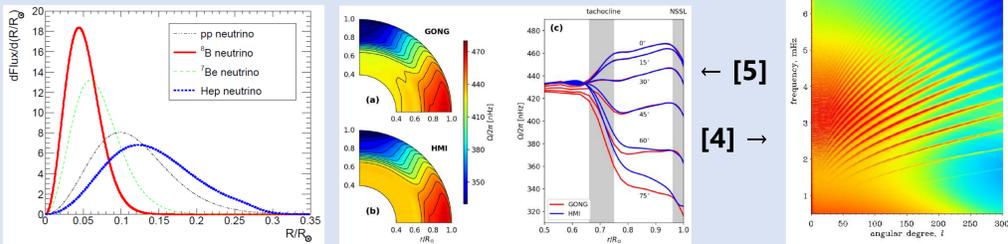
- **The Sun periodically oscillates** [4] →

Name	Reason	Region	Frequency
p-mode	Pressure	Envelope	5 minutes
g-mode	Gravity	Core	1-3 hours



→ Frequency measurements of solar p-modes reveal the 1-d sound speed profile and 2-d rotational profile, etc.

- However, **g-modes are not observed** because its amplitude is small at the surface.

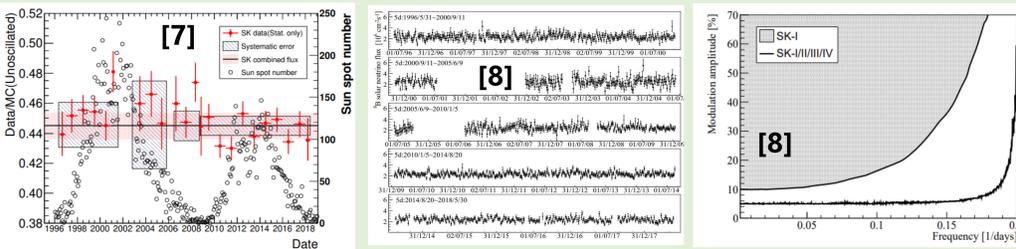


2. Periodic change of solar ν

◆ Current situation of solar neutrino measurements

- The Super-Kamiokande detector has measured the solar ⁸B ν for more than 25 years [6, 7].

→ **No periodic change is found** except for annual modulation. (< 5 days, amplitude < 5.2% (90% C.L.) [8]).



◆ Periodic amplification of solar ⁸B neutrinos

- G-modes have large amplitude in the core.
→ Periodic change of local temperature.

- The energy (production rate of ⁸B ν) **strongly depends on the temperature** [9].

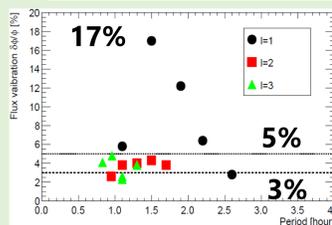
$$\frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \rho}{\rho} + \mu \frac{\delta T}{T}$$

ε : Produced energy
ρ : Density
T : Temperature

- Lopes (2014) [10] suggests that at most **~17% fluctuation of solar ⁸B ν** due to g-modes propagating in the core.

- SNO experiment sets the upper limit of amplitude as 11% for 1-3 hours [11].

Neutrino	Power Index (μ)
pp	[-1.1, -0.9]
pep	-1.4
⁷ Be	11
⁸ B	24~25
¹³ N, ¹⁵ O	20
¹⁷ F	23



3. Motivation and strategy

◆ Goal

- 1) **Detect solar g-mode oscillations using solar neutrinos** by evaluating its amplitude and frequency,
- 2) **Determine the density profile precisely in the core region.**
- 3) Set an upper limit of temperature fluctuation in the core.
- 4) **Improve the solar models by inputting g-mode results.**

◆ Strategy

- i) Reproduce Ref. [10] method by using the latest solar models.
- ii) Consider 2nd order effect to further study the g-modes.
- iii) Compare theoretical predictions with the experimental results and test our theory based on linear adiabatic oscillation.

4. Analysis

◆ Analysis scheme

a) Adding the g-modes effect into the constant solar ν flux under its equilibrium state based on the perturbation theory.

$$\Phi_0 = \int_0^{M_\odot} \varphi_0(m) dm \xrightarrow{\delta T_{nl}(m,t), \delta \varphi_{nl}(m,t)} \Delta \varphi_{nl} = \int_0^{M_\odot} \delta \varphi_{nl}(m,t) dm$$

b) Relating the neutrino production with temperature change.

$$\frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \rho}{\rho} + \mu \frac{\delta T}{T} \quad \frac{\delta \varepsilon}{\varepsilon} = \frac{\delta \varphi}{\varphi} \quad \frac{\delta T}{T} = (\Gamma_3 - 1) \frac{\delta \rho}{\rho} \quad \frac{\delta \varphi}{\varphi} = \left(\frac{1}{\Gamma_3 - 1} + \mu \right) \frac{\delta T}{T}$$

Adiabatic oscillation, ideal gas $\Gamma_3 = 5/3$ at the core.

c) Compute the neutrino flux fluctuations with δT_{nl} that are obtained by solving the eigenvalue problem.

$$\Delta \varphi_{nl}(t) = \Phi_0 \times \mathcal{A}_{nl} \times \int_0^{R_\odot} \Phi_0^{-1}(\mu) \left[\frac{\delta T}{T}(r) \right]_{\text{Norm}} \varphi_0(r) \times 4\pi r^2 \rho dr \times e^{-i\omega_{nl}t}$$

We assumed the constant amplitude of \mathcal{A}_{nl} because g-modes are not observed. (one "free" parameter in this analysis)

5. Results

◆ Results and discussion

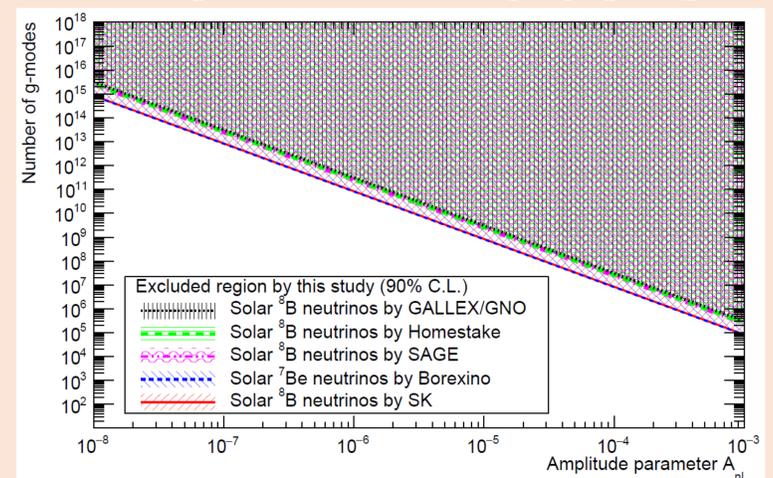
- First order calculation **predicts no periodic change** because of geometrical cancellation.
→ We suspect Lopes (2014) [10] may not consider this effect.

- Second order calculation predicts the **change of neutrino flux with the 11-year solar cycle.**
→ Possibly caused by the **change in how g-modes are excited/damped by turbulent convection.**

- We analyzed the solar neutrino results by SK [8], Borexino [12], Homestake [13], SAGE [14] and GALLEX/GNO [15, 16].

- Set an experimental constraint on the # of g-mode oscillations.
→ **SK result gives the strongest limit: $< 7.8 \times 10^7$ at $A_{nl} = 10^{-5}$.**

- Long term operation of the neutrino detector is important to search for the g-mode oscillations propagating in the Sun.



6. Summary and future prospect

- Solar g-modes propagating inside the Sun is not observed.
→ Search for this oscillation by solar neutrinos.

- No periodic amplification of solar neutrinos due to g-modes is expected by our 1st order calculation.

- Long term measurement with small fluctuation of background is important to search for the g-mode oscillations.

Reference: [1] Phys. Rev. 54, 248 (1938) [2] Phys. Rev. 55, 434 (1939) [3] Mod. Phys. 54, 767 (1982) [4] SOHO (gallery) [5] Spa. Sci. Rev. 21, 77 (2023) [6] Phys. Rev. D 94, 052010 (2016) [7] Phys. Rev. D 109, 092001 (2024) [8] Phys. Rev. Lett. 132, 241803 (2024) [9] Phys. Rev. D 53, 4202 (1996) [10] Astrophys. J. Lett. 792, L35 (2014) [11] Astrophys. J. 710, 540 (2010) [12] Astropart. Phys. 145, 102778 (2023) [13] Astrophys. J. 496, 505 (1998) [14] Phys. Rev. C 80, 015807 (2009) [15] Phys. Lett. B 447, 127 (1999) and reference there in [16] Phys. Lett. B 616, 174 (2005)